

# Math 9 – Unit 4: Word Problems

## Lesson #3: Solving Word Problems

Name: M. Hagen

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**Learning Goal:** We are learning to solve various word problems.

**To solve a word problem, carefully read the question, create the "LET" statements, create the equation, solve the equation, then finally ANSWER THE QUESTION!**

a) The Mackenzie River is 1183 km longer than the St. Lawrence River. The sum of their lengths is 7299 km. How long is each river?

Let: Mack River =  $x + 1183$   
St. Lawrence River =  $x$

Equation:  $x + 1183 + x = 7299$

$$2x = \frac{6116}{2}$$

$$x = 3058$$

∴ The St. Lawrence River is 3058 km and the Mack River is 4241 km

c) The length of a rectangle is 5m more than its width. If the perimeter is 90m, what are the dimensions?

Let: Length =  $x + 5$   
width =  $x$

$P = w + w + l + l$   
 $P = 2w + 2l$

Equation:  $2(x) + 2(x + 5) = 90$

$$2x + 2x + 10 = 90$$

$$4x = 80$$

$$x = 20$$

∴ The width is 20m and the length is 25m.

b) The sum of two numbers is 46. One number is 12 more than the other number. What are the numbers?

Let: number one =  $x$   
number two =  $x + 12$

Equation:  $x + x + 12 = 46$

$$2x = 34$$

$$x = 17$$

∴ the two numbers are 17 and 29.

d) The sum of 3 consecutive numbers is 105. Find the numbers.

Let: number 1 =  $x$   
number 2 =  $x + 1$   
number 3 =  $x + 2$

Equation:  $x + x + 1 + x + 2 = 105$

$$3x + 3 = 105$$

$$3x = 102$$

$$x = 34$$

∴ The three numbers are 34, 35, and 36.

e) The maximum life span of a brown bear is ten times the maximum life span of a mouse. The **sum** of their life spans is 33 years. What are the maximum life spans of each animal?

Let: bear =  $10x$   
mouse =  $x$

Equation:  $10x + x = 33$

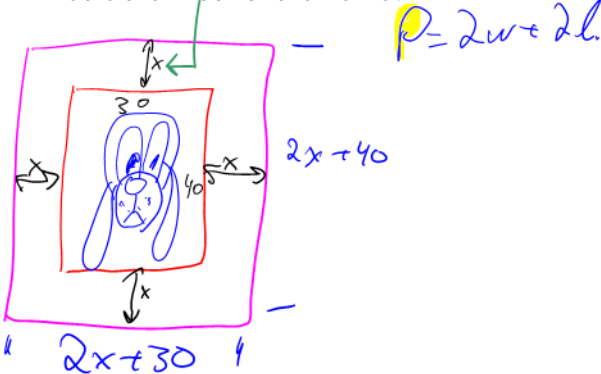
$$\frac{11x}{11} = \frac{33}{11}$$

$$x = 3$$

∴ the mouse's max life span is 3 years and the bear is 30 years.

f) A picture measures 40 cm by 30 cm. The outside **perimeter** of the frame around the picture is 156 cm. What is the width of the frame?

Let:



Equation:  $2(2x + 30) + 2(2x + 40) = 156$

$$4x + 60 + 4x + 80 = 156$$

$$8x + 140 = 156$$

$$\frac{8x}{8} = \frac{16}{8}$$

$$x = 2$$

∴ the width of the frame is 2 cm. thickness

#### Success Criteria:

- I can identify the unknown variable in a given word problem
- I can create an equation that models a given word problem
- I can find the solution to the word problem by solving the equation
- I can express my solution in a complete sentence

g) **Together**, Mary and Luke are 46 years old. If Luke is two years younger than 3 times Mary's age, how old are they?

Let: Luke =  $3x - 2$   
Mary =  $x$

Equation:  $3x - 2 + x = 46$

$$4x = 48$$

$$x = 12$$

∴ Mary is 12 and Luke is 34

h) There are **23 animals** in the field. Some are pigs and some are chickens. There are 76 legs in all. How many of each animal are in the field?

Let: Chickens =  $x$  (2 legs)  
Pigs =  $23 - x$  (4 legs)

Equation:  $2(x) + 4(23 - x) = 76$

$$2x + 92 - 4x = 76$$

$$\frac{-2x}{-2} = \frac{-16}{-2}$$

$$x = 8$$

∴ There are 8 chickens and 15 pigs.