

## Multiplying and Dividing Rational Expressions

**Multiply: Factor, cross out common factors, rewrite, then state restrictions from denominator.**

$$1) \frac{3x-21}{x^2-11x+28} \times \frac{x^2-3x-4}{3x+3}$$

$$= \frac{\cancel{3(x-7)}}{(\cancel{x-7})(\cancel{x-4})} \times \frac{(\cancel{x-4})(\cancel{x+1})}{\cancel{3(x+1)}}$$

$$= 1 \quad \{x \neq -1, 4, 7\}$$

$$3) \frac{p+7}{p^2-11p+30} \cdot \frac{6p+42}{p^2+14p+49}$$

$$2) \frac{10a^2-10a}{a^2-2a+1} \times \frac{a^2+9a-10}{a^2+19a+90}$$

$$= \frac{10a(a-1)}{(a-1)(a+1)} \times \frac{(a+10)(a-1)}{(a+9)(a+10)}$$

$$= \frac{10a}{(a+9)} \quad \{a \neq -10, -9, 1\}$$

$$4) \frac{x^2-2x-48}{x^2-6x-16} \cdot \frac{5x+10}{5x-40}$$

$$5) \frac{r^2-9r+14}{r-7} \cdot \frac{9r^2+81r}{r^2+16r+63}$$

$$6) \frac{x^2-9x+14}{10x-20} \cdot \frac{10x-70}{x^2-8x+7}$$

$$7) \frac{x^2 - 9}{x^2 + 2x - 3} \cdot \frac{x^2 + 8x - 9}{x^2 + 18x + 81}$$

$$8) \frac{8n^2}{n^2 - 9n + 8} \cdot \frac{n^2 - 7n + 6}{3n - 18}$$

**Divide: Factor, flip second fraction and change to multiply. Reduce, rewrite, then state restrictions from first denominator and ENTIRE second fraction.**

$$9) \frac{6v+48}{v+8} \div \frac{28v-20}{56v^2-40v} \quad \cancel{\neq 0}$$

$$= \frac{6(v+8)}{(v+8)} \times \frac{8v^2(v-5)}{4(2v-5)}$$

$$= 12v \quad \left\{ v \neq -8, 0, \frac{5}{2} \right\}$$

$$11) \frac{n^2 + 2n - 80}{6n + 60} \div \frac{n^2 - 17n + 72}{\underline{n^2 - 81}} \\ (n+9)(n-9)$$

$$10) \frac{n^2 - 5n - 14}{24n^2 + 40n} \div \frac{n^2 + 7n + 10}{24n^2 + 40n}$$

$$= \frac{(n-7)(n+2)}{8n(3n+5)} \times \frac{8n(3n+5)}{(n+2)(n+5)}$$

$$= \frac{(n-7)}{(n+5)} \quad \left\{ n \neq -5, -2, \frac{-5}{3}, 0 \right\}$$

$$12) \frac{x^2 - 9x + 18}{x^2 - 64} \div \frac{x^2 - 2x - 3}{x + 8}$$

$$13) \frac{n^2 - 5n + 4}{6n - 6} \div \frac{8n - 32}{6n + 54}$$

$$14) \frac{8m - 24}{m^2 + 4m - 21} \div \frac{8}{2m + 14}$$

$$15) \frac{3x + 18}{x^2 - x - 2} \div \frac{3x + 15}{x^2 + 6x + 5}$$

$$16) \frac{63}{r^2 - 6r + 9} \div \frac{r + 5}{r^2 + 2r - 15}$$

$$17) \frac{9x + 36}{9} \div \frac{x^2 - 4}{x^2 - 5x - 14}$$

$$18) \frac{x^2 - 64}{6x - 48} \div \frac{x + 9}{6x + 54}$$

**Multiply.**

$$19) \frac{10x^2 - 53x + 36}{16x^2 - 72x} \cdot \frac{8x^2 + 40x}{5x^2 + 46x - 40}$$

$$20) \frac{7r^2 - 59r + 70}{21r^2 + 40r - 100} \cdot \frac{21r^2 + 64r - 20}{63r - 18}$$

**Divide.**

$$21) \frac{14n^2 - 11n + 2}{18n^3 - 9n^2} \div \frac{49n - 14}{2n}$$

$$22) \frac{2n^2 + 26n + 72}{5n - 50} \div \frac{14n^2 + 42n - 56}{35n - 35}$$