

A triangle has vertices A(-6, 3), B(5, 7) and C(-1, 2).

- find equation of the median from vertex A
- find equation of the median from vertex B
- find the intersection point of medians from vertex A and vertex B (Note: this point is called the Centroid)

$$a) M_{Bc} = \left(\frac{5+(-1)}{2}, \frac{7+2}{2} \right) = (2, 4.5)$$

$$\text{Slope: } AM_{Bc} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{4.5 - 3}{2 - (-6)} = \frac{1.5}{8} = \frac{3}{16} = m$$

$$(-6, 3) \quad (2, 4.5)$$

$$x_1, y_1 \quad x_2, y_2$$

$$y = mx + b \quad (-6, 3) \quad m = \frac{3}{16}$$

$$x \quad y$$

$$3 = \frac{3}{16}(-6) + b$$

$$3 = \frac{-18}{16} + b$$

$$3 = -\frac{9}{8} + b$$

$$3 + \frac{9}{8} = b$$

$$\frac{33}{8} = b$$

$$y = \frac{3}{16}x + \frac{33}{8}$$

c) Solve (PoI) of

$$y = \frac{3}{16}x + \frac{33}{8}$$

$$y = \frac{9}{17}x + \frac{74}{17}$$

$$\frac{272}{1} \left(\frac{3}{16}x + \frac{33}{8} \right) = \left(\frac{9}{17}x + \frac{74}{17} \right) \times \frac{272}{1}$$

$$51x + 1122 = 144x + 1184$$

$$\frac{-62}{93} = \frac{93x}{93}$$

$$-\frac{2}{3} = x$$

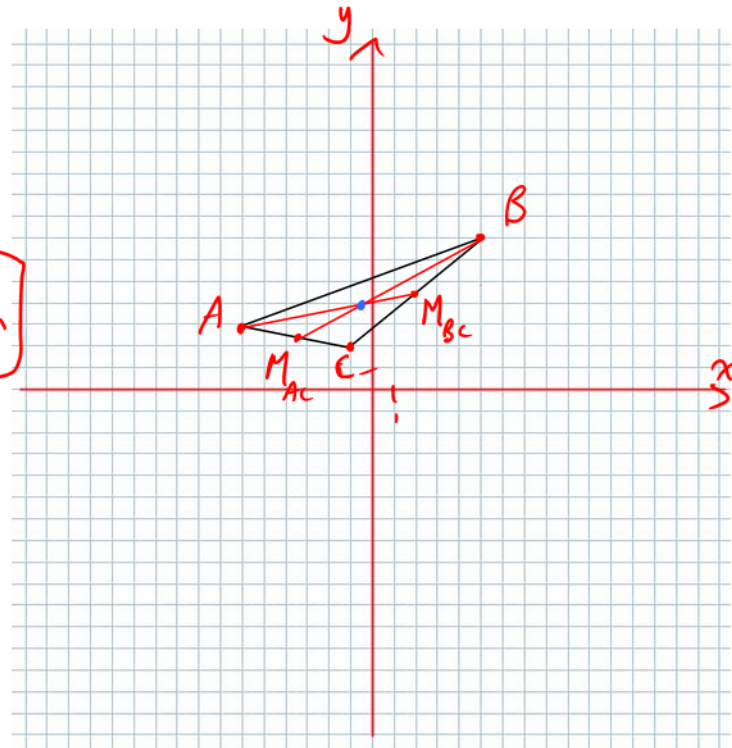
$$y = \frac{3}{16} \left(-\frac{2}{3} \right) + \frac{33}{8}$$

$$y = -\frac{1}{8} + \frac{33}{8}$$

$$y = +\frac{32}{8}$$

$$y = +4$$

∴ The PoI is $\left(-\frac{2}{3}, +4 \right)$



$$b) M_{Ac} = \left(\frac{-6+(-1)}{2}, \frac{3+2}{2} \right) = (-3.5, 2.5)$$

$$(-3.5, 2.5) \quad (5, 7)$$

$$\text{Slope } BM_{Ac} : m = \frac{7 - 2.5}{5 - (-3.5)} = \frac{4.5}{8.5} = \frac{9}{17}$$

$$Eqn: (5, 7) \quad m = \frac{9}{17}$$

$$7 = \frac{9}{17}(5) + b$$

$$7 = \frac{45}{17} + b$$

$$7 - \frac{45}{17} = b$$

$$\frac{119}{17} - \frac{45}{17} = b$$

$$\frac{74}{17} = b$$

$$y = \frac{9}{17}x + \frac{74}{17}$$

