

7.1 Exponent Rules

Learning Goal: We are learning to work with exponents and their laws.

1. Write each expression as a single power, then evaluate.

The law:

The Product law states when you multiply the same bases, you add exponents.

a) $3^2 \times 3^2$
 $3 \times 3 \times 3 \times 3$

$$= 3^{2+2} = 3^4 = 81$$

c) $(-5)^3 \times (-5)^1$

$$= (-5)^{4} = 625$$

e) $\left(-\frac{1}{4}\right)^2 \times \left(-\frac{1}{4}\right)^3$

$$= \left(-\frac{1}{4}\right)^5$$

b) $2^5 \times 2^2$

d) $(-1)^2 \times (-1)^3 \times (-1)^5$

f) $\left(\frac{2}{5}\right)^2 \times \left(\frac{2}{5}\right)^2 \times \left(\frac{2}{5}\right)$

4 → exponent
3 → base

2. Write each expression as a single power, then evaluate.

The law:

Quotient Law: when dividing same bases, you subtract exponents

a) $5^6 \div 5^3$

$$= 5^{6-3} = 5^3 = 125$$

c) $2^{10} \div 2^8$

$$= 2^2 = 4$$

e) $\frac{(-5)^8}{(-5)^6} \times (-5)^2$

$$= (-5)^2 \times (-5)^2 = (-5)^4 = 625$$

b) $8^4 \div 8^2$

d) $\frac{(-3)^7}{(-3)^4}$

f) $\frac{4^6}{4^4} \times 4^2$

division

① Divided
② Multiplied

3. Write each expression as a single power, then evaluate.

The law: *Power Law. When an exponent is raised to another exponent, multiply them.*

a) $(3^2)^3$

b) $(2^4)^2 = 2^{4+4} = 2^8 = 256$

c) $[(-3)^2]^2$

d) $\left(\frac{1}{3^2}\right)^3 = \frac{1}{3^6}$

e) $[(-1)^5]^6$

f) $\left(\frac{1}{4^2}\right)^2 = \frac{1}{4^4}$

4. Show *one* way of evaluating each expression.

a) $5^2 \times 5^3 = 5^5 = 3125$

b) $\frac{2^5}{2^3} \times \frac{2^8}{2^4} = 2^2 \times 2^4 = 2^6$

c) $\frac{4^4}{4^3} \times 4^2$

d) $\frac{3^5 \times 3^3}{3^2 \times 3^2}$

5. a) Write 7^6 as a product of two powers in *one* way.

$7^3 \times 7^3 = 7^6$

- b) Write 5^3 as a quotient of two powers in *one* way.

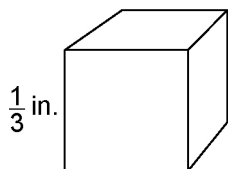
$5^7 \div 5^4 = 5^3$

- c) Write 3^{16} as a power of a power in *one* way.

$(3^2)^8 = 3^{16}$

6. The volume of a cube is given by the formula $V = s^3$, where s represents the side length of the cube. Calculate the volume of each cube.

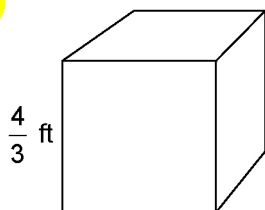
a)



$$V = \left(\frac{1}{3}\right)^3 = \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} = \frac{1}{27}$$

$$= \frac{1^3}{3^3} = \frac{1}{27}$$

b)



7. Simplify each expression. Then, use a calculator to evaluate. Round your answers to two decimal places.

a) $6^{4.2} \times 6^{3.1}$

$$= 6^{7.3} = 979186.01$$

b) $3^{2.9} \times 3^{1.1}$

c) $(2)^{4.6} \times (2)^{3.1}$

$$= 2^{7.7}$$

$$= 207.94$$

d) $(4)^{2.3} \times (4)^{1.5}$

8. The probability of tossing a coin and getting heads is $\frac{1}{2}$. So, the probability of tossing two coins and getting two heads is $\left(\frac{1}{2}\right) \times \left(\frac{1}{2}\right)$ or $\left(\frac{1}{2}\right)^2$.

a) Write the probability of tossing two coins and getting two heads as a fraction.

$$\frac{1}{2} \times \frac{1}{2} = \left(\frac{1}{2}\right)^2 = \frac{1}{4}$$

b) What is the probability of tossing four coins and getting four heads?

$$\frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} = \left(\frac{1}{2}\right)^4 = \frac{1}{16}$$

9. Use exponent rules to simplify each expression.

a) $(4x^3)(2x^4)$

$= 8x^7$

b) $\frac{-12a^5b^3}{3a^2b}$

c) $(m^2n^3)^5$

d) $\left(\frac{k^5h^4}{k^2h^2}\right)^3$

$= (k^3h^2)^3$

$= k^9h^6$

Success Criteria:

- I can simplify exponents by using the Product Law, Quotient Law, and the Power Law.