

Lesson #8.1: Factoring Expressions with Common Factors

Learning Goal: We are learning to Factor expressions that contain common factors.

Let's look at some needed skills this unit (there are others).

$$1) 3x + 4x \quad |b) 3x^2 + 4x| 2) (3x)(4x)$$

$$= 7x \quad = \quad = 12x^2$$

$$3) 5(2x - 7)$$

$$= 2x(5) - 7(5)$$

$$= 10x - 35$$

Expand Factor

4) What is the ^{greatest} common factor of 18 and 96?

$$1, 2, 3, 6, 9, 18$$

$$18 \div 6 = 3$$

$$96 \div 6 = 16$$

5) What is the common factor of 16, 36 and 64?

$$1, 2, 4, 8, 16$$

$$16 \div 4 = 4 \checkmark$$

$$36 \div 4 = 9 \checkmark$$

$$64 \div 4 = 16 \checkmark$$

Notes on Common Factoring: Factoring is the opposite of expanding. Hence, when expanding, that work eliminates brackets. Factoring brings brackets back into the equation. Also, expanding uses multiplication, therefore factoring uses division.

Factor the common factor out of each expression.

$$5) \frac{8n^2}{2} - \frac{6}{2} \quad GCF = 2$$

↳ divide every term by 2.

$$= 2(4n^2 - 3)$$

$$6) 20m^5 + 15 \quad GCF = 5$$

$$= 5(4m^5) + 5(3)$$

Factor out the 5.

$$= 5(4m^5 + 3)$$

7) $\overbrace{2p^5}^{PPPP} + \overbrace{5p^4}^{PPPP}$ $GCF = 1p^4$
 \rightarrow take them away
 \rightarrow subtract the exponents
 $= p^4(2p^1 + 5)$

8) $\overbrace{6x^6}^{XXXXXX} + \overbrace{15x^4}^{XXXX}$ $GCF = 3x^4$
 \rightarrow always the smaller exponent.
 \rightarrow Divide
 $= 3x^4(2x^2 + 5)$

If the first number is negative, make the GCF negative
 9) $\overbrace{-8v^5}^{--} - \overbrace{30v^2}^{--} + \overbrace{2v^1}^{--}$ $GCF = -2v$
 $\div -2$
 \rightarrow take away a v
 $= -2v(4v^4 + 15v - 1)$

Math people like the front in a bracket to be positive.

10) $\overbrace{8x^4y^2}^{--} - \overbrace{18x^3y}^{--} + \overbrace{18x^2}^{--}$ $GCF = 2x^2$
 $= 2x^2(4x^2y^2 - 9xy + 9)$

$5x \square + 8 \square$
 $= \square(5x + 8)$
 11) $\overbrace{5x(x-3)}^{(x-3)} + \overbrace{8(x-3)}^{(x-3)}$ $GCF: (x-3)$
 $= (x-3)(5x + 8)$

12) $\overbrace{3xy(y+2)}^{(y+2)} - \overbrace{17w^2(y+2)}^{(y+2)}$ $GCF: (y+2)$
 $= (y+2)(3xy - 17w^2)$

Success Criteria:

- I can identify common factors
- I can factor expressions by dividing each term by the common factor
- I can write a factored expression as a monomial \times a polynomial