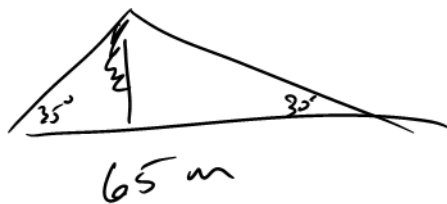


Bonus: #11 pg 413 \rightarrow hand in.



The Sine Law

Sometime^s using a right angle triangle just can't be done and then SOH CAH TOA doesn't work!!! In that case need to use so-called "**OBLIQUE TRIANGLES**". Oblique triangles come in two forms:

- 1) Acute (all angles are less than 90°)
- 2) Obtuse (one angle is more than 90°)

In Grade 10 we will focus on Acute Triangles.

The Sine Law (for *oblique* triangles)

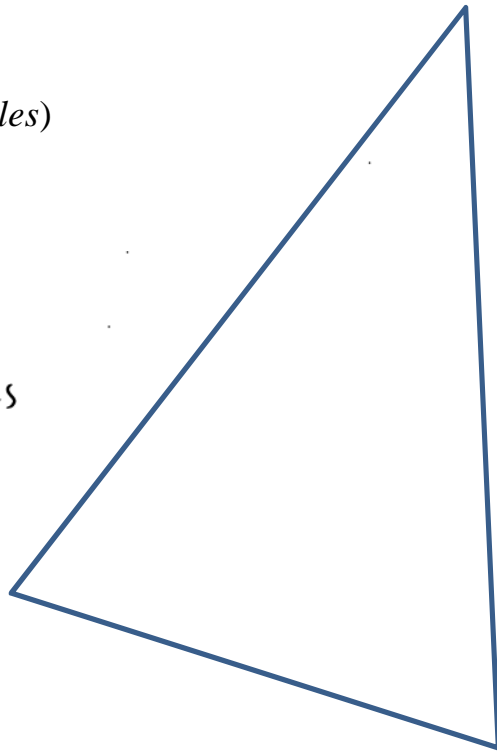
(There are **TWO FORMS** you should know!!)

Given the **non-right triangle**, $\triangle ABC$, then:

$$\frac{\sin(A)}{a} = \frac{\sin(B)}{b} = \frac{\sin(C)}{c} \left. \vphantom{\frac{\sin(A)}{a} = \frac{\sin(B)}{b} = \frac{\sin(C)}{c}} \right\} \text{angles}$$

or

$$\frac{a}{\sin(A)} = \frac{b}{\sin(B)} = \frac{c}{\sin(C)} \left. \vphantom{\frac{a}{\sin(A)} = \frac{b}{\sin(B)} = \frac{c}{\sin(C)}} \right\} \text{sides}$$

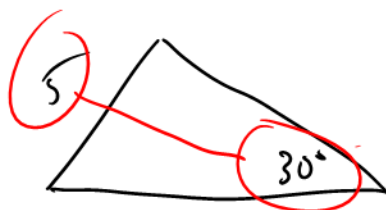


Notes:

- 1) Memorize the SINE LAW!
- 2) If we are trying to **find an angle**, use the first form of the Sine Law (**angles on top**)
- 3) If we are trying to **find the length** of a side, use the second form of the law (**with sides on top**)
- 4) In order to use the Sine Law, you must have the correct information in the triangle. You must have:

- a) 3 pieces of information
- b) One "**CORRESPONDING PAIR**" – an angle with its opposite side (for example you might have side a and angle A)

ASA
ASS
SAA

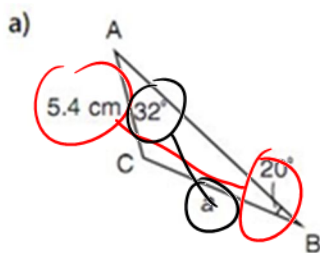


* need a bar bell

★ start with your unknown

Example 8.2.1

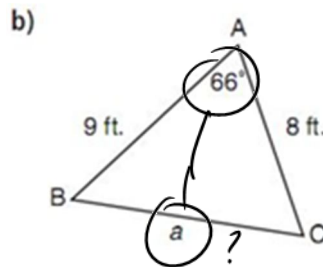
If you can use the Sine Law, determine the length of side a . If you can't use the Sine Law, say why.



$$\sin 32^\circ \times \left(\frac{a}{\sin 32^\circ} \right) = \left(\frac{5.4}{\sin 20^\circ} \right) \times \sin 32^\circ$$

$$a = \left(\frac{5.4}{\sin 20^\circ} \right) \times \sin 32^\circ$$

$$a = 8.4 \text{ cm}$$

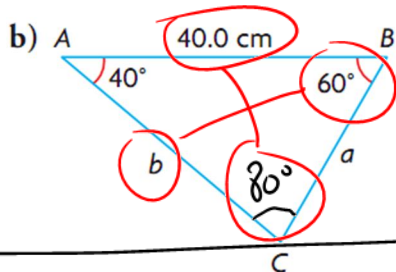


We don't have an angle and its opposite side.

Example 8.2.2

From your Text: Pg. 433 #3b) e)

Determine the unknown sides and/or angles



$$\sin 60^\circ \times \left(\frac{b}{\sin 60^\circ} \right) = \left(\frac{40}{\sin 80^\circ} \right) \times \sin 60^\circ$$

$$b = \left(\frac{40}{\sin 80^\circ} \right) \times \sin 60^\circ$$

$$b = 35.2 \text{ cm}$$

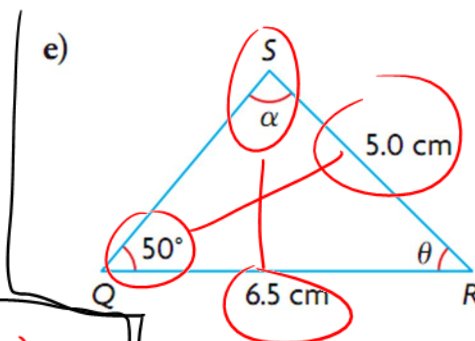
$$\sin 40^\circ \times \left(\frac{a}{\sin 40^\circ} \right) = \left(\frac{40}{\sin 80^\circ} \right) \times \sin 40^\circ$$

$$a = \left(\frac{40}{\sin 80^\circ} \right) \times \sin 40^\circ$$

$$a = 26.1 \text{ cm}$$

$$\angle R = 180 - 50 - 84.8$$

$$\angle R = 45.2^\circ$$



$$6.5 \times \left(\frac{\sin S}{6.5} \right) = \left(\frac{\sin 50^\circ}{5} \right) \times 6.5$$

$$\sin S = \left(\frac{\sin 50^\circ}{5} \right) \times 6.5$$

$$\sin S = 0.99586$$

★ have at least 4 decimals.

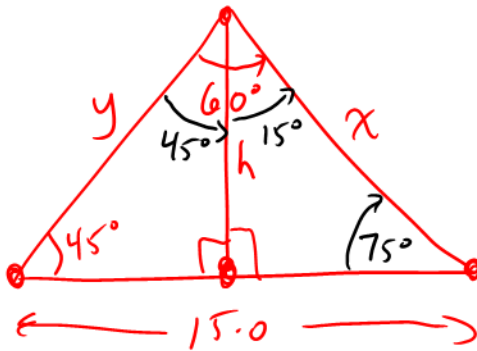
$$\angle S = \sin^{-1}(0.99586)$$

$$\angle S = 84.8^\circ$$

Example 8.2.3

From your Text: Pg. 434 #9

A telephone pole is supported by two wires on opposite sides. At the top of the pole, the wires form an angle of 60° . On the ground, the ends of the wires are 15.0 m apart. One wire makes a 45° angle with the ground. How long are the wires, and how tall is the pole?



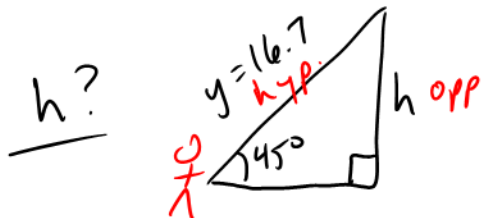
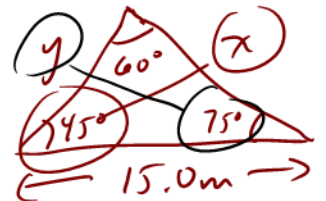
Wires are x and y

$$\sin 45^\circ \left(\frac{x}{\sin 45^\circ} \right) = \left(\frac{15.0}{\sin 60^\circ} \right) \times \sin 45^\circ$$

$$x = 12.2 \text{ m} \quad \checkmark$$

$$\sin 75^\circ \left(\frac{y}{\sin 75^\circ} \right) = \left(\frac{15.0}{\sin 60^\circ} \right) \times \sin 75^\circ$$

$$y = 16.7 \text{ m} \quad \checkmark$$



$$\sin 45^\circ \quad 16.7 \times (\sin 45^\circ) = \left(\frac{h}{16.7} \right) \times 16.7$$

$$11.8 \text{ m} = h$$

Sentence

for monday.

Test

Thurs.
Nov 5