



# Theoretical Probability

**Probability** is used to predict the outcomes of various events. It is the chance of something happening.

Probability is used to make predictions about \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_.

Probabilities can be written in 3 ways:

			Example 1	Example 2		
i. as a fraction	$\frac{\text{\# of successful attempts}}{\text{total \# of attempts}}$		$\frac{1}{2}$			$\frac{\text{\# of successful attempts}}{\text{total \# of attempts}}$
ii. as a decimal	divide the fraction to convert to percent					use place value to convert to fraction
iii. as a percent	multiply by 100 to convert to percent			60%		divide by 100 to convert to decimal

When two or more things have the same probability of happening, they are considered to have **equally likely outcomes**.

**Theoretical Probability** is the chance of something happening in a perfect world. It can be calculated using the formula:

$$P = \frac{\text{\# of favourable outcomes}}{\text{\# of possible outcomes}}$$

## Example 1

A number from 1 to 50 inclusive is chosen at random. What is the probability that the number . . .

a. is even?		b. ends in a 3?	
c. is odd?		d. does not end in a 3?	
e. is greater than 13?		f. is prime?	
g. is divisible by 5?		h. has 2 digits the same?	

**Example 2**

The Toronto Maple Leafs are playing the Detroit Redwings in the 2003 Stanley Cup Finals. The probability of the Maple Leafs winning are  $\frac{4}{11}$ .

- a. What is the probability of each team winning a single game? Write your answers as percentages.
  
  
  
  
  
  
  
  
  
  
- b. If these teams were to play 6 games, how many is each expected to win?

**Example 3**

Suppose you toss a coin three times.

- a. Which event do you think is more likely: you get 3 heads, or you get 1 head and 2 tails? Explain your thinking.
  
  
  
  
  
  
  
  
  
  
- b. Draw a tree diagram to show the possible outcomes when a coin is tossed three times. Are the outcomes equally likely?
  
  
  
  
  
  
  
  
  
  
- c. Use your diagram to determine the probability of each event.
  - i. 3 heads
  - ii. no heads
  - iii. 1 head and 2 tails