

The key to creating equations:

$$f(x) = a \sin(k(x - d)) + c$$

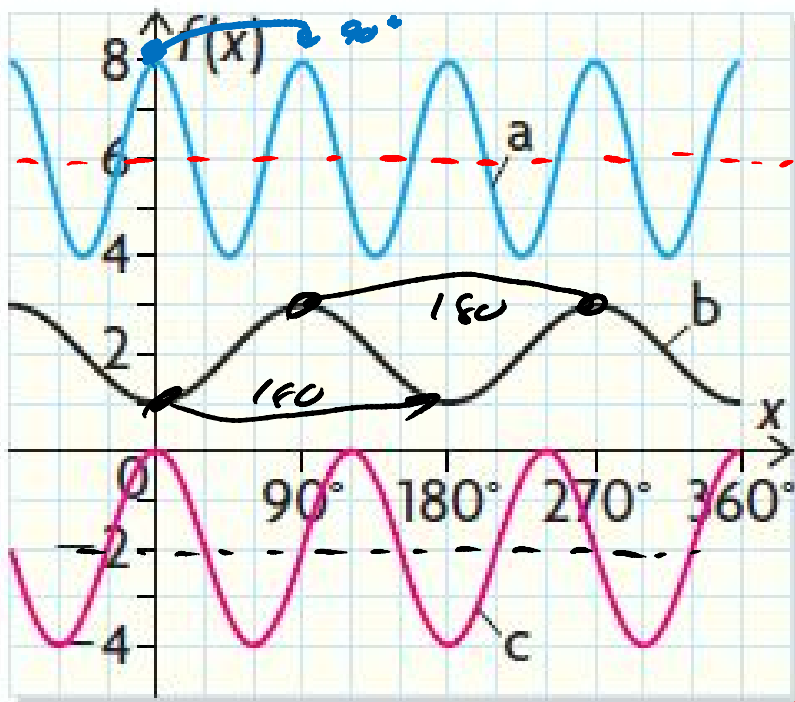
Amplitude = a, found by *peak-EoA*

$$\text{Period} = \frac{360^\circ}{k} \quad \text{therefore } k = \frac{360}{\text{Period}}$$

Phase Shift = d – this is your “starting point” – must be peak, EoA or trough

Equation of Axis = c, found by $\frac{\text{peak} + \text{trough}}{2}$

	Starting at...
+sin	Equation of axis, then heads to peak
-sin	Equation of axis, then heads to trough
+cos	Peak
-cos	Trough



a) Peak = 8 Trough = 4

$$\therefore EoA = \frac{8+4}{2} = 6 \rightarrow \underline{c}$$

Amplitude: $8 - 6 = 2 \underline{a}$

Period: $90^\circ \therefore \underline{k} = \frac{360}{90} = 4$

Because Peak is on y-axis, use cosine with $d=0$

$$f(x) = 2 \cos(4x) + 6 \quad \underline{\text{or}}$$

$$f(x) = 2 \cos(4(x-180)) + 6$$

b) Peak = 3 Trough = 1

$$\therefore EoA = \frac{3+1}{2} = 2 \underline{c}$$

Amplitude = $3 - 2 = 1 \underline{a}$

Period: $180 \therefore \underline{k} = \frac{360}{180} = 2$

$$f(x) = -1 \cos(2x) + 2$$

$$\text{or } f(x) = 1 \cos(2(x-90)) + 2$$

c) Peak = 0, Trough = -4 $\therefore EoA = -2$

Amplitude: 2

Period: $120 \therefore k = \frac{360}{120} = 3$

$$f(x) = 2 \sin(3(x-90)) - 2$$

x	0°	45°	90°	135°	180°	225°	270°
y	9	7	5	7	9	7	5

Peak: 9

Trough: 5

EoA: 7

Amp: 2

Period: 180°

$$k = \frac{360}{180} = 2$$

$$f(x) = 2\cos(2x) + 7$$

$$f(x) = -2\sin(2(x - 225)) + 7$$

A sinusoidal function has an amplitude of 4 units, a period of 120°, and a maximum at (0,9). Determine the equation of the function.

Amp = 4

Period: 120 ∴ $k = \frac{360}{120} = 3$

Peak = 9

$$EoA = 9 - 4 = 5$$

$d = 0$

$$\therefore f(x) = 4\cos(3x) + 5$$

pg 391 # 4,5,6,7,8,11

pg 398 # 1,2,3,5,6

A group of students is tracking a friend, John, who is riding a Ferris wheel. They know that John reaches a maximum height of 11m at 10s and then reaches a minimum height of 1m at 55s. How high is John after 2 minutes?