

Math 9 – Unit 1: Real Numbers

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Lesson #2: Multiplying and Dividing Fractions

Learning Goal: We are learning to multiply and divide fractions.

Much of Mathematics is learning the rules. These next few lessons have rules. Follow them and you will succeed.

Multiplying Fractions:

The process to multiplying fractions is straight-forward:

1. Multiply the numerators together
2. Multiply the denominators together
3. Reduce to lowest terms.

Examples:

$$\begin{array}{l} \text{a) } \frac{2}{3} \times \frac{4}{5} \\ \quad \quad \quad \rightarrow \quad \rightarrow \\ = \frac{8}{15} \end{array}$$

$$\begin{array}{l} \text{b) } \frac{-8}{5} \times \frac{15}{4} \\ \quad \quad \quad \rightarrow \quad \rightarrow \\ = \frac{-120}{20} \div 20 \\ = -6 \end{array}$$

$$\begin{array}{l} \text{c) } \frac{-4}{3} \times \frac{2}{7} \times \frac{-5}{3} \\ \quad \quad \quad \rightarrow \quad \rightarrow \quad \rightarrow \\ = \frac{40}{63} \end{array}$$

Typically, the hardest part is reducing. There is another way to approach multiplying fractions. First reduce ANY numerator with ANY denominator (this is sometimes called **cross-reducing**). Let's look at example two again, but this time reduce first.

$$\begin{array}{l} \frac{-8}{5} \times \frac{15}{4} \\ \quad \quad \quad \rightarrow \quad \rightarrow \\ = \frac{-6}{1} \\ = -6 \end{array}$$

Another!

$$\begin{array}{l} \frac{6}{7} \times \frac{21}{12} \\ \quad \quad \quad \rightarrow \quad \rightarrow \\ = \frac{3}{2} \end{array}$$

An big one!

$$\begin{array}{l} \frac{17}{5} \times \frac{8}{3} \times \frac{9}{14} \times \frac{25}{4} \\ \quad \quad \quad \rightarrow \quad \rightarrow \quad \rightarrow \quad \rightarrow \\ = \frac{15}{1} = 15 \end{array}$$

***NOTE:** You may reduce first or last, it does not matter, but you must always reduce*

Dividing Fractions:

The process to dividing has one extra step done BEFORE the multiplying steps. We need to change the division to a multiplication, so instead of dividing by a fraction, we multiply by the reciprocal. This means to flip the fraction to the right of the division sign. Once this is done, you now have a multiplication question and can follow the steps from above.

Examples:

$$\begin{array}{l} 10 - 2 = 8 \\ 10 + (-2) = 8 \end{array}$$

flippin' multiply

a) $\frac{4}{5} \div \frac{3}{7}$

b) $\frac{9}{4} \div \frac{8}{3}$ (note: you may be tempted to reduce, but not yet!)

$$= \frac{4}{5} \times \frac{7}{3}$$

$$= \frac{28}{15}$$

$$= \frac{9}{4} \times \frac{3}{8}$$

$$= \frac{27}{32}$$

c) $\frac{6}{11} \div \frac{-3}{2}$

d) $\frac{5}{9} \div \frac{6}{7} \div \frac{12}{14}$

$$= \frac{6}{11} \times \frac{-2}{3}$$

$$= \frac{-4}{11} \quad \left| \quad \frac{-12}{33} \div 3 \right.$$

$$= \frac{5}{9} \times \frac{7}{6} \times \frac{14}{12}$$

$$= \frac{245}{324}$$

Application: A chemist is measuring the acid needed for an experiment. If she has $2\frac{1}{5}$ cylinders (or $\frac{11}{5}$) and she needs $\frac{1}{10}$ of a cylinder for each experiment, how many experiments can she do?

$$\frac{11}{5} \div \frac{1}{10}$$

$$= \frac{11}{5} \times \frac{10}{1} = \frac{22}{1} = 22$$

\therefore She can do
22 exper. mnts

Success Criteria:

- I can multiply fractions by reducing before OR after multiplying
- I can divide fractions by multiplying by the reciprocal of the divisor