

Math 9 – Unit 4: Word Problems

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Date: October 16, 2019

Lesson #3: Solving Word Problems Involving Cost

Learning Goal: We are learning to solve word problems involving cost.

To solve a word problem involving cost, we will use a chart instead of a "LET" statement.

a) Matthew has \$0.85 in nickels and dimes. He has 2 more nickels than dimes. How many of each coin does he have?

Coin	Value	Amount	Total Value Worth
nickel	\$0.05	$x+2$	$0.05(x+2)$
dime	\$0.1	x	$0.1x$

Value (Amount)

Equation:

$$0.05(x+2) + 0.1x = 0.85$$

$$0.05x + 0.1 + 0.1x = 0.85$$

$$0.15x + 0.1 = 0.85$$

$$\frac{0.15x}{0.15} = \frac{0.75}{0.15}$$

$$x = 5$$

∴ Matthew has 5 dimes and 7 nickels.

b) A jar contains \$18.50 in dimes and quarters. If there are 110 coins in the jar, determine the number of dimes and the number of quarters.

Coin	Value	Amount	Total
Dimes	\$0.1	x	$0.1x$
Quarters	\$0.25	$110 - x$ left over.	$0.25(110 - x)$

10 dimes, 100¢
40 dimes, 70¢
x d, 110 - x

$$\text{Equation: } 0.1x + 0.25(110 - x) = 18.50$$

$$0.1x + 27.5 - 0.25x = 18.50$$

$$-0.15x + 27.5 = 18.50$$

$$\frac{-0.15x}{-0.15} = \frac{-9}{-0.15} \Rightarrow x = 60$$

∴ there are 60 dimes and 50 quarters in the jar.

c) Tickets to a concert cost \$9.00 for adults and \$6.50 for students. A total of 950 people paid \$7675.00 to attend. How many students attended the concert?

Tickets	Value	Amount	\$ total
Adult	\$9	$950 - x$	$9(950 - x)$
Student	\$6.50	x	$6.5x$

∴ 350 students came to the concert
600 adults came as well.

Equation:

$$9(950 - x) + 6.5x = 7675$$

$$8550 - 9x + 6.5x = 7675$$

$$8550 - 2.5x = 7675$$

$$\begin{array}{r} -2.5x = -875 \\ \underline{-2.5} \quad \underline{-2.5} \end{array}$$

$$x = 350$$

d) Timothy needed to do some Christmas shopping, so he took a hammer to his piggy bank and smashed it open. Timothy noticed that he has 4 times the amount of dimes than nickels, 8 more quarters than nickels, half the number of toonies than nickels, and twice the number of loonies as quarters. Timothy counted a total of \$55. How many of each coin does he have? (After doing this, Timothy added "Piggy Bank" to his Christmas list).

Coin	Value	Amount	\$ Total
dimes	\$0.1	$4x$	$0.1(4x)$
nickels	\$0.05	x	$0.05x$
quarters	\$0.25	$x + 8$	$0.25(x + 8)$
loonies	\$1.00	$2(x + 8)$	$2(x + 8)$
toonies	\$2.00	$\frac{x}{2} = 0.5x$	$2(\frac{x}{2}) = x$

Equation

$$0.1(4x) + 0.05x + 0.25(x + 8) + 2(x + 8) + x = 55$$

$$0.4x + 0.05x + 0.25x + 2 + 2x + 16 + x = 55$$

$$3.7x + 18 = 55$$

Success Criteria:

- I can write the value of common coins as a decimal (Quarter = 0.25, etc...)
- I can set up a chart to represent the given information and unknowns

$$3.7x = 37 \quad \xrightarrow{\quad} \quad \begin{array}{r} 3.7x = 37 \\ \underline{3.7} \quad \underline{3.7} \end{array}$$

$$x = 10$$