

Math 9 – Unit 4: Word Problems

Lesson #2: Solving Word Problems

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Learning Goal: We are learning to solve various word problems.

To solve a word problem, carefully read the question, create the "LET" statements, create the equation, solve the equation, then finally ANSWER THE QUESTION!

a) The Mackenzie River is 1183 km longer than the St. Lawrence River. The sum of their lengths is 7299 km. How long is each river?

Let: Mackenzie River = $x + 1183$
St. Lawrence River = x

Equation: $(x + 1183) + (x) = 7299$

$$\begin{array}{r} 2x + 1183 = 7299 \\ -1183 \quad -1183 \end{array}$$

$$\frac{2x}{2} = \frac{6116}{2}$$

$$x = 3058$$

∴ The St. Lawrence River is 3058 km and the Mackenzie River is 4241 km

b) The sum of two numbers is 46. One number is 12 more than the other number. What are the numbers?

Let: number 1 = $x + 12$
number 2 = x

Equation: $(x + 12) + (x) = 46$

$$\begin{array}{r} 2x + 12 = 46 \\ -12 \quad -12 \end{array}$$

$$\frac{2x}{2} = \frac{34}{2}$$

$$x = 17$$

∴ The two numbers are 17 and 29.

c) The length of a rectangle is 5m more than its width. If the perimeter is 90m, what are the dimensions?

Let: width = x
length = $x+5$

$x+5$
 $P=90$

 x

Equation: $2w + 2l = P$
 $2(x) + 2(x+5) = 90$
 $2x + 2x + 10 = 90$
 $4x + 10 = 90$
 $\quad -10 \quad -10$
 $4x = 80$
 $\frac{4x}{4} = \frac{80}{4}$
 $x = 20$

\therefore the width is 20 cm and the length is 25 cm

4, 5, 6

\nearrow in a row

d) The sum of 3 consecutive numbers is 105. Find the numbers.

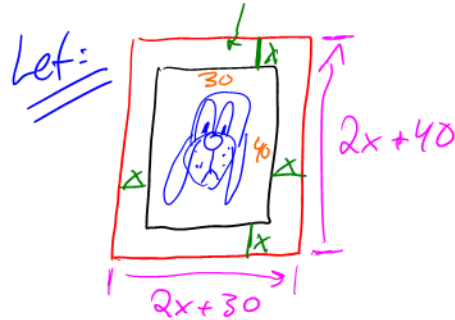
Let: number 1 = x
number 2 = $x+1$
number 3 = $x+2$

Equation: $(x) + (x+1) + (x+2) = 105$
 $3x + 3 = 105$
 $\quad -3 \quad -3$
 $3x = 102$
 $\frac{3x}{3} = \frac{102}{3}$
 $x = 34$

\therefore the 3 numbers are 34, 35, and 36.

e) The maximum life span of a brown bear is ten times the maximum life span of a mouse. The sum of their life spans is 33 years. What are the maximum life spans of each animal?

f) A picture measures 40 cm by 30 cm. The outside perimeter of the frame around the picture is 156 cm. What is the width of the border?



Equation: $2w + 2l = P$

$$2(2x+30) + 2(2x+40) = 156$$

$$4x + 60 + 4x + 80 = 156$$

$$8x + 140 = 156$$

$$\begin{array}{r} -140 \end{array} \quad \begin{array}{r} -140 \end{array}$$

$$\frac{8x}{8} = \frac{16}{8}$$

$$x = 2$$

\therefore the width of the border is 2 cm.

g) Together, Mary and Luke are 46 years old. If Luke is two years younger than 3 times Mary's age, how old are they?

Let: Luke = $3x - 2$
 Mary = x

Equation: $(x) + (3x - 2) = 46$

$$4x - 2 = 46$$

$+2$ $+2$

$$\frac{4x}{4} = \frac{48}{4}$$

$$x = 12$$

\therefore Mary is 12 years old
 and Luke is 34 years old.

h) There are 23 animals in the field. Some are pigs and some are chickens. There are 76 legs in all. How many of each animal are in the field?

Let # of pigs = $23 - x$ # of chickens = x

$23 - x$

Equations: $4(\underbrace{23 - x}_{\text{\# of pigs}}) + 2(\underbrace{x}_{\text{\# of chickens}}) = 76$

$$92 - 4x + 2x = 76$$

$$92 - 2x = 76$$

-92 -92

$$-2x = -16$$

$\underline{-2}$ $\underline{-2}$

$$x = 8$$

\therefore There are 8 chickens and 15 pigs in the field.

Success Criteria:

- I can identify the unknown variable in a given word problem
- I can create an equation that models a given word problem
- I can find the solution to the word problem by solving the equation
- I can express my solution in a complete sentence