

Math 9 – Unit 2: Algebra One

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Lesson #5: Dividing Monomials

Learning Goal: We are learning to divide by monomials.

We've added, subtracted, multiplied, and even raised monomials to powers. All that is left is dividing by monomials. First, let's develop a rule with numbers.

$$\text{Simplify } \frac{4^5}{4^3} = \frac{\cancel{4} \times \cancel{4} \times \cancel{4} \times \cancel{4} \times 4}{\cancel{4} \times \cancel{4} \times \cancel{4}} = 4^2$$

This leads to our 4th exponent law. When dividing, Subtract the exponents. Time to put it into practice!

$$\text{a) } \frac{x^8}{x^5} = x^3$$

$$\text{b) } \frac{y^{72}}{y^{46}} = y^{72-46} = y^{26}$$

$$\text{c) } \frac{m^5 n^3}{m^2 n^1} = m^{5-2} n^{3-1} = m^3 n^2$$

$$\text{d) } \frac{18p^6 q^9}{3p^2 q^2} = 6p^{6-2} q^{9-2} = 6p^4 q^7$$

The final step is to divide a monomial into a polynomial, such as $\frac{4x^5 - 2x^3 + 6x^2}{2x^2}$. However, first let's look back

at adding fractions so we can see an integral step that we will need to use:

$$\frac{4 \times 1}{4 \times 2} + \frac{3}{4} + \frac{5}{8} = \frac{4+6+5}{8} =$$

$$\frac{4}{8} + \frac{6}{8} + \frac{5}{8}$$

COMMON DENOMINATOR

Keep in mind when doing the following questions that the denominator gets applied to all the terms in the numerator.

$$\text{a) } \frac{4x^5 - 2x^3 + 6x^2}{2x^2}$$

$$= \frac{4x^5}{2x^2} - \frac{2x^3}{2x^2} + \frac{6x^2}{2x^2}$$

$$= 2x^3 - x + 3$$

$$\frac{x^2}{x^2}$$

$$\text{b) } \frac{16x^3 y^5 + 8x^2 y^4}{4x^2 y}$$

$$= \frac{16x^3 y^5}{4x^2 y} + \frac{8x^2 y^4}{4x^2 y}$$

$$= 4xy^4 + 2y^3$$

$$c) \frac{40a^3b^6 - 50a^2b^3 + 10ab}{10ab}$$

$$= \frac{40a^3b^6}{10ab} - \frac{50a^2b^3}{10ab} + \frac{10ab}{10ab}$$

$$= 4a^2b^5 - 5ab^2 + 1$$

$$d) \frac{9x^7 + 27x^5 - 15x^4}{-3x^3}$$

$$= \frac{9x^7}{-3x^3} + \frac{27x^5}{-3x^3} - \frac{15x^4}{-3x^3}$$

$$= -3x^4 - 9x^2 + 5x$$

$$e) \frac{192r^{78}s^{34} - 144r^{65}s^{53} - 256r^{98}s^{23} + 80r^{88}s^{45}}{16r^{33}s^{21}}$$

$$= \frac{192r^{78}s^{34}}{16r^{33}s^{21}} - \frac{144r^{65}s^{53}}{16r^{33}s^{21}} - \frac{256r^{98}s^{23}}{16r^{33}s^{21}} + \frac{80r^{88}s^{45}}{16r^{33}s^{21}}$$

$$= 12r^{45}s^{13} - 9r^{32}s^{32} - 16r^{65}s^2 + 5r^{55}s^{24}$$

Success Criteria:

- I can divide like variables by subtracting their exponents
- I can understand the difference between dividing coefficients and dividing variables
- I can divide the monomial into each term of a polynomial separately
- I can recognize that when you divide two identical monomials, the result is one.