

## Math 9 – Unit 1: Real Numbers

### Lesson #4: Order of Operations



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First day of snow!

**Learning Goal:** We are learning to work with the Order of Operations

Evaluate the following expression on your own, without anybody's help:

$$\begin{aligned} & 2(4-6)^2 - 9 \div (5-2) + 1 \\ &= 2(-2)^2 - 9 \div (3) + 1 \\ &= 2(4) - 9 \div (3) + 1 \\ &= 8 - 3 + 1 = 6 \end{aligned}$$

6  
4

Without order, there is chaos. Math cannot have chaos, so logically there must be an order. The order of operations (sometimes known as **BEDMAS**) gives the structure or algorithm to solve mathematical questions.

The order is:

Brackets  
Exponents  
Divide ~~and~~ Multiply  
Add and Subtract.

$$3(4)^2 \neq 12^2 = 144$$

The same order **MUST** be applied when we work with fractions. Let's do some examples:

a)  $2 + \frac{4}{5} \times \frac{1}{4}$

$$\begin{aligned} &= \frac{2 \times 5}{1 \times 5} + \frac{1}{5} \quad (\text{CD } 13 \ 5) \\ &= \frac{10}{5} + \frac{1}{5} \\ &= \frac{11}{5} \end{aligned}$$

b)  $\frac{3}{2} - \frac{7}{5} \div \frac{1}{3} + \frac{3}{2}$

$$\begin{aligned} &= \frac{3}{2} - \frac{7}{5} \times \frac{3}{1} + \frac{3}{2} \quad (\text{CD} = 10) \\ &= \frac{3 \times 5}{2 \times 5} - \frac{21 \times 2}{5 \times 2} + \frac{3 \times 5}{2 \times 5} \\ &= \frac{15 - 42 + 15}{10} = \frac{-12}{10} = -\frac{6}{5} \end{aligned}$$

$$\begin{aligned} \text{c) } & \frac{5}{6} + \left( \frac{9}{5} \div \frac{6}{5} \right)^2 - \frac{1}{2} \\ & = \frac{5}{6} + \left( \frac{9}{5} \times \frac{5}{6} \right)^2 - \frac{1}{2} \\ & = \frac{5}{6} + \left( \frac{3}{2} \right)^2 - \frac{1}{2} \end{aligned}$$

$$= \frac{5}{6 \times 2} + \frac{9 \times 3}{4 \times 3} - \frac{1 \times 6}{2 \times 6} = \frac{10}{12} + \frac{27}{12} - \frac{6}{12} = \frac{31}{12}$$

$$\text{d) } \frac{2}{5} \times \frac{3}{5} + \left( \frac{4}{3} + \frac{2}{7} \right) \times \frac{1}{2}$$

$$= \frac{6}{25} + \left( \frac{4}{3} + \frac{6}{3} \right) \times \frac{1}{2}$$

$$= \frac{6}{25} + \frac{10}{3} \times \frac{1}{2}$$

$$= \frac{6 \times 3}{25 \times 3} + \frac{5 \times 25}{3 \times 25} \quad \text{c.d. is 75}$$

$$= \frac{18}{75} + \frac{125}{75} = \frac{143}{75}$$

In Math, you are usually given an algebraic expression which you need to use to solve given certain values. When you substitute numbers into letters, always do so with parenthesis ().

Example: Solve the following two expressions given  $x = 4$  and  $y = -2$ .

$$\text{a) } 6y - x^2 - y$$

$$= 6(-2) - (4)^2 - (-2)$$

$$= -12 - 16 + 2$$

$$= -26$$

$$\text{b) } (x - y)(x + y)$$

$$= (4 - (-2))(4 + (-2))$$

$$= (6)(2)$$

$$= 12$$

**Application:** Jimmy went to Tim Horton's during their "Roll up the Rim" season and won a bike. However, in order to get the bike, he had to answer the following skill testing question:  $4 + 4 \div 2 \times (3 + 1)$ . Jimmy answered 16. Did he get the bike?

$$= 4 + 4 \div 2 \times 4$$

$$= 4 + 2 \times 4$$

$$= 4 + 8$$

$$= 12$$



#### Success Criteria:

- I can BEDMAS
- I can solve multi-step questions using the proper order of operations
- I can safely substitute numbers into parentheses/brackets