

# 7.1 Arithmetic Sequences

First some terminology:

## sequence

an ordered list of numbers

$= 4, 1, 4, 9, 10, 11, 12, 100$

## term

a number in a sequence.

Subscripts are usually used to identify the positions of the terms.

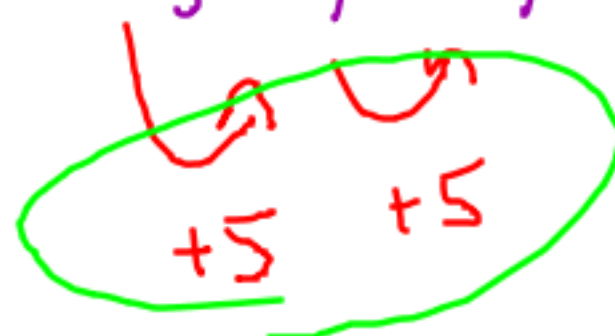
$$t_3 = 3^{\text{rd}} \text{ term} \\ = 4$$

$$t_6 = 11$$

## arithmetic sequence

a sequence that has the same difference, the common difference, between any pair of consecutive terms

$4, 9, 14, 19, 24, \dots$



d

Terminology continued...

### recursive sequence

a sequence for which one term (or more) is given and each successive term is determined from the previous term(s)

1, 1, 2, 3, 5, 8, 13, 21, 34 ...

Fibonacci

### general term

a formula, labelled  $t_n$ , that expresses each term of a sequence as a function of its position. For example, if the general term is  $t_n = 2n$ , then to calculate the 12th term ( $t_{12}$ ), substitute  $n = 12$ .

$$\begin{aligned} t_{12} &= 2(12) \\ &= 24 \end{aligned}$$

$$t_n = a + (n - 1)d$$

$\downarrow$   
 $t_1$

$\uparrow$   
difference

Some examples:

1. Determine if the sequence is arithmetic. If it is, state the general term, then find the 40<sup>th</sup> term.

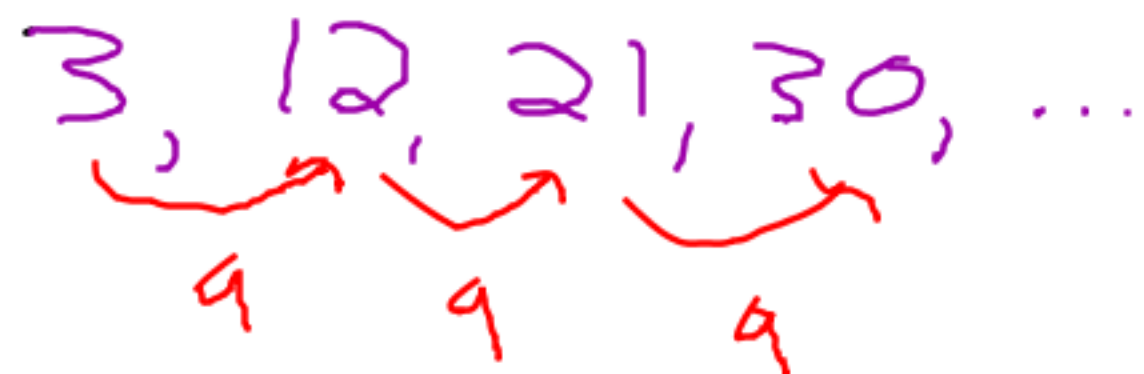
$$3, 12, 21, 30, \dots$$


Diagram illustrating the sequence  $3, 12, 21, 30, \dots$  with red arrows indicating a constant difference of 9 between consecutive terms.

$$d = 9 \quad a = 3$$

$$t_n = a + (n-1)d$$

$$t_n = 3 + (n-1)(9)$$

$$t_n = 3 + 9n - 9$$

$$\rightarrow t_n = 9n - 6$$

$$t_{40} = 9(40) - 6$$

$$t_{40} = 354$$

2. The 7<sup>th</sup> term of an arithmetic sequence is 53 and the 11<sup>th</sup> term is 97. Find the common difference and the first term.



$$t_{11} - t_7 = 97 - 53 = 44$$

$$4d = 44$$

$$d = 11$$

$$\begin{aligned} 53 - 6(11) \\ t_1 = -13 \end{aligned}$$



3. How many terms in the finite arithmetic sequence?

18, 11, 4, -3, ... -129

$a, d, n$

$$\boxed{t_n} = 18 + (n-1)(-7)$$

$$-129 = 18 + (n-1)(-7)$$

$$-147 = (n-1)(-7)$$

$$21 = n-1$$

$$\boxed{22} = n$$