

7.5] Arithmetic Series

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$$27 + 23 + 19 + 15 + 11 + 7 + 3$$

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$$\begin{array}{r} t_1 3 + 7 + 11 + 15 + 19 + 23 + 27 \\ t_n 27 + 23 + 19 + 15 + 11 + 7 + 3 \\ \hline 30 + 30 + 30 + 30 + 30 + 30 + 30 \end{array}$$

$$\frac{7(30)}{2} = \frac{210}{2} = 105$$

The two formulas:

$$S_n = \frac{n(t_1 + t_n)}{2}$$

$$S_n = \frac{n(a + a + (n-1)d)}{2}$$

do not need

d

$$S_n = \frac{n(2a + (n-1)d)}{2}$$

need d

Two examples:

Find S_{22} of the sequence 32, 25, 18...

$$S_n = \frac{n(2a + (n-1)d)}{2}$$

$$S_{22} = \frac{22(2(32) + (22-1)(-7))}{2}$$

$$S_{22} = -913$$

Find the sum of arithmetic sequence:

$$8 + 11 + 14 + \dots + 2129$$

$\xrightarrow{+3}$

$$t_n = a + (n-1)d$$

$$2129 = 8 + (n-1)(3)$$

$$2121 = (n-1)(3)$$

$$707 = n-1$$

$$708 = n$$

$$S_n = \frac{n(t_1 + t_n)}{2}$$

$$S_{708} = \frac{708(8 + 2129)}{2}$$

$$S_{708} = 756498$$