

## Three Primary and Three Reciprocal Ratios.

$$\sin \theta = \frac{\text{opposite}}{\text{hypotenuse}}$$

$$\csc \theta = \frac{\text{hypotenuse}}{\text{opposite}}$$

"cosecant"

$$\cos \theta = \frac{\text{adjacent}}{\text{hypotenuse}}$$

$$\sec \theta = \frac{\text{hypotenuse}}{\text{adjacent}}$$

"secant"

$$\tan \theta = \frac{\text{opposite}}{\text{adjacent}}$$

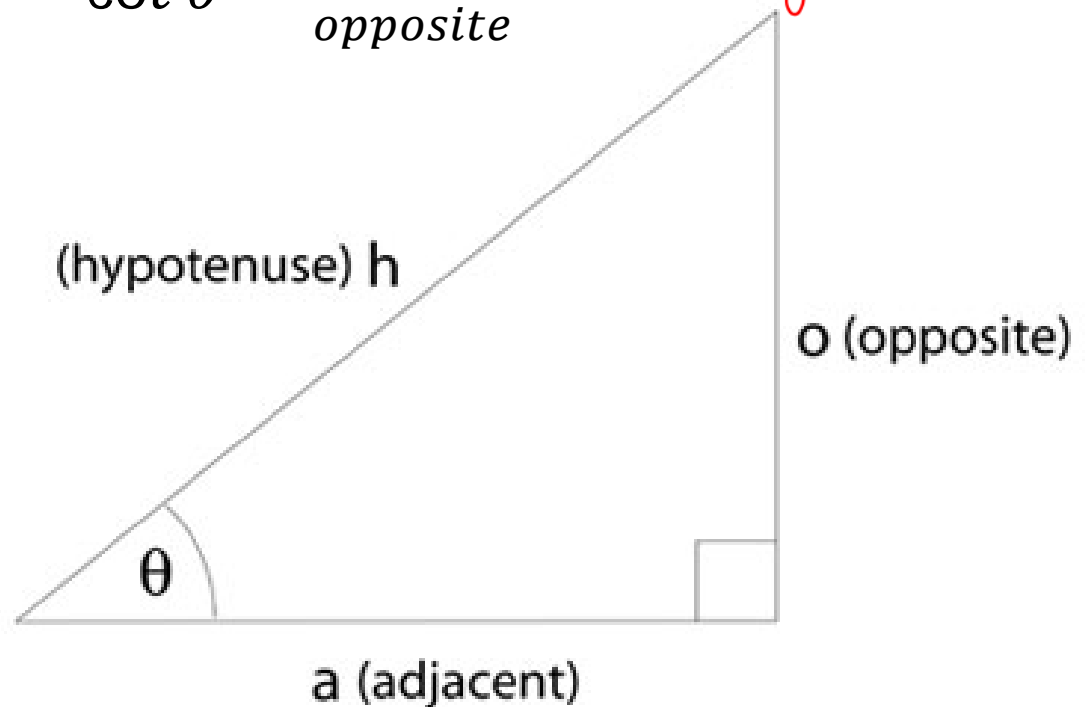
$$\cot \theta = \frac{\text{adjacent}}{\text{opposite}}$$

"cotangent"

$$\csc \theta = \frac{1}{\sin \theta}$$

$$\sec \theta = \frac{1}{\cos \theta}$$

$$\cot \theta = \frac{1}{\tan \theta}$$



There are no *csc*, *sec*, *cot* buttons on the calculator!

Determine the following ratios:

$$1. \sin 36^\circ \\ = 0.5878$$

$$2. \csc 86^\circ = \frac{1}{\sin 86} = 1.0024$$

$$3. \sec 23^\circ \\ = \frac{1}{\cos 23} = 1.0864$$

$$4. \cot 75^\circ \\ = \frac{1}{\tan 75} = 0.2679$$

Determine the following angles:

1.  $\cos \theta = 0.2745$

$$\theta = \cos^{-1}(0.2745)$$

$$\theta = 79^\circ$$

3.  $\csc \theta = 1.2241$

$$\sin \theta = \frac{1}{1.2241}$$

$$\theta = \sin^{-1}\left(\frac{1}{1.2241}\right)$$

$$\theta = 55^\circ$$

2.  $\sec \theta = 3.2471$

$$\frac{1}{\cos \theta} = 3.2471$$

$$\frac{1}{3.2471} = \cos \theta$$

$$\cos^{-1}\left(\frac{1}{3.2471}\right) = \theta$$
$$72^\circ = \theta$$

4.  $\cot \theta = 5.3267$

$$\tan \theta = \frac{1}{5.3267}$$

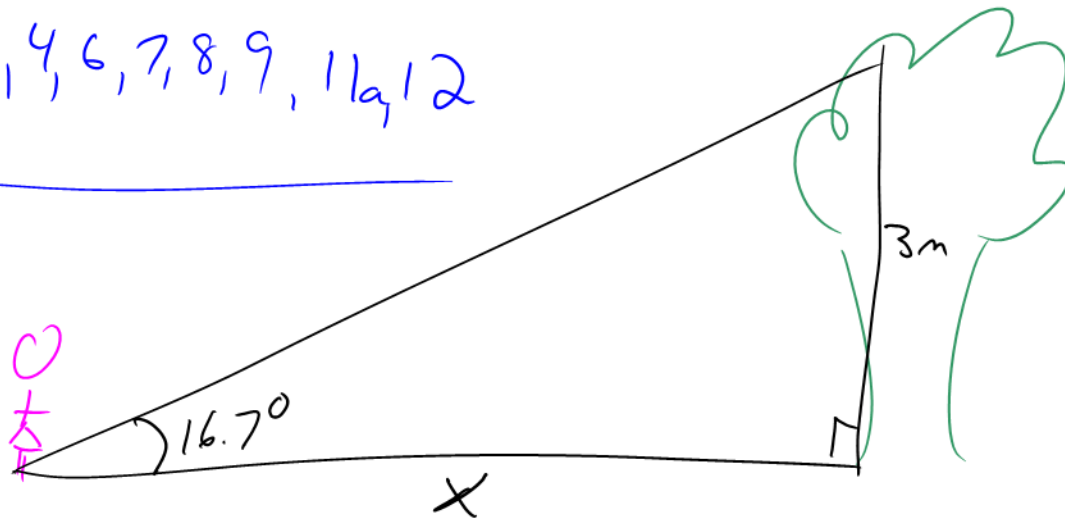
$$\theta = \tan^{-1}\left(\frac{1}{5.3267}\right)$$

$$\theta = 11^\circ$$

### A word problem:

From a position some distance away from the base of a tree, Monique uses a clinometer and determines that the angle of elevation to the top of the tree is  $16.7^\circ$ . Monique estimates that the high of the tree is 3m. How far away is Monique from the base of the tree?

Hw pg 280 # 1, 4, 6, 7, 8, 9, 11, 12



$$\tan 16.7^\circ = \frac{3}{x}$$

~~$$\cot 16.7^\circ = \frac{x}{3}$$~~

$$x = \frac{3}{\tan 16.7^\circ} \rightarrow x = 10 \text{ m}$$