

Problems Involving Quadratic Relations in Factored Form

Example 1

The profit of a chocolate bar can be modeled by the equation $P = -0.3(n - 7)^2 + 10.8$, where P is the profit in Thousands of dollars and n is the number of chocolates sold in thousands.

a) What is the coordinates of the vertex? Explain what it represents

b) What is the y-intercept? Explain what it represents

c) What are the zeros? Explain what they represent.

UNDERSTANDING PROBLEMS

RELATED TO FACTORED FORM

- draw sketches to help visualize the situation
- consider how key features relate to the context of the problem:
 - initial point = _____
 - break-even points/distance/time/etc. = _____
 - max/min profit/distance/height/etc. = _____
 - point at which max/min occurs = _____

Example 2

The path of a soccer ball can be modelled by the relation $h = -0.1d^2 + 0.5d + 0.6$, where h is the ball's height and d is the horizontal distance from the kicker. Both measured in meters.



- a. Find the zeros of the relation.

- b. What do the zeros mean in the context of the question?

Example 3

The arch of a small suspension bridge over a gorge can be modelled by the equation $y = -2x^2 + 4x + 6$ where x is the distance in meters from the edge of the gorge and y is the height above the ground, also in meters.



- a. What are the zeros? What do they represent?

- b. How long is the bridge? Justify your answer.

Example 4

A rider on a mountain bike jumps off a ledge. Her path is modelled by the relation $h = -0.3d^2 + 1.2d + 1.5$, where h is her height above the ground and d is her horizontal distance from the ledge, both in metres.

- a. What is the height of the ledge?
- b. How far was the rider from the ledge when she landed?

