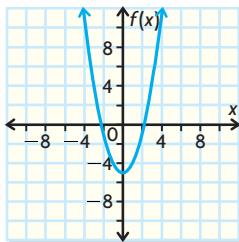


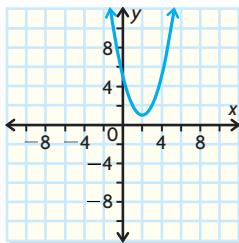
Chapter 4

Getting Started, pp. 192–194

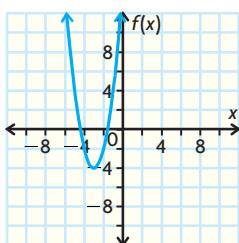
1. a) (iv) c) (v) e) (i)
b) (iii) d) (ii) f) (vi)
2. a) $(x + 10)(x - 3); x = -10 \text{ or } x = 3$
b) $(x + 5)(x + 3); x = -5 \text{ or } x = -3$
c) $(x + 2)(x - 3); x = -2 \text{ or } x = 3$
d) $(x - 2)(x - 3); x = 2 \text{ or } x = 3$
3. a) $(x + 3)^2$ c) $(3x + 1)^2$
b) $(x - 4)^2$ d) $(2x - 3)^2$
4. a) $-15x^2 + 7x + 8$ c) $12x^2 - x - 35$
b) $2x^2 + 6$ d) $4x^2 - 1$
5. a) $(x - 5)(x + 8)$ c) $(9x - 7)(9x + 7)$
b) $(2x + 3)(3x - 2)$ d) $(3x + 1)^2$
6. a) 9 c) $28x$
b) $10x$ d) 16
7. a) $f(x) = (x - 9)(x + 2)$ c) $b(x) = (2x - 5)(2x + 5)$
b) $g(x) = -(x - 8)(2x - 1)$ d) $y = (3x - 1)(2x + 5)$
8. a) vertex: $(-3, -4)$; domain: $\{x \in \mathbb{R}\}$; range: $\{y \in \mathbb{R} \mid y \geq -4\}$
b) vertex: $\left(\frac{5}{4}, -\frac{121}{8}\right)$; domain: $\{x \in \mathbb{R}\}$; range: $\left\{y \in \mathbb{R} \mid y \geq -\frac{121}{8}\right\}$
c) vertex: $\left(-\frac{7}{12}, \frac{121}{24}\right)$; domain: $\{x \in \mathbb{R}\}$; range: $\left\{y \in \mathbb{R} \mid y \leq \frac{121}{24}\right\}$
d) vertex: $\left(\frac{3}{2}, \frac{147}{4}\right)$; domain: $\{x \in \mathbb{R}\}$; range: $\left\{y \in \mathbb{R} \mid y \leq \frac{147}{4}\right\}$
9. a) $f(x) = x^2$ vertically shifted down 5 units



b) $f(x) = x^2$ translated 2 units right and 1 unit up

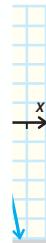


c) $f(x) = x^2$ translated 3 units left, stretched vertically by a factor of 2 and translated 4 units down



d)

its right, compressed vertically by a factor of 2 and translated 2 units up



10. 0.5

11.

Essential characteristics:
A polynomial equation containing one variable with highest degree 2.

Examples:

$$\begin{aligned} x^2 - 9 &= 0 \\ x^2 + 4x - 21 &= 0 \\ (3x - 1)(2x + 5) &= 0 \end{aligned}$$

Non-essential characteristics:
Does not have to = 0.
Can have fractional or decimal coefficients.
Can have variables on both sides of the = sign.

Does not have a solution.

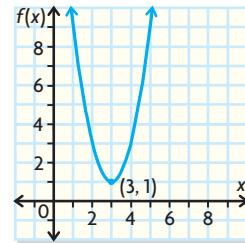
Quadratic Equation

Non-examples:

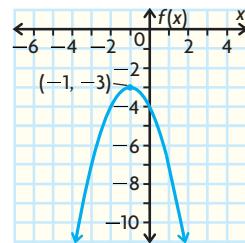
$$\begin{aligned} x^2 + x^2 &= 0 \\ x^2 + \frac{1}{x} &= 0 \end{aligned}$$

Lesson 4.1, pp. 203–205

1. a) $(3, -5)$; min c) $(-1, 6)$; max
b) $(5, -1)$; max d) $(-5, -3)$; min
2. a) $x = 3$, domain: $\{x \geq \mathbb{R}\}$; range: $\{y \geq \mathbb{R} \mid y \geq -5\}$
b) $x = 5$, $\{x \geq \mathbb{R}\}$; range: $\{y \geq \mathbb{R} \mid y < -1\}$
c) $x = -1$, $\{x \geq \mathbb{R}\}$; range: $\{y \geq \mathbb{R} \mid y < 6\}$
d) $x = -5$, $\{x \geq \mathbb{R}\}$; range: $\{y \geq \mathbb{R} \mid y \geq -3\}$
3. a) $f(x) = 2x^2 - 12x + 19$



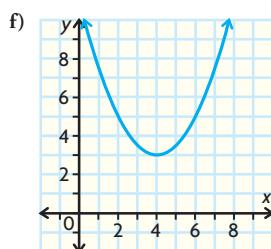
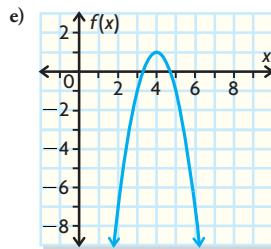
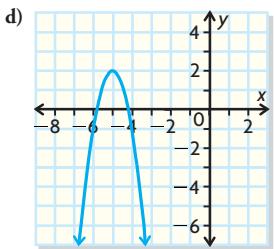
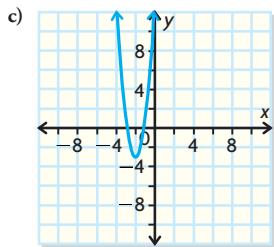
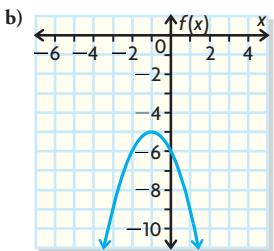
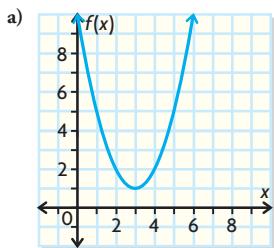
b) $f(x) = -x^2 - 2x - 4$



4.

Function	Vertex	Axis of Symmetry	Opens Up/Down	Range
a) $f(x) = (x - 3)^2 + 1$	(3, 1)	$x = 3$	up	$y \geq 1$
b) $f(x) = -(x + 1)^2 - 5$	(-1, -5)	$x = -1$	down	$y \leq -5$
c) $y = 4(x + 2)^2 - 3$	(-2, -3)	$x = -2$	up	$y \geq -3$
d) $y = -3(x + 5)^2 + 2$	(-5, 2)	$x = -5$	down	$y \leq 2$
e) $f(x) = -2(x - 4)^2 + 1$	(4, 1)	$x = 4$	down	$y \leq 1$
f) $y = \frac{1}{2}(x - 4)^2 + 3$	(4, 3)	$x = 4$	up	$y \geq 3$

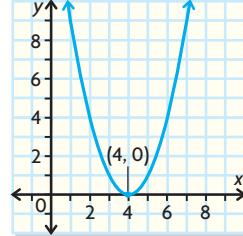
Sketches (from table above)

5. a) $x = -8, 14$ b) $x = -12, 2$ c) $x = 1$ d) $x = -6.873$ or -0.873 e) $x = 0.192$ or 7.808

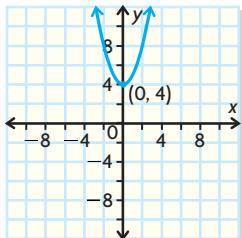
f) no zeros

6. $f(x) = (x - 7)^2 - 25$; vertex form: vertex $(7, -25)$; axis: $x = 7$; direction of opening: up $f(x) = x^2 - 14x + 24$; standard form: y intercept is 24; direction of opening: up $f(x) = (x - 12)(x - 2)$; factored form: zeros: $x = 12$ and $x = 2$; direction of opening: up7. a) after 0.3 s; maximum since $a < 0$ so the parabola opens down
b) 110 m
c) 109.55 m8. a) $y = -3(x + 4)^2 + 8$, $y = -3x^2 - 24x - 40$ b) $y = -(x - 3)^2 + 5$, $y = -x^2 + 6x - 4$ c) $f(x) = 4(x - 1)^2 - 7$, $y = 4x^2 - 8x - 3$ d) $y = (x + 6)^2 - 5$, $y = x^2 + 12x + 31$ 9. a) $f(x) = (x + 3)^2 - 4$ b) $f(x) = (x - 2)^2 + 1$ c) $f(x) = -(x - 4)^2 - 2$ d) $f(x) = -(x + 1)^2 + 4$

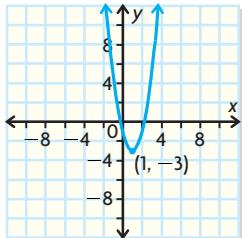
10. a) 23 m b) 2 s c) 1 s or 3 s

11. a) vertex: $(4, 0)$; two possible points $(3, 1), (5, 1)$ 

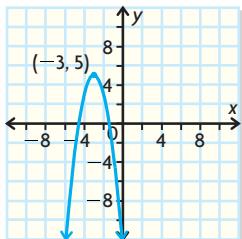
- b) vertex: $(0, 4)$; two possible points: $(2, 8), (-2, 8)$



- c) vertex: $(1, -3)$; two possible points: $(-1, 5), (3, 5)$



- d) vertex: $(-3, 5)$; two possible points: $(-2, 3), (-4, 3)$



12. $y = 2(x + 1)^2 - 8$

13. Expand and simplify. For example,

$$\begin{aligned}f(x) &= (x + 2)^2 - 4 \\&= x^2 + 4x + 4 - 4 \\&= x^2 + 4x\end{aligned}$$

14. a) y -intercept, opens upward or downward

b) vertex, opens upward or downward, max/min

15. $y = -0.88(x - 1996)^2 + 8.6$

16. $f(x) = (x - 1)^2 - 36$

Lesson 4.2, pp. 213–215

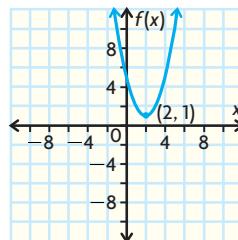
1. a) 16 b) 36 c) 25 d) $\frac{25}{4}$
2. a) $m = 10, n = 25$ c) $m = 12, n = 36$
b) $m = 6, n = 9$ d) $m = \frac{7}{2}, n = \frac{49}{4}$
3. a) $(x + 7)^2$ c) $(x - 10)^2$
b) $(x - 9)^2$ d) $(x + 3)^2$
4. a) $(x + 6)^2 + 4$ c) $(x - 5)^2 + 4$
b) $(x - 3)^2 - 7$ d) $\left(x - \frac{1}{2}\right)^2 - \frac{13}{4}$
5. a) $a = 3, b = 2, k = 5$
b) $a = -2, b = -5, k = -3$
c) $a = 2, b = 3, k = 5$
d) $a = \frac{1}{2}, b = -3, k = -5$

6. a) $f(x) = (x + 4)^2 - 13$

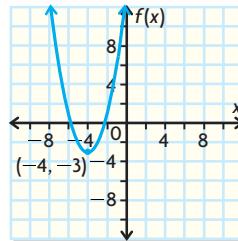
b) $f(x) = (x - 6)^2 - 1$

c) $f(x) = 2(x + 3)^2 - 11$

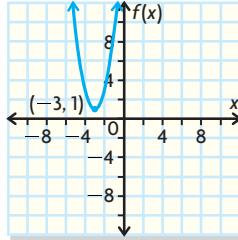
7. a) $f(x) = (x - 2)^2 + 1$; domain: $\{x \in \mathbb{R}\}$; range: $\{y \in \mathbb{R} \mid y \geq 1\}$



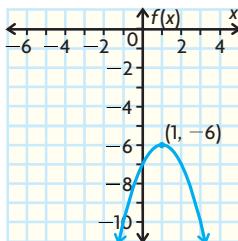
- b) $f(x) = (x + 4)^2 - 3$; domain: $\{x \in \mathbb{R}\}$; range: $\{y \in \mathbb{R} \mid y \geq -3\}$



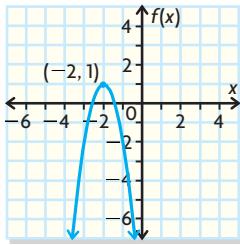
- c) $f(x) = 2(x + 3)^2 + 1$; domain: $\{x \in \mathbb{R}\}$; range: $\{y \in \mathbb{R} \mid y \geq 1\}$



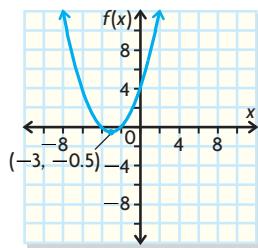
- d) $f(x) = -(x - 1)^2 - 6$; domain: $\{x \in \mathbb{R}\}$; range: $\{y \in \mathbb{R} \mid y \leq -6\}$



e) $f(x) = -3(x + 2)^2 + 1$; domain: $\{x \in \mathbb{R}\}$; range: $\{y \in \mathbb{R} \mid y \leq 1\}$



f) $f(x) = \frac{1}{2}(x + 3)^2 - \frac{1}{2}$; domain: $\{x \in \mathbb{R}\}$; range: $\{y \in \mathbb{R} \mid y \geq -0.5\}$



8. a) $g(x) = 4(x - 3)^2 - 5$

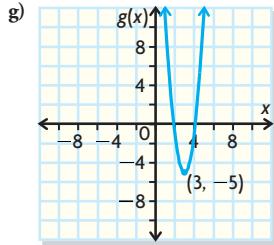
b) $x = 3$

c) $(3, -5)$

d) minimum value of -5 because $a > 0$; parabola opens up

e) domain: $\{x \in \mathbb{R}\}$

f) $\{g(x) \in \mathbb{R} \mid g(x) \geq -5\}$



9. Colin should have taken the square root of both 9 and 4 to get $\frac{3}{2}$, not $\frac{3}{4}$.

10. $61\ 250\ \text{m}^2$

11. $\$15$

12. a) $y = 3(x - 5)^2 - 2$

b) vertex, axis of symmetry, max/min

13. Reflection about the x -axis, a vertical stretch of 2, a horizontal shift of 4, a vertical shift of 3. I completed the square to determine the vertex.

14. Each form provides different information directly.

15.
$$\begin{aligned}f(x) &= ax^2 + bx + c \\&= x^2 + bx + c \\&= x^2 + bx + \left(\frac{b}{2}\right)^2 - \left(\frac{b}{2}\right)^2 + c \\&= \left(x + \frac{b}{2}\right)^2 + \left(c - \frac{b^2}{4}\right)\end{aligned}$$

Example:

$$\begin{aligned}f(x) &= x^2 + 6x + 4 \\&= x^2 + 6x + \left(\frac{6}{2}\right)^2 - \left(\frac{6}{2}\right)^2 + 4 \\&= x^2 + 6x + 9 - (9 + 4) \\&= (x + 3)^2 - 5\end{aligned}$$

16. $y = -5(x - 1)^2 + 6$

17. $(1, 6)$

Lesson 4.3, pp. 222–223

1. a) $a = 3, b = -5, c = 2$ c) $a = 16, b = 24, c = 9$

b) $a = 5, b = -3, c = 7$ d) $a = 2, b = -10, c = 7$

2. a) $x = \frac{-(-5) \pm \sqrt{(-5)^2 - 4(3)(2)}}{2(3)}$

b) $x = \frac{-(-3) \pm \sqrt{(-3)^2 - 4(5)(7)}}{2(5)}$

c) $x = \frac{-(24) \pm \sqrt{(24)^2 - 4(16)(9)}}{2(16)}$

d) $x = \frac{-(-10) \pm \sqrt{(-10)^2 - 4(2)(7)}}{2(2)}$

b) a) $x = 1$ or $x = \frac{2}{3}$ c) $x = -\frac{3}{4}$

b) no solution d) $x = 4.16$ or $x = 0.84$

3. a) no solution

b) $x = -5$ or $x = 1.5$

c) $x = 5.5$

d) $x = -0.84$ or $x = 2.09$

e) no solution

f) $x = -0.28$ or $x = 0.90$

4. a) no solution

b) $x = -5$ or $x = 1.5$

c) $x = 5.5$

d) $x = -0.84$ or $x = 2.09$

e) no solution

f) $x = -0.28$ or $x = 0.90$

5. For example:

a) factoring, $x = 0$ or $x = 15$

b) take the square root of both sides, $x = -10.72$ or $x = 10.72$

c) factoring, $x = 8$ or $x = \frac{3}{2}$

d) expand, then use quadratic formula, $x = 2.31$ or $x = 11.69$

e) isolate the squared term, $x = -2$ or $x = 8$

f) quadratic formula, $x = 0.09$ or $x = 17.71$

6. a) 10.9 s b) approx. 9 s

7. 20 m \times 20 m and 10 m \times 40 m

8. 9.02 s

9. 91 km/h

10. Answers may vary. E.g., 2 solutions $2x^2 - 4x = 0$, $3x^2 - 4x - 2 = 0$; 1 solution $3x^2 - 6x + 3 = 0$, $x^2 - 2x + 1 = 0$; 0 solutions $x^2 - 6x + 10 = 0$

11. a) $x = 1.62$ or $x = 6.38$

b) $x = 1.62$ or $x = 6.38$

c) The method in part (a) was best because it required fewer steps to find the roots.

12. $(-1, -2)$ and $(3, 6)$

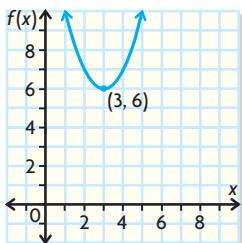
13. $(-1.21, -5.96)$ and $(2.21, 4.29)$

14. a) $x = 0$ and $x = 0.37$

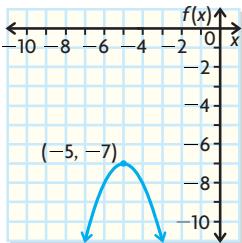
b) $x = -3$ and $x = -2.4$, and $x = 2.4$ and $x = 3$

Mid-Chapter Review, p. 226

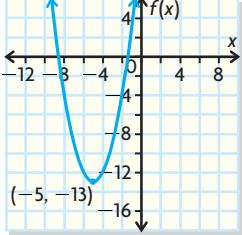
1. a) $f(x) = x^2 - 16x + 68$
 b) $g(x) = -x^2 + 6x - 17$
 c) $f(x) = 4x^2 - 40x + 109$
 d) $g(x) = -0.5x^2 + 4x - 6$
2. a) vertex: $(3, 6)$; axis: $x = 3$; min. 6; domain: $\{x \in \mathbb{R}\}$; range: $\{y \in \mathbb{R} | y \geq 6\}$



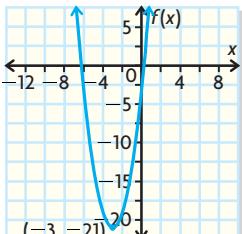
- b) vertex: $(-5, -7)$; axis: $x = -5$; max. -7 ; domain: $\{x \in \mathbb{R}\}$; range: $\{y \in \mathbb{R} | y \leq -7\}$



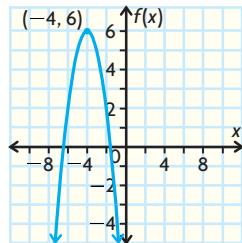
3. Answers may vary. E.g., the vertex form. From this form, I know the location of the vertex, which helps me sketch the graph. If $f(x) = (x + 2)^2 - 5$, then the vertex is $(-2, -5)$ and the parabola opens up.
4. a) $f(x) = 2(x - 2)^2 + 5$
 b) $f(x) = -3(x + 1)^2 - 4$
5. a) $f(x) = (x + 5)^2 - 13$



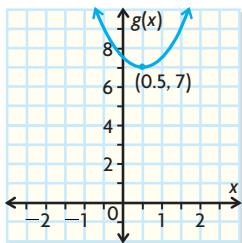
- b) $f(x) = 2(x + 3)^2 - 21$



c) $f(x) = -(x + 4)^2 + 6$



d) $g(x) = 2(x - 0.5)^2 + 7$



6. \$205
 7. 10 000 m²
 8. a) $x = -5, x = 3$ c) $x = 5.27, x = 8.73$
 b) $x = \frac{1}{3}$ d) no solution
 9. about 4 s
 10. \$1.67 and \$10
 11. a) 62 m b) about 8 s c) at 3 s and 5 s

Lesson 4.4, pp. 232–233

1. a) $(-5)^2 - 4(1)(7)$ c) $(12)^2 - 4(3)(-7)$
 b) $(11)^2 - 4(-5)(17)$ d) $(1)^2 - 4(2)(-11)$
 2. a) two distinct c) one e) two distinct
 b) none d) none f) one
 3. No, there are two solutions; $b^2 - 4ac = (-5)^2 - 4(1)(2) > 0$
 4. a) two c) one e) none
 b) none d) two f) one
 5. $k > 4$ or $k < -4$
 6. $m = 4$
 7. $k < \frac{1}{2}$, $k = \frac{1}{2}$, $k > \frac{1}{2}$
 8. a) Put a , b , and c into the discriminant and set the discriminant equal to zero. Solve for k .
 b) $(-5)^2 - 4(3)(k) = 0, k = \frac{25}{12}$
 9. $k = -4, k = 8$
 10. a) $-50 < k < 50$
 b) $k = \pm 50$
 c) $k < -50, k > 50$
 11. Answers may vary. E.g., if $a = 2$, $b = 3$, and $c = -1$, then $0 = 2x^2 + 3x - 1$. In this case, the discriminant ($b^2 - 4ac$) has a value of 17, so there are 2 solutions.
 12. Yes. The discriminant will be greater than zero. $x = 99.9$
 13. Answers may vary. E.g., discriminant, quadratic formula
 14. Yes. Set the expression equal to each other and solve. You would get $p = 1$ or $p = -13$.
 15. two distinct zeros for all values of k

Lesson 4.5, pp. 239–241

- Complete the square to put the function in vertex form.
The y -coordinate of the vertex will be the maximum revenue.
- \$3025
- Solve the equation $-4.9t^2 + 1.5t + 17 = 5$ for $t > 0$.
- 1.73 s
- \$1865; \$6
- a) 8600
b) approx. 2011
c) no; the graph does not cross the horizontal axis
- when selling between 1000 and 7000 pairs of shoes
- 128 m^2
- a) 8.4 m
b) 20 km/h
- 2 m
- 2017
- a) \$6.50 b) \$8.00
- a) about 1.39 m c) no, the ball hits the ground at 4.3 s
b) 23 m d) $t = 0.47$ s and $t = 3.73$ s
- a) $f(x) = -60(x - 5.5)^2 + 1500$
b) \$2 or \$9
- An advantage of the vertex form is that it provides the minimum or maximum values of the function. A disadvantage is that you must expand and simplify to find the zeros of the function using the quadratic formula.
- $5 \text{ cm} \times 12 \text{ cm}$
- 10 cm

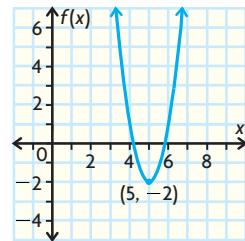
Lesson 4.6, pp. 250–252

- a) no, the graph increases too quickly
b) yes, the graph decreases and increases
- a)
b) (1989, 23.5)
c) up, e.g., $a = 1$
d) e.g., needs to be wider so use a smaller, positive value for a
e) $y = 0.23(x - 1989)^2 + 23.5$, or
 $y = 0.23x^2 - 912.53x + 908\ 060.52$
f) domain: $\{x \in \mathbb{R} \mid 1981 \leq x \leq 1996\}$
range: $\{y \in \mathbb{R} \mid 23.5 \leq y \leq 41.7\}$
- a) $y = (x - 5)^2 - 3$
b) $y = -0.5(x + 4)^2 + 6$
- a) $y = 2x^2 - 8x + 11$
b) $y = -2x^2 - 4x + 3$
c) $y = -4x^2 + 24x - 43$
d) $y = 6x^2 + 24x + 19$
- a)
Length of skid (m)
Speed (km/h)

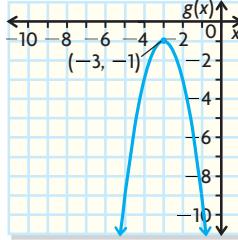
- b) $y = 0.007x^2 - 0.0005x - 0.016$
c) Skid will be 100.7 m.
d) domain: $\{x \in \mathbb{R} \mid x \geq 0\}$; range: $\{y \in \mathbb{R} \mid y \geq 0\}$
- a) $y = 0.000\ 83x^2 - 0.116x + 21.1$
b) 21.1¢
c) domain: $\{x \in \mathbb{R} \mid x \geq 0\}$; range: $\{y \in \mathbb{R} \mid y \geq 17\}$
- a) $y = -15(x - 1987)^2 + 1075$
b) not very well, because they would be selling negative cars
c) domain: $\{x \in \mathbb{R} \mid x \geq 1982\}$; range: $\{y \in \mathbb{R} \mid y \leq 1075\}$
- $y = -5(x - 2)^2 + 20.5$; $x \geq 0$, $y \geq 0$; 4 s
- a) $y = -0.53x^2 + 1.39x + 0.13$
b) domain: $\{x \in \mathbb{R} \mid x \geq 0\}$; range: $\{y \in \mathbb{R} \mid y \leq 1.1\}$
c) 0.57 kg/ha or 2.05 kg/ha
- a) $y = 0.03(x - 90)^2 + 16$
b) 1096 mph, no a regular car can't drive that fast!
- $f(x) = 2x^2 + 4x + 6$
- If the zeros of the function can be determined, use the factored form $f(x) = a(x - r)(x - s)$. If not, then use graphing technology and quadratic regression.
- 12.73 m
- 15, 24
- \$6250, \$12.50

Chapter Review, pp. 254–255

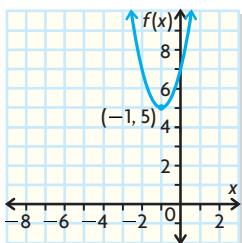
- a) $f(x) = x^2 + 6x + 2$
b) $f(x) = -x^2 - 14x - 46$
c) $f(x) = 2x^2 - 4x + 7$
d) $f(x) = -3x^2 + 12x - 16$
e) $f(x) = (x - 3)^2 - 5$
f) $f(x) = \frac{1}{2}(x + 2)^2 - 3$
- a) $f(x) = -(x - 6)^2 + 4$
b) $f(x) = 2(x - 5)^2 + 3$
- a) $f(x) = (x + 1)^2 - 16$
b) $f(x) = -(x - 4)^2 + 9$
c) $f(x) = 2(x + 5)^2 - 34$
d) $f(x) = 3(x + 2)^2 + 7$
e) $f(x) = \frac{1}{2}(x - 6)^2 + 8$
f) $f(x) = 2\left(x + \frac{1}{2}\right)^2 + \frac{7}{2}$
- a) vertex: $(5, -2)$; axis: $x = 5$; opens up because $a > 0$; two zeros because the vertex is below the x -axis; parabola opens up



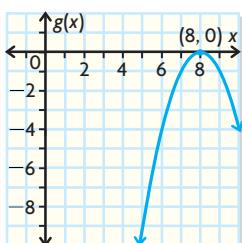
- b) vertex: $(-3, -1)$; axis: $x = -3$; opens down because $a < 0$; no zeros because the vertex is below the x -axis; parabola opens down



- c) vertex: $(-1, 5)$; axis: $x = -1$; will have no zeros because the vertex is above the x -axis; parabola opens up



- d) vertex: $(8, 0)$; axis: $x = 8$; $a < 0$, will have one zero because the vertex is on the x -axis; parabola opens down



5. a) $x = -\frac{1}{2}, x = 8$

b) no solution

c) $x = \frac{1}{3}$

d) $x = 1.16, x = -2.40$

6. a) 2.7 m b) 1.5 s

7. a) no solution
b) two distinct solutions
c) one solution

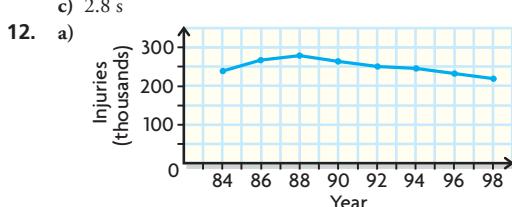
8. a) $\frac{16}{5} > k$ b) $\frac{16}{5} = k$ c) $\frac{16}{5} < k$

9. a) 25 cars b) \$525

10. a) $41\ 472 \text{ m}^2$ b) $10\ 720 \text{ m}^2$ c) 36 m

11. a) $y = -4.9(x - 1.5)^2 + 10.5$
b) domain: $\{x \in \mathbb{R} \mid 0 \leq x \leq 2.96\}$;
range: $\{y \in \mathbb{R} \mid 0 \leq y \leq 10.5\}$

c) 2.8 s



b) $y = -673.86x^2 + 2\ 680\ 816x - 2\ 665\ 999\ 342$

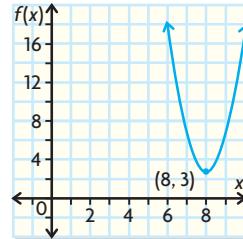
c) Use the quadratic regression function on a graphing calculator to determine the curve's equation. $y = -673.86x^2 + 2\ 680\ 816x - 2\ 665\ 999\ 342$

d) 160 715, using the above equation

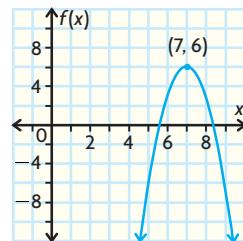
e) 1989

Chapter Self-Test, p. 256

- a) $f(x) = x^2 + 6x + 2$
b) $f(x) = -3x^2 - 30x - 73$
- a) $f(x) = (x - 5)^2 + 8$
b) $f(x) = -5(x - 2)^2 + 8$
- a) vertex: $(8, 3)$; axis: $x = 8$; min. 3



- b) vertex: $(7, 6)$; axis: $x = 7$; max. 6



- If you get a negative under the square root, you cannot solve. There are no solutions to these equations.
- a) $x = -1.12, x = 7.12$
b) no solution
- a) no solution b) one solution
- a) 20.1m b) 15.2 m
- a) \$13 812 b) \$24
- a) $y = -1182(x - 2)^2 + 4180$
b) It fits the data pretty well.
c) domain: $\{x \in \mathbb{R} \mid x \geq 0\}$; range: $\{y \in \mathbb{R} \mid y \leq 4180\}$
d) \$4106
- It is easier to use this method to find the max/min and vertex.

Chapter 5

Getting Started, pp. 260–262

- a) (v) c) (ii) e) (iv)
b) (vi) d) (i) f) (iii)
- a) $\sin A = \frac{12}{13}$, $\cos A = \frac{5}{13}$, $\tan A = \frac{12}{5}$
b) $\sin A = \frac{8}{17}$, $\cos A = \frac{15}{17}$, $\tan A = \frac{8}{15}$
- a) $\angle A \doteq 27^\circ$ b) $b \doteq 3$ c) $\angle A \doteq 50^\circ$ d) $d \doteq 16$
- a) 12 cm b) 10 m
- a) $\sin A = \frac{4}{13}$, $\cos A = \frac{12}{13}$, $\tan A = \frac{1}{3}$; $\angle A \doteq 18^\circ$
b) $\sin D = \frac{5}{7}$, $\cos D = \frac{5}{7}$, $\tan D = 1$; $\angle D \doteq 44^\circ$
c) $\sin C = \frac{12}{13}$, $\cos C = \frac{4}{13}$, $\tan C = 3$; $\angle C \doteq 72^\circ$