Name: _____

Similar Triangles
and
Trigonometry

Unit Outline:

a. Review of Angle Theorems

b. Similar Triangles

c. Right Angle Triangle Ratios

d. Solving Triangles using Primary Trigonometric Ratios SOH CAH TOA

e. Sine Law

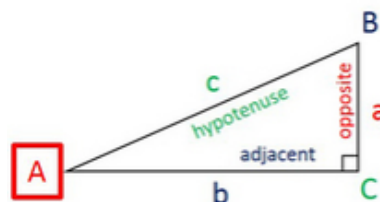f. Cosine Law

Formula Sheet

Pythagorean Theorem:

$$c^2 = a^2 + b^2$$

Right Angle Triangles SOHCAHTOA

$$\sin(A) = \frac{\text{opposite}}{\text{hypotenuse}} = \frac{a}{c}$$

$$\cos(A) = \frac{\text{adjacent}}{\text{hypotenuse}} = \frac{b}{c}$$

$$\tan(A) = \frac{\text{opposite}}{\text{adjacent}} = \frac{a}{b}$$

Sine Law

For the Sine Law we need: - An angle and its opposite side, and one other piece of information.
- OR SAS, ASA [and ASS (use with caution!)]

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C} \quad \text{or} \quad \frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$

The length of any side, divided by the Sine of its opposite angle is the same for all three pairs
If we are trying to **find an angle**, use the first form of the Sine Law (**angles on top**)
If we are trying to **find the length** of a side, use the second for of the law (**with sides on top**)

Cosine Law

For the Cosine Law we need: - 2 sides and the included angle.
- 3 sides

To find a side (have SAS):   To find an angle (have SSS):

$$a^2 = b^2 + c^2 - 2bc\cos A \qquad\qquad \cos A = \frac{a^2 - b^2 - c^2}{-2bc}$$

$$b^2 = a^2 + c^2 - 2ac\cos B \qquad\qquad \cos B = \frac{b^2 - a^2 - c^2}{-2ac}$$

$$c^2 = a^2 + b^2 - 2ab\cos C \qquad\qquad \cos C = \frac{c^2 - a^2 - b^2}{-2ab}$$

Lesson 1.0 - Trigonometry Prerequisite Skills

A Solving for x, to 2 decimal places if necessary.

$x^2 = 100$

$\Rightarrow x = \sqrt{100}$

$\Rightarrow x = \pm 10$

$x^2 = 3^2 + 4^2$

$\Rightarrow x^2 = 9 + 16 = 25$

$\Rightarrow x = \sqrt{25}$

$\Rightarrow x = \pm 5$

$8^2 + x^2 = 12^2$

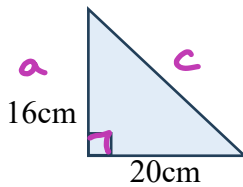$\Rightarrow 64 + x^2 = 144$

$\Rightarrow x^2 = 144 - 64$

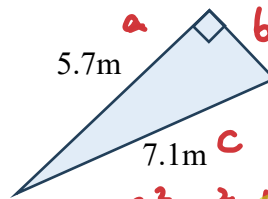$\Rightarrow x = \sqrt{80}$

$\Rightarrow x \approx \pm 8.9$

B The Pythagorean Theorem: Find the unknown side.

$c^2 = a^2 + b^2$

$c^2 = 16^2 + 20^2 = 256 + 400$

$c^2 = 656 \Rightarrow c = \sqrt{656} \Rightarrow c \approx 25.6\,cm$

$c^2 = a^2 + b^2$

$7.1^2 = 5.7^2 + b^2$
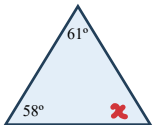
$7.1^2 - 5.7^2 = b^2$

$50.41 - 32.49 = b^2$

$\sqrt{17.92} = b$

$b \approx 4.2$

C Angle Theorems

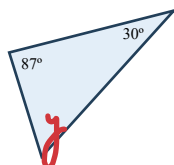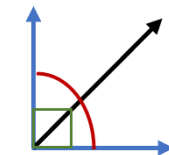Sum of a Triangle:
Angles in a triangle add up to __$180°$__   Comp $\angle s$ add to __$90°$__   Supp $\angle s$ add to __$180°$__

$x = 180 - 61 - 58$

$x = 61°$

$y = 180 - 30 - 87$

$y = 63°$

Complementary

Comp $(45°) = 45°$

Comp $(60°) = 30°$
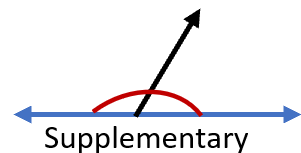
Supplementary

Sup. $(90°) = 90°$

Sup $(120°) = 60°$
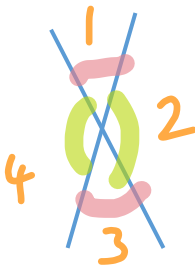
$\angle 1 = \angle 3$

$\angle 2 = \angle 4$

VERTICALLY OPPOSITE ANGLES

ANGLES around a POINT = 360°

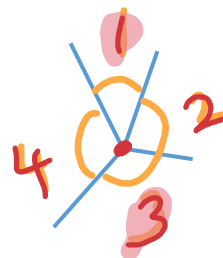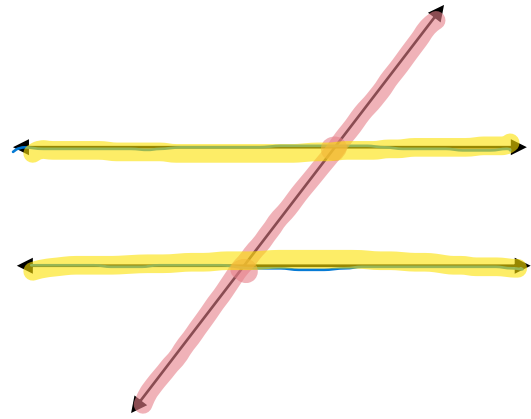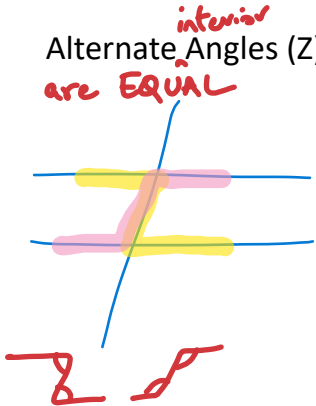$\therefore \angle 1 + \angle 2 + \angle 3 + \angle 4 = 360°$

Parallel Lines intersected by a TRANSVERSAL
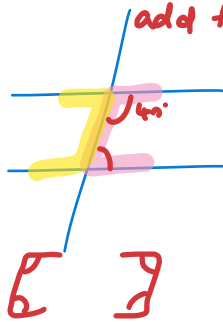
A <u>TRANSVERSAL</u> is a line that cuts two lines at two distinct points

Alternate Angles (Z)
interior
are EQUAL

Co-Interior Angles (C)
add to 180°

Corresponding Angles (F)
are EQUAL
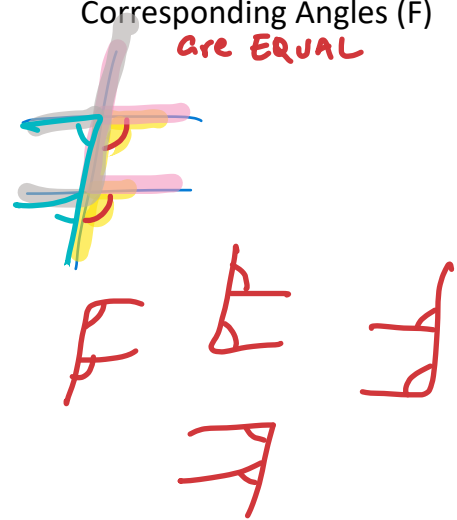
D Solving Proportions

$$\frac{3}{a} = \frac{5}{9}$$

$$\Rightarrow \frac{a}{3} = \frac{9}{5} \times 3$$

$$\Rightarrow a = \frac{9 \times 3}{5} = \frac{27}{5} = 5.4$$

$$\frac{x}{19} = \frac{2.3}{3}$$

$$\Rightarrow x = \frac{2.3 \times 19}{3}$$

$$\Rightarrow x = \frac{43.7}{3} \approx 14.6$$

$$\frac{2}{x+7} = \frac{4}{11}$$

$$\Rightarrow \frac{x+7}{2} = \frac{11}{4}$$

$$\Rightarrow x+7 = \frac{11 \times 2}{4} = \frac{22}{4} = 5.5$$

$$\Rightarrow x+7 = 5.5$$

$$\Rightarrow x = 5.5 - 7$$

$$\Rightarrow x = -1.5$$

PRACTICE

Solve Equations

1. Solve.

    a) $x^2 = 36$

    b) $x^2 - 6 = 19$

    c) $x^2 = 64 + 36$

    d) $x^2 = 5^2 + 12^2$

    e) $7^2 + x^2 = 25^2$

1) ANSWERS

a) $x^2 = 36$
$x = \sqrt{36}$
$x = \pm 6$

b) $x^2 - 6 = 19$
$x^2 = 19 + 6$
$x^2 = 25$
$x = \sqrt{25}$
$x = \pm 5$

c) $x^2 = 64 + 36$
$x^2 = 100$
$x = \sqrt{100}$
$x = \pm 10$

d) $x^2 = 5^2 + 12^2$
$x^2 = 25 + 144$
$x^2 = 169$
$x = \sqrt{169}$
$x = \pm 13$

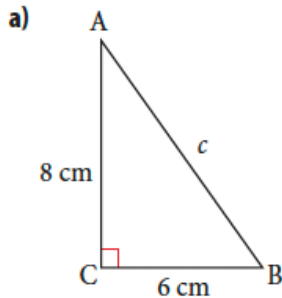e) $7^2 + x^2 = 25^2$
$49 + x^2 = 625$
$x^2 = 625 - 49$
$x = \sqrt{576}$
$x = 24$

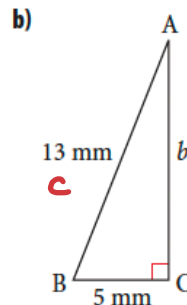### The Pythagorean Theorem

2. Find the measure of the unknown side.

a)

A, 8 cm, C, 6 cm, B, c

$c^2 = 8^2 + 6^2$
$c = \sqrt{64 + 36}$
$c = \sqrt{100}$
$\boxed{c = 10 \text{ cm}}$

b)

A, 13 mm, b, c, B, 5 mm, C, a

$13^2 = 5^2 + b^2$
$169 = 25 + b^2$
$169 - 25 = b^2$
$\sqrt{144} = b$
$\boxed{12 \text{ mm} = b}$

c) A, 16 m, C, 25 m, c, a, B
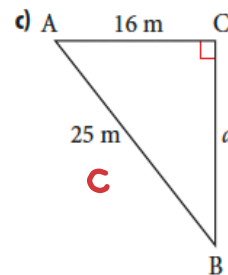
$25^2 = a^2 + 16^2$
$625 = a^2 + 256$
$625 - 256 = a^2$
$\sqrt{369} = a$
$\boxed{a \approx 19.2 \text{ m}}$

Rounding

8. Round each value to two decimal places.

    a) $3.4576 \approx 3.46$

    b) $19.832 \approx 19.83$

    c) $9015.98236 \approx 9015.98$

9. Evaluate each answer to one decimal place.

    a) $\sqrt{59} \approx 7.7$
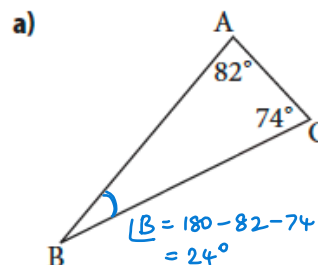
    b) $\sqrt{723} \approx 26.9$

    c) $\sqrt{0.85} \approx 0.9$

Angle Sum of a Triangle

10. Determine the measure of the missing angles.
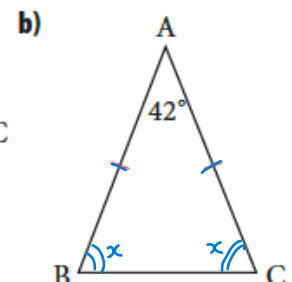
a)

A, 82°, 74° C, B

$\angle B = 180 - 82 - 74$
$= 24°$

b)

A, 42°, B, x, x, C
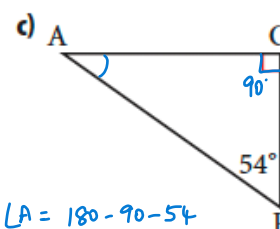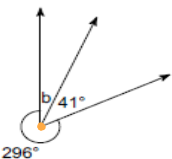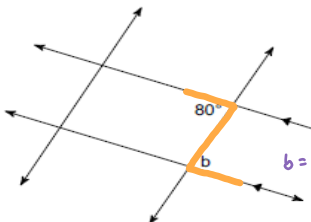
$2x + 42 = 180$
$2x = 180 - 42$
$x = \frac{138}{2} = 69°$
$\angle B = \angle C = 69°$

c)

A, C, 90°, 54°, B

$\angle A = 180 - 90 - 54$
$\angle A = 36°$
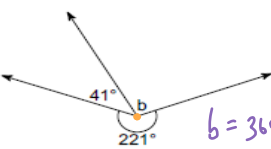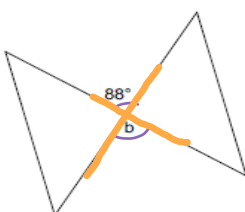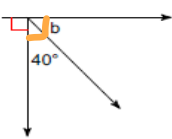
11. Angle Theorems
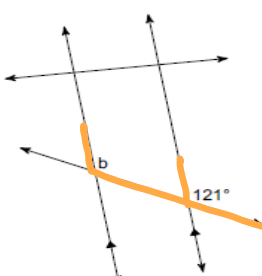
1)
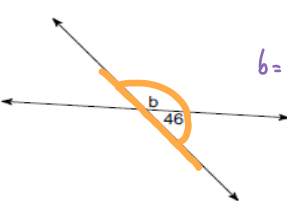
$b = 360 - 296 - 41$

$b = 23°$ (Angles around a point)

2)
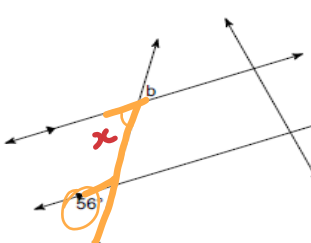
$b = 80°$ (Z-pattern)

3)
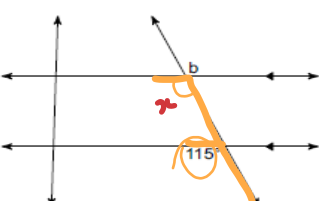
$b = 360 - 221 - 41$

$b = 98°$

4)
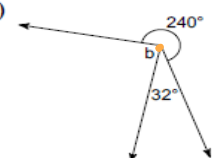
$b = 88°$ (Opposite angles)

5)

$b = 90 - 40 = 50°$

6)

$b = 121°$ (F-pattern)

7)

$b = 180 - 46 = 134°$

8)

$x = 56°$ (F-pattern)

$b = x = 56$ (opposite angles)

9)

$x = 115°$ (F-pattern)

$b = x = 115$ (opposite angles)

10)

$b = 360 - 240 - 32$ (angles around a point)

$b = 88°$

Prerequisite Skills, pages 4–5

1. a) $x = \pm6$ **b)** $x = \pm5$ **c)** $x = \pm10$
   d) $x = \pm13$ **e)** $x = \pm24$

2. a) 10 cm   **b)** 12 mm   **c)** 19.2 m

3. 5.8 m

4. a) 1:2   **b)** 3:7   **c)** 2:5

5. $10.50

6. a) $x = 3$ **b)** $x = 3$ **c)** $x = 20, y = 4$

7. a) 1 unit of distance on the map represents 700 000 of the same unit of distance on the earth.
   b) 84 km
   c) 5.7 cm

8. a) 3.46   **b)** 19.83   **c)** 9015.98

9. a) 7.7   **b)** 26.9   **c)** 0.9

10. a) 24°   **b)** 69°   **c)** 36°

11. 1)23°. 2)80°. 3)98°. 4)88°. 5)50°. 6)121°. 7)134°. 8)56°. 9)115°. 10)88°

Lesson 1.1 Congruence and Similarity in Triangles

Congruent Triangles are triangles which *are exactly the same in size and shape.*
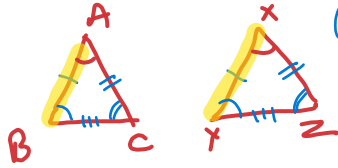
$$AB = XY \qquad \angle A = \angle X$$
$$BC = YZ \qquad \angle B = \angle Y$$
$$AC = XZ \qquad \angle C = \angle Z$$

Similar triangles are triangles which have the exact same angle measures but the side lengths have a different scale i.e. side lengths may be resized. The scale factor which is a ratio of corresponding side lengths states how much bigger (or smaller) the second triangle is compared to the first triangle through proportions. You can use this proportion to solve for the unknown side lengths.

$$\angle A = \angle X$$
$$\angle B = \angle Y$$
$$\angle C = \angle Z$$
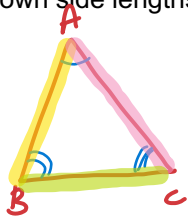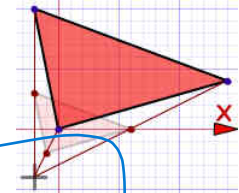
$$\frac{AB}{XY} = \frac{AC}{XZ} = \frac{BC}{YZ}$$

The following are similar triangles. Solve for unknown sides.
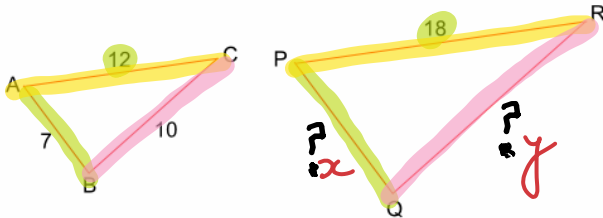
$$\frac{AB}{PQ} = \frac{AC}{PR} = \frac{BC}{QR}$$

$$\frac{7}{x} = \frac{\cancel{12}^{\,2}}{\cancel{18}_{\,3}} = \frac{10}{y}$$

$$\frac{7}{x} = \frac{2}{3}$$

$$21 = 2x$$

$$x = \frac{21}{2} = 10.5$$

$$\frac{2}{3} = \frac{10}{y} \quad {}^{\times 5}$$

$$2y = 30$$
$$y = \frac{30}{2}$$
$$y = 15$$

$$\Rightarrow y = 15$$

$$\boxed{\begin{array}{l} PQ = 10.5 \\ QR = 15 \end{array}}$$

$$\boxed{\begin{array}{l} XY = 14 \\ XZ = 24 \end{array}}$$
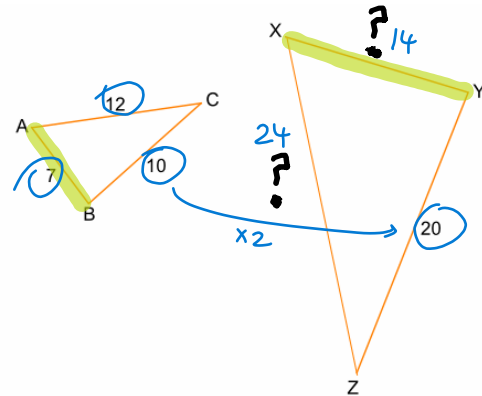
Mathematical Notation:

The ⌇ symbol is used to indicate similarity. The ≅ symbol is used to indicate congruence.

> **When naming triangles that are congruent or similar, the corresponding vertices must be listed in the same order.**

For example, if $\angle A = \angle D$, $\angle B = \angle E$ and $\angle C = \angle F$, then $\triangle ABC \sim \triangle DEF$. (ABC ≠ EDF)

$\triangle ABC \sim \triangle RST$. Complete each statement.

a) $\angle ABC = \angle RST$

b) $\angle BCA = \angle STR$

c) $\dfrac{AB}{RS} = \dfrac{BC}{ST} = \dfrac{AC}{RT}$

d) $\triangle STR \sim \triangle BCA$

e) $\dfrac{ST}{BC} = \dfrac{RS}{AB} = \dfrac{RT}{AC}$

f) $\angle SRT = \angle BAC$
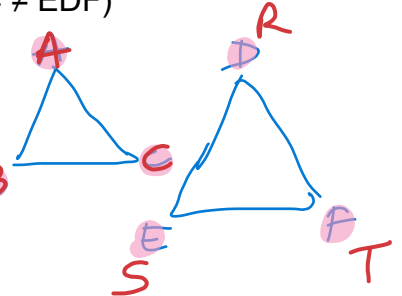
But How Do You Know the given Triangles are SIMILAR?

Properties of Similar Triangles – Symbol: ⌇

- Similar triangles have the exact same shape BUT have a different scale
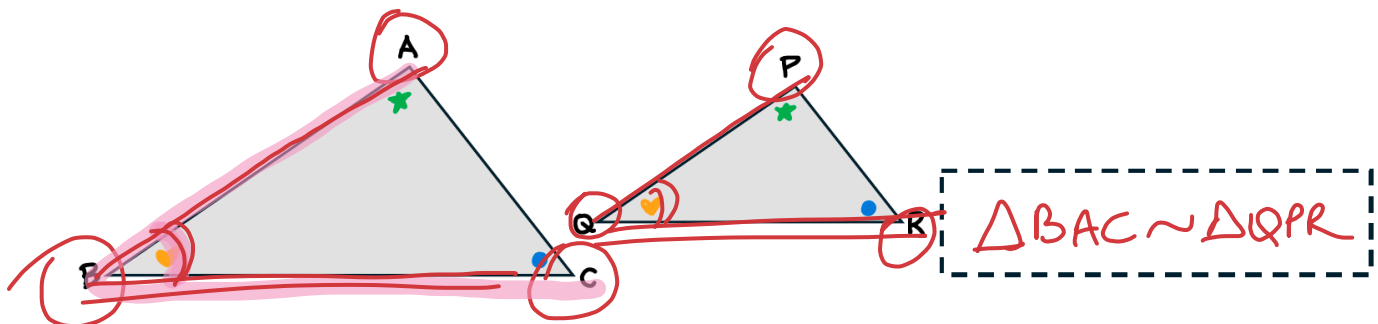
$\triangle BAC \sim \triangle QPR$

PROOF #1: Show that all three angles are equal (**AAA**) → ⌇ AA

$\angle ABC = \angle PQR$

$\angle BAC = \angle QPR$

$\angle ACB = \angle PRQ$

PROOF #2: Show that the ratios of the corresponding side lengths are equal (**SSS**)

$$\frac{AB}{PQ} = \frac{BC}{QR} = \frac{AC}{PR}$$

PROOF #3: (**SAS**) Show that 2 ratios of corresponding sides are equal and 1 angle is equal.

$$\frac{AB}{PQ} = \frac{BC}{QR} \; ; \; \angle B = \angle Q$$

Similarity Proofs	
Angle-Angle (AA)	If two angles of one triangle are congruent to two angles of another triangle, the triangles are similar.
SSS proportional	If the three sets of corresponding sides of two triangles are in proportion, the triangles are similar.
SAS proportional	If an angle of one triangle is congruent to the corresponding angle of another triangle and the lengths of the sides including these angles are in proportion, the triangles are similar.

Q1) Is ΔDEF similar to ~~ΔABC~~ ΔACB? What is the length of side DF? Provide Proof.

Statement
reason

SAS
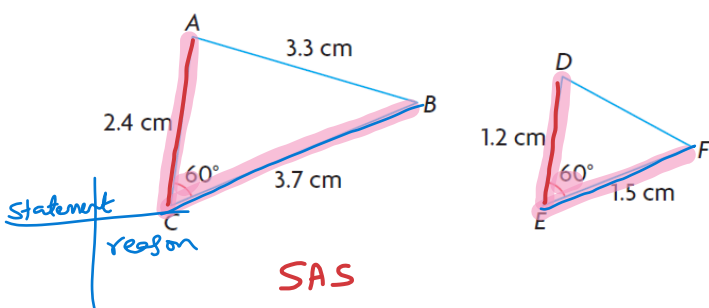
$$\angle C = \angle E \ (=60°)$$

$$\frac{AC}{DE} = \frac{2.4}{1.2} = 2$$

$$\frac{CB}{EF} = \frac{3.7}{1.5} = 2.467$$

$$\therefore \ \frac{AC}{DE} \neq \frac{CB}{EF}$$

$$\therefore \ \Delta DEF \not\sim \Delta ACB$$

Q2) Is ΔDEF ~ ΔACB ?
= What is the length of DF ?

SAS
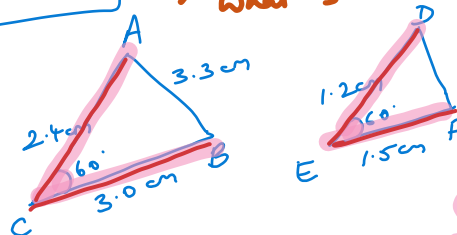
$$\boxed{\angle C = \angle E \ (=60°)}$$

$$\frac{AC}{DE} = \frac{2.4}{1.2} = 2$$

$$\frac{CB}{EF} = \frac{3.0}{1.5} = 2$$

$$\therefore \ \boxed{\frac{AC}{DE} = \frac{CB}{EF}}$$

$$\therefore \ \Delta DEF \sim \Delta ACB \ \boxed{(SAS)}$$

Example
a) Show that the two triangles to the right are similar, with reasons.
b) Determine *x and y*

a) Statement | Reason

6.0 cm

3.6 cm

C → E

8.0 cm

6.0 cm

y

B

x

A

D
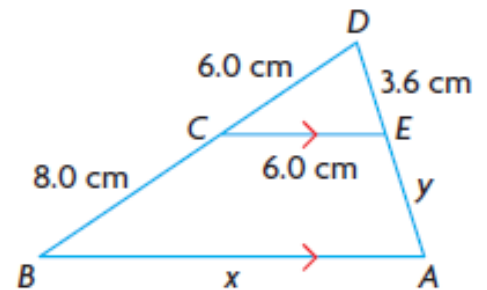
Example
A new bridge is going to be built across a river, but the width of the river cannot be measured directly. Surveyors set up posts at points A, B, C, D and *E*. Then they took measurements relative to the posts.
What is the width of the river?
a) Show that the two triangles in this diagram are similar.
b) Determine the width of the river

a) Statement | Reason

B

river

9 m

A

50 m

C

D

13 m

E
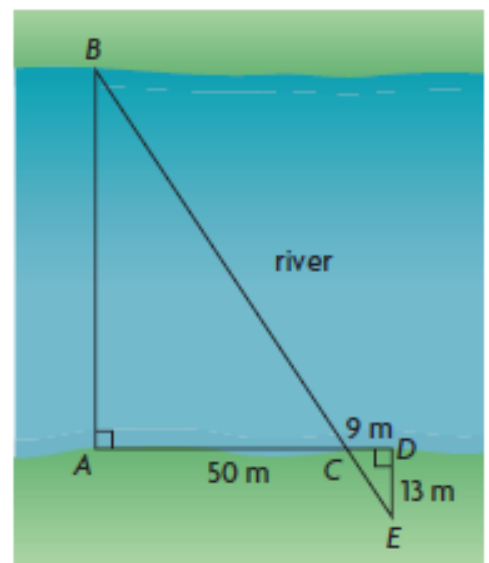
In order to solve "real world problems" you have to be SURE that the triangles you are working with are similar. All that is needed for proof of similarity is AA similarity.

1. Is $\triangle ABC \sim \triangle DEF$? Justify your answer.

A   5.4 cm   B

36°

67°

5.1 cm

3.3 cm

D   1.8 cm   E

36°

77°

1.7 cm   1.1 cm

C

F
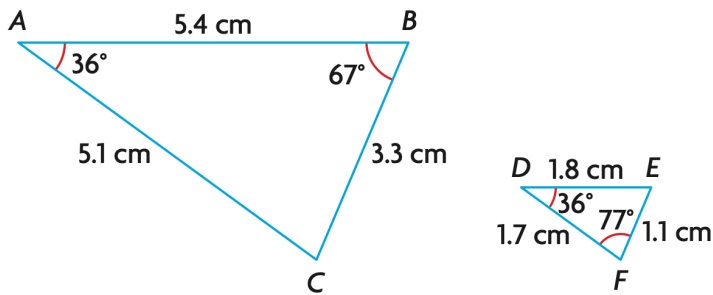
2. Suppose that $\triangle PQR \sim \triangle LMN$ and $\angle P = 90°$.
a) What angle in $\triangle LMN$ equals 90°? How do you know?
b) If $MN = 13$ cm, $LN = 12$ cm, $LM = 5$ cm, and $PQ = 15$ cm, what are the lengths of PR and QR?

3. Shiva is standing beside a lighthouse on a sunny day, as shown. She measures the length of her shadow and the length of the shadow cast by the lighthouse. Shiva is 1.6 m tall. How tall is the lighthouse?

lighthouse

Shiva
1.6 m

4.8 m

75.0 m

h
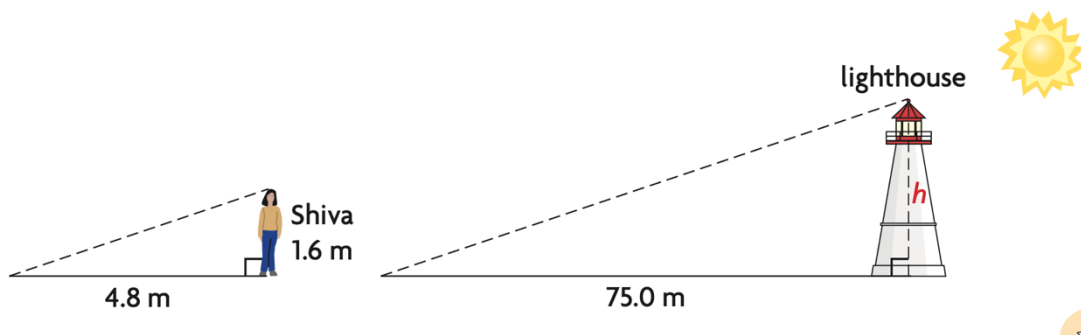
Lesson 1.2a Exploring Similar Right Angle Triangles

ΔADE ~ ΔAFG therefore AD ~ AF
AE~ AG
DE ~ FG
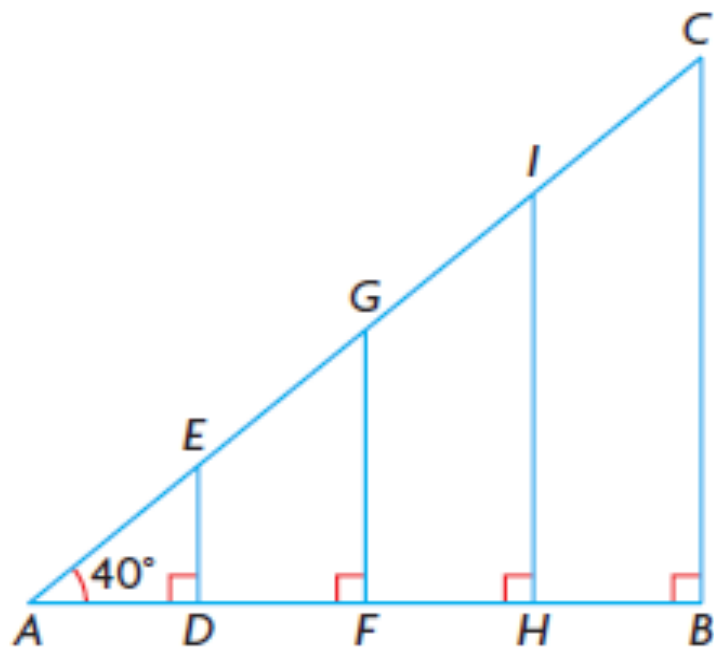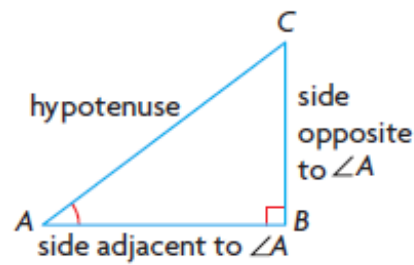
Use a ruler and measure the side lengths then calculate the ratios.

				Trigonometric Ratios		
Triangle	Side OPPOSITE to $\angle$A	Side ADJACENT to $\angle$A	HYPOTENUSE	OPPOSITE HYPOTENUSE	ADJACENT HYPOTENUSE	OPPOSITE ADJACENT
ΔABC						
ΔADE						
ΔAFG						
ΔAHI						

So, instead of saying $\frac{opp}{hyp}$, we call this ratio _____, and for $\frac{adj}{hyp}$ _____ and for $\frac{opp}{adj}$ _____

Mathematicians have calculated the side ratios for each possible angle and programmed the algorithms necessary into the scientific calculators. Even triangles with angles to the hundredth decimal place can be solved!

Having observed now that sides and angles of triangles are connected and related in so many different ways, we are ready to formally move into a brand-new branch of Mathematics called TRIGONOMETRY 😊

TRIGONOMETRY is the branch of Mathematics that deals with the properties of triangles and calculations based on these properties. As you will find out soon, Trigonometry has a lot of advantages in helping us solve real world problems.

Angle	Sine	Cosine	Tangent	Angle	Sine	Cosine	Tangent
1°	.0175	.9998	.0175	46°	.7193	.6947	1.0355
2°	.0349	.9994	.0349	47°	.7314	.6820	1.0724
3°	.0523	.9986	.0524	48°	.7431	.6691	1.1106
4°	.0698	.9976	.0699	49°	.7547	.6561	1.1504
5°	.0872	.9962	.0875	50°	.7660	.6428	1.1918
6°	.1045	.9945	.1051	51°	.7771	.6293	1.2349
7°	.1219	.9925	.1228	52°	.7880	.6157	1.2799
8°	.1392	.9903	.1405	53°	.7986	.6018	1.3270
9°	.1564	.9877	.1584	54°	.8090	.5878	1.3764
10°	.1736	.9848	.1763	55°	.8192	.5736	1.4281
11°	.1908	.9816	.1944	56°	.8290	.5592	1.4826
12°	.2079	.9781	.2126	57°	.8387	.5446	1.5399
13°	.2250	.9744	.2309	58°	.8480	.5299	1.6003
14°	.2419	.9703	.2493	59°	.8572	.5150	1.6643
15°	.2588	.9659	.2679	60°	.8660	.5000	1.7321
16°	.2756	.9613	.2867	61°	.8746	.4848	1.8040
17°	.2924	.9563	.3057	62°	.8829	.4695	1.8807
18°	.3090	.9511	.3249	63°	.8910	.4540	1.9626
19°	.3256	.9455	.3443	64°	.8988	.4384	2.0503
20°	.3420	.9397	.3640	65°	.9063	.4226	2.1445
21°	.3584	.9336	.3839	66°	.9135	.4067	2.2460
22°	.3746	.9272	.4040	67°	.9205	.3907	2.3559
23°	.3907	.9205	.4245	68°	.9272	.3746	2.4751
24°	.4067	.9135	.4452	69°	.9336	.3584	2.6051
25°	.4226	.9063	.4663	70°	.9397	.3420	2.7475
26°	.4384	.8988	.4877	71°	.9455	.3256	2.9042
27°	.4540	.8910	.5095	72°	.9511	.3090	3.0777
28°	.4695	.8829	.5317	73°	.9563	.2924	3.2709
29°	.4848	.8746	.5543	74°	.9613	.2756	3.4874
30°	.5000	.8660	.5774	75°	.9659	.2588	3.7321
31°	.5150	.8572	.6009	76°	.9703	.2419	4.0108
32°	.5299	.8480	.6249	77°	.9744	.2250	4.3315
33°	.5446	.8387	.6494	78°	.9781	.2079	4.7046
34°	.5592	.8290	.6745	79°	.9816	.1908	5.1446
35°	.5736	.8192	.7002	80°	.9848	.1736	5.6713
36°	.5878	.8090	.7265	81°	.9877	.1564	6.3138
37°	.6018	.7986	.7536	82°	.9903	.1392	7.1154
38°	.6157	.7880	.7813	83°	.9925	.1219	8.1443
39°	.6293	.7771	.8098	84°	.9945	.1045	9.5144
40°	.6428	.7660	.8391	85°	.9962	.0872	11.4301
41°	.6561	.7547	.8693	86°	.9976	.0698	14.3007
42°	.6691	.7431	.9004	87°	.9986	.0523	19.0811
43°	.6820	.7314	.9325	88°	.9994	.0349	28.6363
44°	.6947	.7193	.9657	89°	.9998	.0175	57.2900
45°	.7071	.7071	1.0000				

Lesson 1.2b The Primary Trigonometric Ratios

Given the Right $\triangle ABC$
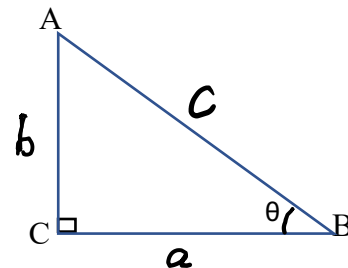
We use θ (Theta) to indicate angle in geometry.
*For any one of the two **non-right angle**s θ, we have an **adjacent side** and an **opposite side**.*
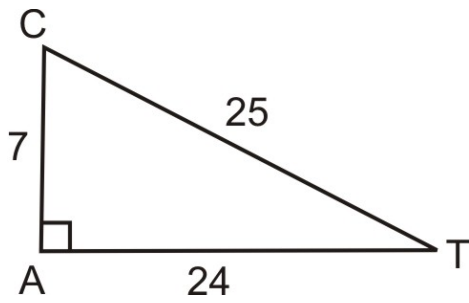
In the given triangle,
c -

a -

b -

The Trig Ratios

Sine: $\sin \theta =$

Cosine: $\cos \theta =$

Tangent: $\tan \theta =$

C

25

7

A   24   T

Examples $\triangle ACT$

Sine: sin T =

Cosine: cos T =

Tangent: tan T =

What is the Value of ∠T?

Sine   *Cosine*   *Tangent*

SOH CAH TOA

Let's Practice on our Scientific Calculators some more:

1. Find the value of each trigonometric ratio to the nearest ten-thousandth
    (_____ decimal places)

    a) $\sin 45 =$ b) $\cos 38 =$ c) $tan80 =$

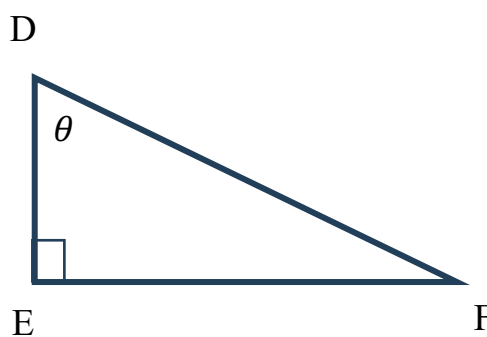2. Find each angle measure to the nearest degree

    a) $sin\theta = 0.422618$ b) $cos\theta = 4.393267$ c) $tan\theta = 0.176327$

SOH CAH TOA

Given Right ΔDEF, label

-   The Hypotenuse side
-   The Adjacent side
-   The Opposite side

The 3 TRIG RATIOS:

Sine: $\sin \theta =$	Cosine: $\cos \theta =$	Tangent: $\tan \theta =$

Lesson 1.3   Solving Right Angle Triangles

Solving for Sides using the Primary Trigonometric Ratios

Solve for the unknown in the following:
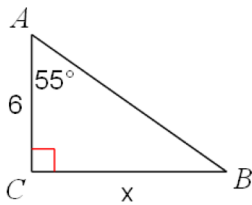
$\sin 35 = \frac{x}{8}$ $\tan 62 = \frac{3}{y}$

Notice: Pay close attention to when the unknown is in the numerator and when the unknown is in the denominator.

Steps to Solve: 1. Identify the given angle you are solving.
               2. Identify 1 known side and one unknown side.
               3. Write the appropriate Trig Ratio using #1 and 2 and solve

Solve for the unknown side in the following examples

SOH CAH TOA

SOH CAH TOA

Solving for Angles using the Primary Trigonometric Ratios

To solve for the angle, you must use the **INVERSE** function, which is Sin^{-1}, Cos^{-1}, Tan^{-1}

Solve for θ in the following examples

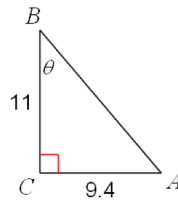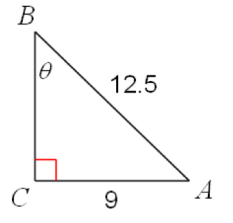$sinθ=0.4782$ $tanθ=2.01$ $cosθ=\frac{3}{5}$

$θ = sin^{-1} 0.4782$

$θ=$

Steps to Solve: 1. Identify the angle you are solving.
                         2. Identify 2 known sides.
                         3. Write the appropriate Trig Ratio using #2 and solve

Solve the Triangle (Find ALL missing measurements)

In $\triangle DEF$, $\angle E = 90°$, $d = 7.2cm$, and $f = 5.8cm$. Solve the triangle.

(Remember to draw Rough Figures always!! Math is a visual subject and Drawings are your best Friends!)

Lesson 1.4 Solving Right Triangle Real World Problems

Angle of Elevation vs Angle of Depression

The word "elevation" means "rise" or "move up". Angle of elevation is the angle between the horizontal and the line of sight to an object above the horizontal.

The word "depression" means "fall" or "drop". Angle of depression is the angle between the horizontal and the line of sight to an object beneath the horizontal.
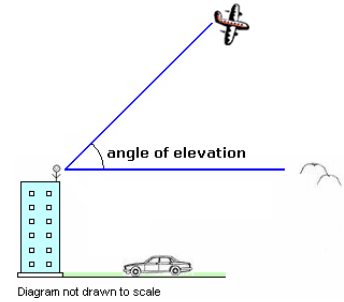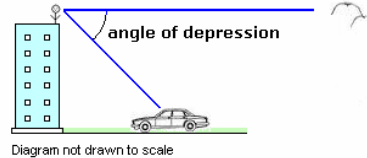
Word Problems

#4 A tree that is 9.5 m tall casts a shadow that is 3.8 m long. What is the angle of elevation of the Sun?

#6 A building code states that a set of stairs cannot rise more than 72 cm for each 100 cm of run. What is the maximum angle at which the stairs can rise?

#8 Firefighters dig a triangular trench around a forest fire to prevent the fire from spreading. Two of the trenches are 800 m long and 650 m long. The angle between them is 36°. Determine the area that is enclosed by these trenches.

#15   A video camera is mounted on top of a building that is 120 m tall. The angle of depression from the camera to the base of another building is 36°. The angle of elevation from the camera to the top of the same building is 47°a) How far apart are the two buildings?
b) How tall is the building viewed by the camera?

47°
36°
120 m
h
distance between
buildings
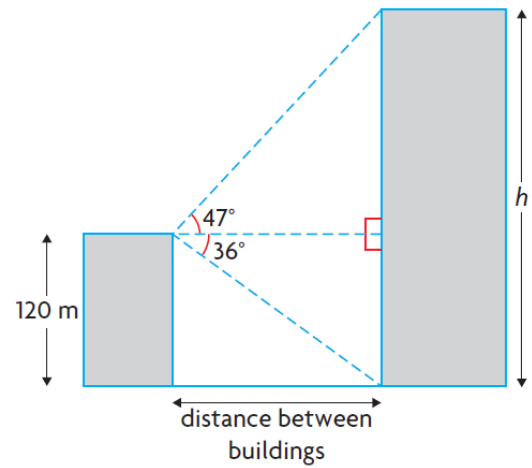
Understand that solving problems involves drawing a picture and then developing a plan to solve for the un-known.
This may take several steps, PATIENCE, and PRACTICE.

---*we've just concluded the first part of Trigonometry* ☺

Lesson 1.5 Sine Law *(Super useful when it is NOT a Right Triangle!!)*

For the Sine Law we need: - An angle and its opposite side, and one other piece of information.

The Sine Law:
$$\frac{a}{sinA} = \frac{b}{sinB} = \frac{c}{sinC} \quad \text{or} \quad \frac{sinA}{a} = \frac{sinB}{b} = \frac{sinC}{c}$$

where a is the side opposite $\angle A$, b is the side opposite $\angle B$, and c is the side opposite $\angle C$

If we are trying to **find an angle**, use the first form of the Sine Law (**angles on top**)
If we are trying to **find the length** of a side, use the second form of the law (**with sides on top**)

Ex 1.   Calculate
$$a = (\frac{3}{sin60})sin72$$

Ex 2. Calculate:
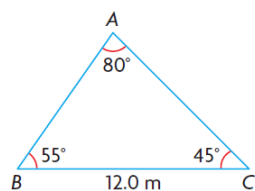$$sinA = (\frac{sin72}{15})12$$

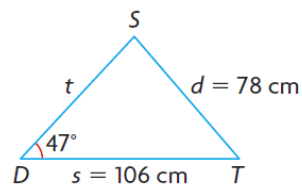Ex. 3 – Solve for the given variable (correct to 1 decimal place) in each of the following:

(a) $\dfrac{a}{\sin 55°} = \dfrac{12}{\sin 30°}$

(b) $\dfrac{35}{\sin 65°} = \dfrac{b}{\sin 38°}$

Ex 4 - Find the Length of Side b to the nearest tenth

A
80°
55°   45°
B   12.0 m   C

Ex. 5 – Find ∠S to the nearest degree.

S
t   d = 78 cm
47°
D   s = 106 cm   T

A telephone pole is supported by two wires on opposite sides. At the top of the pole, the wires form an angle of 60°. On the ground, the ends of the wires are 15.0 m apart. One wire makes a 45° angle with the ground. How long are the wires, and how tall is the pole?

Optional Extra Practice: Textbook Pg. 433 – 434 #2b, 3acdf, 4 – 8, 10, 11

Lesson 1.6 Cosine Law

Which Law do I Use?
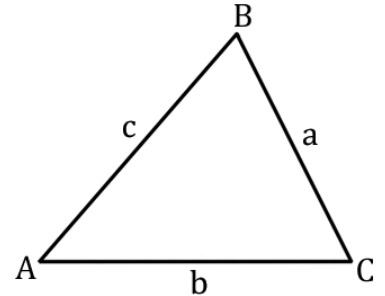
For the Cosine Law we need: - 2 sides and the included angle.
                                    - 3 sides

The cosine law is an extension of the Pythagorean theorem to triangles with no right angle.

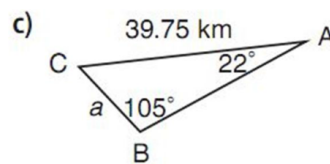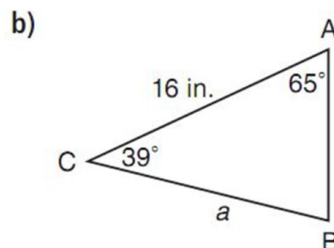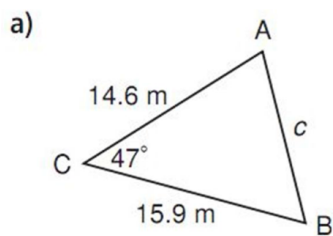| **To find a side (have SAS):**	**To find an angle (have SSS):**
$a^2 = b^2 + c^2 - 2bc\cos A$	$\cos A = \dfrac{a^2 - b^2 - c^2}{-2bc}$
$b^2 = a^2 + c^2 - 2ac\cos B$	$\cos B = \dfrac{b^2 - a^2 - c^2}{-2ac}$
$c^2 = a^2 + b^2 - 2ab\cos C$	$\cos C = \dfrac{c^2 - a^2 - b^2}{-2ab}$

Ex 1.   Calculate a if

$$a^2 = 4^2 + 6^2 - 2(4)(6)\cos 56$$

Ex 2. Calculate $\angle X$ if:

$$\cos X = \frac{4.5^2 - 3.2^2 - 4.6^2}{-2(3.2)(4.6)}$$

Determine if you need to use the SINE law or the COSINE law for the following triangles:

Draw the triangle and then find ∠A to the nearest tenth if a = 3m, b = 5m, and c = 4.7m

Draw the triangle then find side b, to the nearest tenth if ∠B = 68°, a = 17 cm, and c = 22 cm

Ex. 5 The bases in a baseball diamond are 90 ft apart. A player picks up a ground ball 11 ft from third base, along the line from second base to third base. Determine the angle that is formed between first base, the player's present position, and home plate.