

Name: _____

Math 10 Unit

Systems of Linear Equations

Learning Goals. We are learning to:

- o create the graphs which represent given linear equations;
- o determine a solution to a linear system graphically;
- o explain what the solution to a linear system means;
- o determine a solution to a linear system algebraically by substitution;
- o determine a solution to a linear system algebraically by elimination; and
- o create and solve a linear system which models a given situation (word problem)

Solving Linear Systems

“Solving” a Linear System means finding the solution which is the point at which all the lines intersect. A solution will always satisfy each equation of the Linear System. A Linear System can intersect in 3 ways:

One	None	Infinite

We will refer to the solution as the Point of Intersection **POI = (x , y)**

Method 1: Solve by Graphing:

Steps:

1. **Graph** the 2 linear equations
2. **State the POI** (Point of Intersection) by stating “POI = (x , y)”

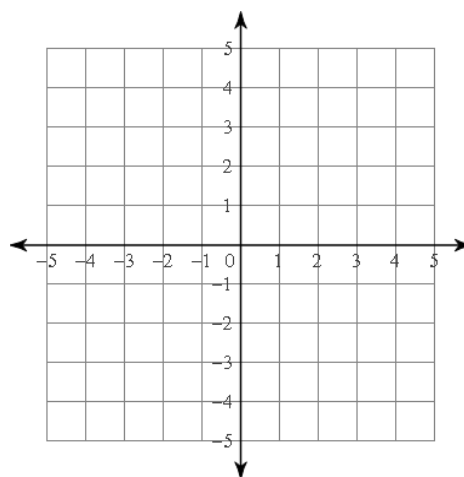
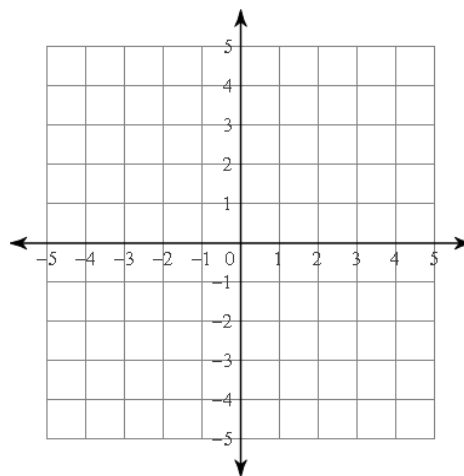
Examples

$$y = -6x - 4$$

$$y - 2x = 4$$

$$y = -\frac{2}{3}x - 2$$

$$y = -4$$



Method 2: Solve by Substitution:

Steps:

1. Isolate
2. Substitute
3. Solve
4. State the POI

Examples

$$\begin{aligned}x &= -6y - 11 \\ x &= y + 3\end{aligned}$$

$$\begin{aligned}2x + y &= -15 \\ 3x - y &= -15\end{aligned}$$

$$\begin{aligned}y - 3x &= 5 \\ y + x &= 3\end{aligned}$$

$$\begin{aligned}4x + y &= 11 \\ x + 2y &= 8\end{aligned}$$

Method 3: Solve by Elimination:

Steps:

1. Arrange
2. Same
3. Eliminate
4. Solve
5. State the POI

Examples

$$\begin{aligned}4x + 3y &= -15 \\ x - 3y &= 0\end{aligned}$$

$$\begin{aligned}-5x + 3y &= -1 \\ -7x + 3y &= -11\end{aligned}$$

$$\begin{aligned}3x + 4y &= -6 \\ 5x + 6y &= -8\end{aligned}$$

$$\begin{aligned}4x &= -2y + 24 \\ -x - 3y &= -21\end{aligned}$$

Unit 1 - Linear Systems: Success Criteria

1. I can determine the best method to use to solve the system.
 - a) I can solve by Graphing: Usually used for applications comparing two scenarios.
To be successful:
 1. use an appropriate scale
 2. use a ruler label: axes, equations scale, pencil .
 3. Be able to interpret the graph to state the solution.
 - b) I can solve By Substitution:
To be successful:
 1. Rewrite one equation to Isolate "x" or "y".
 2. Substitute the new equation into the other equation.
 3. Solve for one variable,
 4. Substitute found value in #3 and solve for the other.
 - c) I can solve By Elimination:
To be successful:
 - 1) Set up the equations so one of the variables have opposite coefficients.
 - 2) Add the equations together to eliminate one variable and solve for the other.
 - 3) Substitute found value in #2 and solve for the other variable.
2. I can clearly state the solution POI = (,).
3. I can check the solution.

To create a linear system: (Application Word problems)

1. I can Interpret the question to Identify the unknown variables (x and y)
2. I can Interpret the question to create 2 equations to represent the information in the question in one of 3 formats:
 - a. $y=mx+b$
 - b. $x + y = \text{total (sum)}$
 - c. _____ x + _____ y = _____ total where _____ is a #, \$ or %
 - i. $\$4x + \$2y = \$ 250$
 - ii. $13\% x + 35\% y = 25\% \text{ total}$
3. I can Solve the system using graphing, substitution or elimination (see above criteria)
4. I can state the solution, ensuring that it answers the question.
5. I can check the solution.

Word Problems- Review**All questions need to follow this format:**

1. Establish the unknowns (usually x and y). These are called the “Let statements”.
2. Create the two equations. Label/name the equations.
3. Solve. You may use elimination or substitution (or graphing).
4. Write the answer in a sentence statement.

Type 1: $y=mx+b$ or “total cost = variable price + set/constant cost”

A house needs some plumbing work done, so two plumbers are called. Pipe Cleaners charges \$120 service fee and then \$60/h. Water Works charges \$80 for showing up plus \$75/h.

Thinking Questions: If you need them for 2 hours, how much will each plumber cost? If you need them for 3 hours, how much will each plumber cost? See the pattern? Now use it to create your equations!!!

Now the real question: After how many hours do the two plumbers charge the same amount? How much do they charge at that time?

Another Type 1 Example:

Jasmyne is a car salesperson, and she earns \$500/week plus 6% commission selling cars. She noticed a job posting at another company that offered \$800/week plus 4% commission. How much does Jasmyne need to sell to earn the same at both jobs? Should she switch jobs?

Type 2: Selling or buying two items for a total cost. Prices of items are unknown.

Marcus and his friends are having a Final Four party. Marcus buys 5 burgers and 9 drinks for \$28.75 at the Beefy Burger joint. When more of his friends show up, he heads back to the Beefy Burger joint for 10 more burgers and 10 more drinks, spending \$47.50. How much is the cost of one burger and one drink?

Another Type 2 Example:

The school that Chelsea goes to is selling tickets to the annual talent show. On the first day of ticket sales the school sold 11 student tickets and 4 adult tickets for a total of \$166. The school took in \$124 on the second day by selling 11 student tickets and 1 adult ticket. Find the price of an adult ticket and the price of a student ticket.

Type 3: Sum and Difference (easy!)

Find the value of two numbers if their sum is 135 and their difference is 33.

The difference of two numbers is 10.56. Their sum is 167.42. Find the numbers.

Type 4: Sum of two unknowns coupled with other information.

A money jar contains 87 coins, made up of only dimes and quarters. The total value is \$10.90. How many of each coin is in the jar?

There are 23 animals in the field. Some are pigs and some are chickens. There are 76 legs in all. How many of each animal are in the field?

There are 17 vehicles lining up to get gas. Each car gets 8 gallons of gasoline. Each truck gets 19 gallons of gasoline. The station sells 169 gallons of gasoline. How many of each vehicle pumped gas?

Type 5: Mixture

Kali is working on a chemistry experiment. She needs 16 litres of a 25% acid solution. Unfortunately, she doesn't have any. The good news is that she does have a 50% acid solution and a 10% acid solution. She can use some 50% acid solution and dilute it with the 10% solution. How many litres of each solution does she need?

Jacob's Red-Hot Peanuts, which cost \$3.00/kg, are made by combining peanuts, which cost \$3.55/kg, with spices, which cost \$1.60/kg. Find the number of kg of peanuts and spices required to make 11.7kg of Jacob's Red-Hot Peanuts.

Note: This is not an exhaustive list. There could be others types. Use these as a guide.