

Name: _____

MCR3U Unit 6 Review - Exponential Functions

Practice Problems

1. Evaluate. Express your answer in rational form.

$$(-3)^{-4}$$

2. Evaluate. Express your answer in rational form.

$$7^{-3} \div \left(\frac{7^2}{7^{-1}} \right)^{-2}$$

3. Simplify the expression. Express your answer with positive exponents. Explain each of your steps.

$$\frac{m^{-4}n^{-6}}{mn^{-1}}$$

4. Simplify the expression. Express your answer with positive exponents.

$$\left(\frac{(4x^6)^3(4y^{-8})}{(2x)^4(12y^3)^2} \right)^{\frac{1}{2}}$$

5. Simplify the expression. Express your answer with positive exponents.

$$\frac{\sqrt{81z^{16}}}{\sqrt{100z^{-4}}}$$

6. Simplify the expression. Express your answer with positive exponents.

$$\left(\frac{(x^{12})^{0.25}(216x^9)}{(3x)^6(x^{18})^{0.5}} \right)^{-\frac{1}{3}}$$

7. The function $g(x) = -2(3^{2x-6}) + 9$ is the result of transformations of $f(x) = 3^x$. State the y -intercept, the horizontal shift and the horizontal asymptote.

8. A cup of hot liquid was left to cool in a room whose temperature was 18°C . The temperature changes according to

the function $T(t) = 80\left(\frac{1}{2}\right)^{\frac{t}{30}} + 18$, where t is in minutes. Determine the temperature of the liquid after:

- i) 30 minutes, ii) 60 minutes, iii) 5 hours

Explain the meaning of the y -intercept and the horizontal asymptote in the context of this problem.

9. A baker records the internal temperature of a pie that has been left to cool on a counter. The room temperature is 14°C . An equation that models this situation is $T(t) = 68(0.5)^{\frac{t}{10}} + 14$ where T is the temperature in degrees Celsius and t is the time in minutes. Determine the temperature, to the nearest degree, of the pie after 15 minutes. How much time did it take for the pie to reach an internal temperature of 31°C ?
10. A laptop computer loses its value each month after it is purchased. Its value as a function of time, in months, is modelled by $V(m) = 1800(0.92)^m$.
 What is the rate of depreciation?
 What is the value of the laptop after 3 months?
 In which month after it is purchased does the laptop's worth fall below \$1000?
11. The population of a town has grown at an annual rate of approximately 2.7%.
 Write an exponential function which will describe the town's population over time.
 How long will it take for its population of 18 450 people to double at this growth rate? Explain how you found your answer.
12. In 2001, a sum of \$4000 is invested at a rate of 6.5% per year for 5 years. What is the value of the investment when it matures?
13. Determine the exponent that makes the equation true.

$$13^x = \frac{1}{2197}$$
14. Simplify.

$$\left(\frac{r^3 s^{-1}}{r^2 s^6} \right)^{-1}$$
15. Solve for x .

$$\sqrt[3]{\frac{1}{64}} + \left(\frac{243}{x} \right)^{\frac{2}{5}} = \sqrt{\frac{25}{4}}$$
16. The doubling time for a certain type of cell is 4 h. The number of cells after t hours is described by $N(t) = N_0 2^{\frac{t}{4}}$ where N_0 is the initial population.
 Determine the number of cells after 24 hours if there were 3 cells initially.
 What are the domain and range of this function in the context of this problem?
17. An antique painting is purchased in 1980 for \$995. The value increases by 3.1% every year.
 Write an equation that models the value of the painting after t years.
 Determine the increase in value of the painting in the 6th year after it was purchased (from year 5 to year 6).
 Determine the increase in value of the painting in the 25th year after it was purchased.