

# Exponent Laws

## EXPONENT LAWS CAN ONLY BE USED WHEN LIKE BASES EXIST

1. Complete each table.
2. Examine the relationship between the exponents in the original expression and the exponent in the expression as a single power. State a rule for this relationship.

### DEVELOPING THE MULTIPLICATION LAW

MULTIPLICATION	EXPAND & SIMPLIFY	EXPRESSION AS A SINGLE POWER
$a^4 \times a^5$	$a \times a \times a \times a \times a \times a \times a \times a \times a \times a$	$a^9$
$a^2 \times a^4$		
$a^5 \times a$		
$a^6 \times a^2$		
$a^4 \times a^3$		
Rule:		

### DEVELOPING THE DIVISION LAW

DIVISION	EXPAND & SIMPLIFY	EXPRESSION AS A SINGLE POWER
$a^5 \div a^4$	$\frac{a \times a \times a \times a \times a}{a \times a \times a \times a}$	$a^1$
$a^4 \div a^2$		
$a^5 \div a$		
$a^6 \div a^2$		
$a^4 \div a^3$		
Rule:		

DEVELOPING THE **POWER OF A POWER LAW**

DIVISION	EXPAND & SIMPLIFY	EXPRESSION AS A SINGLE POWER
$(a^4)^5$	$a^4 \times a^4 \times a^4 \times a^4 \times a^4$	$a^{20}$
$(a^5)^2$		
$(a^2)^3$		
$(a^3)^4$		
$(a^6)^2$		
Rule:		

**Example 1**

Use the exponent laws to simplify.

a.  $(x^3)(x^8)$

c.  $(x^2)^4$

e.  $x^4(x^6y^3)$

b.  $x^9 \div x^3$

d.  $(x^3y^2)(xy^5)$

f.  $2x^7y^4 \div x^6y$

When using these laws with *more than one variable* apply the **distributive property**.

**POWER OF A PRODUCT LAW**

$$(x^4 y^3)^2$$

**Example 2**

Use the exponent laws to simplify.

a.  $(x^2 y^7)^3$

b.  $(2x^6 y)^4$

**POWER OF A QUOTIENT LAW**

$$(x^4 \div y^3)^2$$

c.  $\left(\frac{x^4}{y^5}\right)^3$

d.  $\left(\frac{3y^2}{x^6}\right)^3$

**POWER OF A SUM/DIFFERENCE**

$$(x^4 - y^3)^2$$

e.  $(x + 2y^3)^2$

**USING THE DIVISION LAW TO UNDERSTAND ZERO AND NEGATIVE EXPONENTS**

1. Complete the table.
2. Examine the relationship between the exponents in the original expression and the exponent in the expression as a single power. State a rule for zero and negative exponents.
3. Test the rules to see if they hold true.

DIVISION	EXPAND & SIMPLIFY	EXPRESSION AS A SINGLE POWER	USE EXPONENT LAWS
$a^3 \div a$	$\frac{a \times a \times a}{a}$	$a^2$	$a^2$
$a^3 \div a^2$			
$a^3 \div a^3$			
$a^3 \div a^4$			
$a^3 \div a^5$			
$a^3 \div a^6$			
$a^3 \div a^7$			

**ZERO LAW**

Rule:		
Test:		
	EXPAND & SIMPLIFY	USE DIVISION LAW
$x^2 \div x^2$		
$2^3 \div 2^3$		
$5^4 \div 5^4$		

**NEGATIVE EXPONENT LAW**

Rule:		
Test:		
	EXPAND & SIMPLIFY	USE DIVISION LAW
$x^2 \div x^5$		
$2^3 \div 2^4$		
$5^4 \div 5^6$		

**Example 3**

Use the exponent laws to simplify. Write each answer with a positive exponent.

a.  $x^{-8} \times x^8$

b.  $x^{10} \div x^{12}$

c.  $(x^9)^0$

d.  $x^{-4} \times x^{-2}$

e.  $\frac{2x}{x^3}$

f.  $\frac{x^0}{4x^{-3}}$

g.  $(5x^2y^5)^2 \cdot (5^{-2}x^{-6}y)$

h.  $\frac{(9x^2y^5)^2}{3^3x^6y^{14}}$