

Mathematics 10D

8.1 Sine Law

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Goal: Explore the relationship between each side in an acute triangle and the sine of its opposite angle.

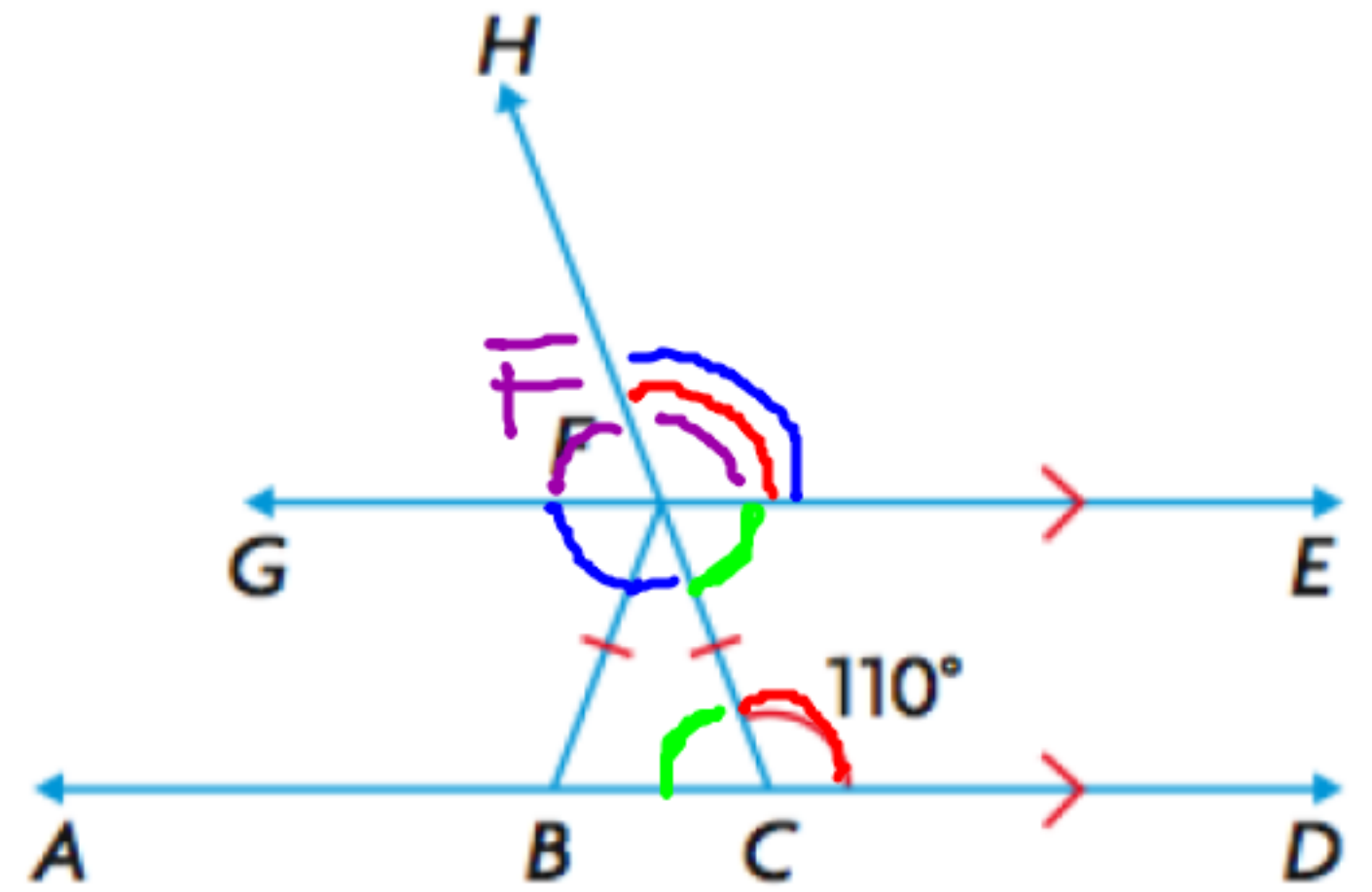
Acute triangle: 3 acute angles ($< 90^\circ$)



Supplementary Angles

$\angle A + \angle B = 180^\circ$

e.g. $\angle GFH + \angle EFH = 180^\circ$



Alternate Angles

$\angle BCF = \angle CFE$

b/c $GE \parallel AD$ (parallel)

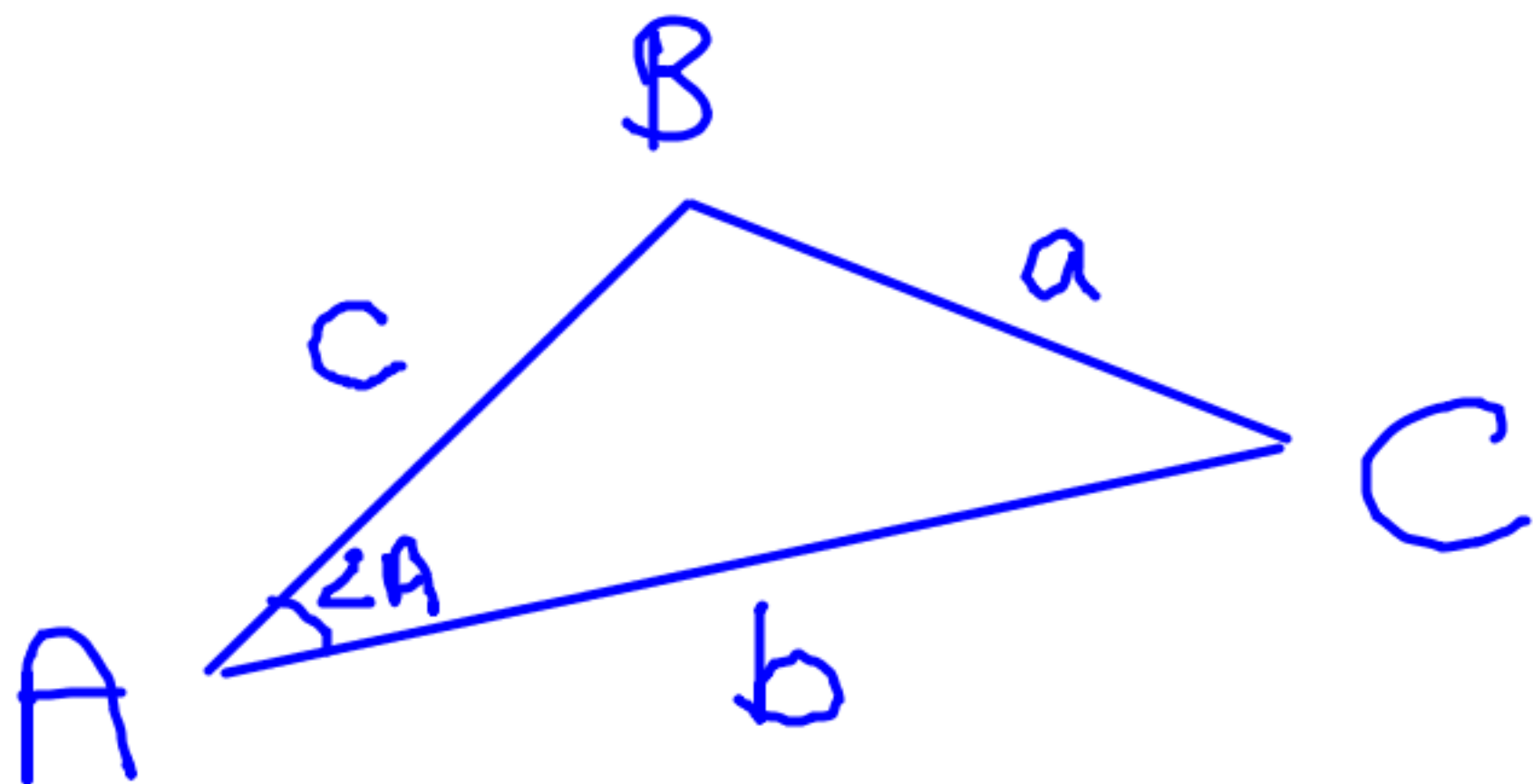
Opposite angle:



Corresponding Angles

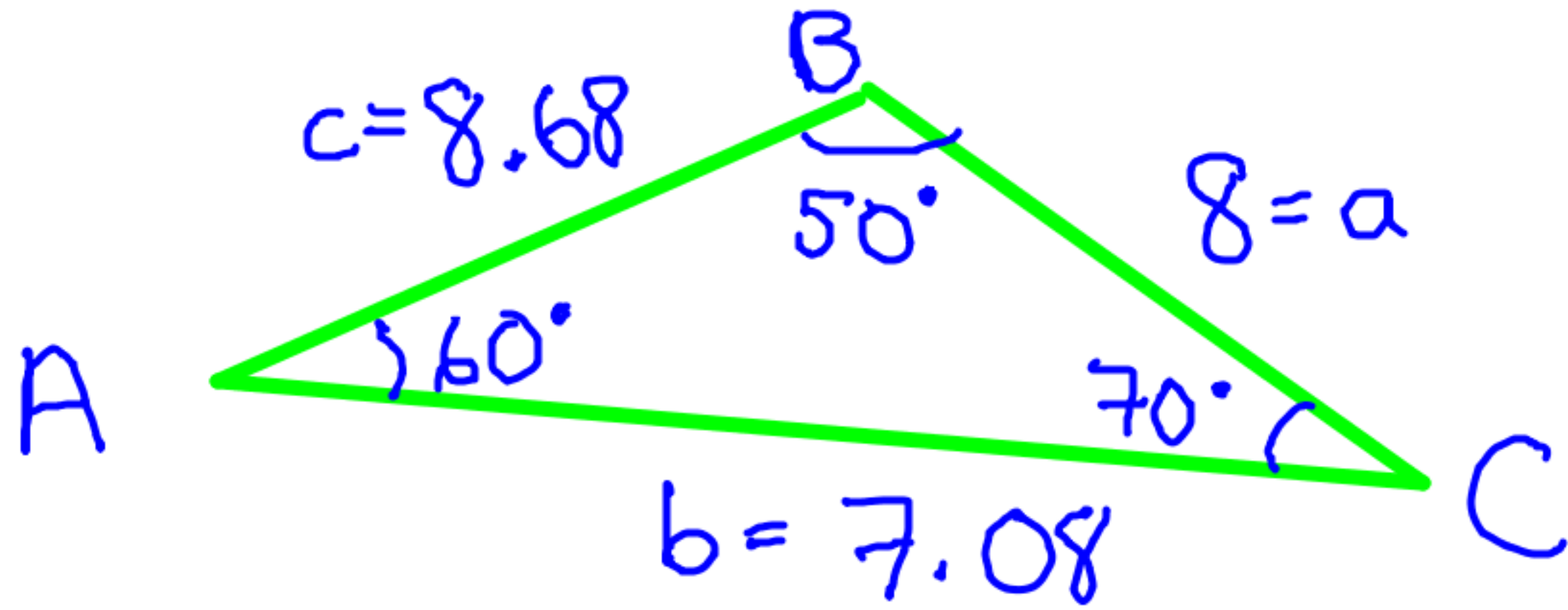
$\angle DCF = \angle EFH$ (b/c $GE \parallel AD$)

Sine Law:



$$\frac{\text{opposite side}}{\sin(\angle)}$$

$$\frac{a}{\sin(\angle A)} = \frac{b}{\sin(\angle B)} = \frac{c}{\sin(\angle C)}$$



$$\begin{aligned}
 & \frac{a}{\sin(\angle A)} \\
 = & \frac{8}{\sin(60^\circ)} \\
 = & \frac{8}{0.866} \\
 \approx & 9.24
 \end{aligned}$$

$$\begin{aligned}
 & \frac{b}{\sin(\angle B)} \\
 = & \frac{7.08}{\sin(50^\circ)} \\
 = & \frac{7.08}{0.766} \\
 \approx & 9.24
 \end{aligned}$$

$$\begin{aligned}
 & \frac{c}{\sin(\angle C)} \\
 = & \frac{8.68}{\sin(70^\circ)} \\
 = & \frac{8.68}{0.9397} \\
 \approx & 9.24
 \end{aligned}$$