

Math 9 – Unit 3: Solving Equations

Lesson #2: Solving with Variables on Both Sides

Name: Mr. Hagen
 Date: October 4, 2021

Learning Goal: We are learning to solve equations with variable on both sides.

In many equations that you will see for the rest of your Mathematical career (may it be long and fruitful), the variable will be scattered throughout the equation, even on both sides! The goal is to collect the variables on the same side and move all the constants to the other side.

a) $5x = 4x + 7$
 $-4x \quad -4x$
 $x = 7$

$5(7) = 35$
 $4(7) + 7$
 $28 + 7$
 35

b) $5y = 9y - 8$
 $-9y \quad -9y$
 $-4y = -8$
 $-4 \quad -4$
 $y = 2$

c) $-30 + 5x = 2x$
 $-5x \quad -5x$
 $-30 = -3x$
 $-3 \quad -3$
 $10 = x$

d) $2w = 0.35 - 5w$
 $+5w \quad +5w$
 $7w = 0.35$
 $7 \quad 7$
 $w = 0.05$

e) $2m + 3m = 8m - 3$
 $5m = 8m - 3$
 $-8m \quad -8m$
 $-3m = -3$
 $-3 \quad -3$
 $m = 1$

f) $5p - 3p = 6 - p$
 $2p = 6 - p$
 $+1p \quad +1p$
 $3p = 6$
 $3 \quad 3$
 $p = 2$

First clean up
the sides before
solving.

g) $8y = 5y + y + 14$
 $-6y \quad -6y$
 $2y = 14$
 $2 \quad 2$
 $y = 7$

h) $3n = 10.1 + 9.9 - 2n$
 $3n = 20 - 2n$
 $+2n \quad +2n$
 $5n = 20$
 $5 \quad 5$
 $n = 4$

Variable = constants

$$i) 8k - 3 = 4k + 17$$

$$\begin{array}{r} -4k + 3 \\ \hline 4k = 20 \\ \hline k = 5 \end{array}$$

$$4k = 20$$

$$\frac{4k}{4} = \frac{20}{4}$$

$$k = 5$$

$$j) -10x + 14 = 18 - 2x$$

$$\begin{array}{r} +2x -14 \\ \hline -8x = 4 \\ \hline x = -\frac{1}{2} \text{ or } x = -0.5 \end{array}$$

$$\frac{-8x}{-8} = \frac{4}{-8}$$

$$x = -\frac{1}{2} \text{ or } x = -0.5$$

$$k) 2u + 10 = 9 - 3u + 11$$

$$\begin{array}{r} 2u + 10 = 20 - 3u \\ -2u -20 \\ \hline -10 = -5u \\ \hline 2 = u \end{array}$$

$$\frac{-10}{-5} = \frac{-5u}{-5}$$

$$2 = u$$

$$l) 16 + 3x - 9 = -3 + 8x + 10$$

$$\begin{array}{r} 7 + 3x = 7 + 8x \\ -7 -8x \\ \hline -5x = 0 \\ \hline x = 0 \end{array}$$

$$\frac{-5x}{-5} = \frac{0}{-5}$$

$$x = 0$$

$$m) -29k - 18 + 11 = -36k - 10k - 177$$

$$\begin{array}{r} -29k - 7 = -46k - 177 \\ +46k + 7 \\ \hline 17k = -170 \\ \hline k = -10 \end{array}$$

$$\frac{17k}{17} = \frac{-170}{17}$$

$$k = -10$$

$$n) 6x - 4 - 2x = 4x + 8$$

$$\begin{array}{r} 4x - 4 = 4x + 8 \\ -4x + 4 \\ \hline 0x = 12 \\ \hline 0 = 12 \text{ Not true} \end{array}$$

$$0x = 12$$

$$0 = 12$$

Not true \therefore undefined, no solution.

| | |
|----------|---------------------------|
| $\{$ | $\{$ |
| $0x = 0$ | $6 = 6$ |
| $0 = 0$ | True! Infinite Solutions. |

Success Criteria:

- I can solve equations by grouping variables on one side of the equation, and constants on the other side of the equation