

Prove the following identities on a separate sheet of paper.

Proving involves showing the "Left Side = Right Side".

- ① 1. $\sin A \cot A = \cos A$
- 2. $\cot \theta \sec \theta = \csc \theta$
- 3. $\sin \theta \sec \theta = \tan \theta$
- ② 6. $\cot A \sec A \sin A = 1$
- ③ 7. $(1 - \cos^2 A) \csc^2 A = 1$
- ④ 8. $\cot^2 \theta (1 - \cos^2 \theta) = \cos^2 \theta$
- 10. $(1 - \cos^2 A) \sec^2 A = \tan^2 A$
- ⑤ 11. $(1 + \tan^2 A) \cos^2 A = 1$
- 12. $(\sec^2 A - 1) \cot^2 A = 1$
- 14. $\sin^2 A (1 + \cot^2 A) = 1$
- 15. $(\csc^2 \theta - 1) \tan^2 \theta = 1$
- ⑥ 16. $\sin^2 \theta \cot^2 \theta + \sin^2 \theta = 1$
- ⑦ 17. $(1 - \cos^2 A)(1 + \cot^2 A) = 1$
- 18. $(1 + \tan^2 A)(1 - \sin^2 A) = 1$

- ⑧ 19. $\frac{\sin A}{\csc A} + \frac{\cos A}{\sec A} = 1$
- 20. $\frac{\sec A}{\cos A} - \frac{\tan A}{\cot A} = 1$
- ⑨ 21. $\sin^4 \theta - \cos^4 \theta = 2 \sin^2 \theta - 1$
- 22. $\sec^4 \theta - 1 = 2 \tan^2 \theta + \tan^4 \theta$
- 23. $\csc^4 A - 1 = 2 \cot^2 A + \cot^4 A$
- ⑩ 24. $\frac{\sin A \cot^2 A}{\cos A} = \frac{1}{\tan A}$
- 25. $\frac{\sec^2 A \cot A}{\csc^2 A} = \tan A$
- ⑪ 26. $\sec \theta - \tan \theta \sin \theta = \cos \theta$
- ⑫ 27. $\tan \theta + \cot \theta = \sec \theta \csc \theta$

Key Ideas

- A trigonometric identity is an equation involving trigonometric ratios that is true for all values of the variable.
- Some trigonometric identities are a result of a definition, while others are derived from relationships that exist among trigonometric ratios.

Need to Know

- Some trigonometric identities that are important to remember are shown below ($0^\circ \leq \theta \leq 360^\circ$).

Identities Based on Definitions		Identities Derived from Relationships	
Reciprocal Identities		Quotient Identities	Pythagorean Identities
$\csc \theta = \frac{1}{\sin \theta}$, where $\sin \theta \neq 0$	$\tan \theta = \frac{\sin \theta}{\cos \theta}$, where $\cos \theta \neq 0$	$\sin^2 \theta + \cos^2 \theta = 1$	
$\sec \theta = \frac{1}{\cos \theta}$, where $\cos \theta \neq 0$	$\cot \theta = \frac{\cos \theta}{\sin \theta}$, where $\sin \theta \neq 0$	$1 + \tan^2 \theta = \sec^2 \theta$	
$\cot \theta = \frac{1}{\tan \theta}$, where $\tan \theta \neq 0$		$1 + \cot^2 \theta = \csc^2 \theta$	

- To prove that a given trigonometric equation is an identity, both sides of the equation need to be shown to be equivalent. This can be done by
 - simplifying the more complicated side until it is identical to the other side or manipulating both sides to get the same expression
 - rewriting all trigonometric ratios in terms of x , y , and r
 - rewriting all expressions involving tangent and the reciprocal trigonometric ratios in terms of sine and cosine
 - applying the Pythagorean identity where appropriate
 - using a common denominator or factoring as required