

# Mathematics 11UC

## 3.3 – Solving Quadratic Equations

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$$f(x) = x^2 - 8x + 12$$

$$\overset{+3}{-3} = x^2 - 8x + \overset{+3}{12}$$

$$0 = x^2 - 8x + 15 \quad \begin{matrix} \textcircled{x} & 15 \\ \textcircled{+} & -8 \end{matrix} \quad -3, -5$$

$$0 = \underbrace{(x-3)}_{=0} \underbrace{(x-5)}_{=0}$$

$$x-3=0$$

$$\underline{x=3}$$

$$x-5=0$$

$$\underline{x=5}$$

What is the value of  $x$  when  $f(x) = -3$ ?

$$15^2 - 8(5) + 12$$

$$= 25 - 40 + 12$$

$$= -3$$

The population of an Ontario city is modelled by the function  $P(t) = 0.5t^2 + 10t + 300$ , where  $P(t)$  is the population in thousands and  $t$  is the time in years. Note:  $t = 0$  corresponds to the year 2000.

- a) What was the population in 2000?  $\rightarrow t = 0$   
b) What will the population be in 2010?  $\rightarrow t = 2010 - 2000 = 10$   
c) When is the population expected to be 1 050 000? 1050

$$\begin{aligned} \text{a) } P(0) &= 0.5(0)^2 + 10(0) + 300 \\ &= 300,000 \end{aligned}$$

$$\text{b) } P(10) = 450,000$$

c) in the year 2030, the pop will be 1,050,000.

The function  $h(t) = 2 + 50t - 1.862t^2$ , where  $h(t)$  is the height in metres and  $t$  is time in seconds, models the height of a golf ball above the planet Mercury's surface during its flight.

- a) What is the maximum height reached by the ball?  $\rightarrow 337.66 \text{ m}$   
b) How long will the ball be above the surface of Mercury?  $\rightarrow 26.89 \text{ seconds}$   
c) When will it reach a height of 200 m on the way down?  $\rightarrow 22 \text{ seconds}$

a) Find zeros, average them, then use that value as your  $x$ .

Zeros are:  $-0.0399$  and  $26.8928$

$$h = \frac{-0.0399 + 26.8928}{2} = 13.413$$