

1.5 Evaluating Limits

Don't forget: If you “*plug it in and see what happens*”, and get “ $\frac{0}{0}$ ”, then **MORE WORK** needs to be done.

Note: you may find the following helpful: $a^3 \pm b^3 = (a \pm b)(a^2 \mp ab + b^2)$

Evaluate the following Limits:

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| a) $\lim_{x \rightarrow -2} (3x^2 - 5x + 1)$ | b) $\lim_{x \rightarrow 2} (\sqrt{2x-1})$ | c) $\lim_{t \rightarrow 1} \left(\frac{3t}{t-1} \right)$ |
| d) $\lim_{x \rightarrow 2} (\sqrt{x} + \sqrt{x+7})$ | e) $\lim_{x \rightarrow -2} \left(\sqrt{\frac{4x-1}{x+1}} \right)$ | f) $\lim_{n \rightarrow -2} \left(\frac{3}{2-n} \right)^n$ |
| g) $\lim_{x \rightarrow 3} \left(\frac{x^2 - 9}{x - 3} \right)$ | h) $\lim_{t \rightarrow 3} \left(\frac{\sqrt{x+1} - 2}{x - 3} \right)$ | i) $\lim_{x \rightarrow -2} \left(\frac{x^3 + 8}{x + 2} \right)$ |
| j) $\lim_{m \rightarrow -2} \left(\frac{2m^2 + 3m - 2}{3m^2 - 12} \right)$ | k) $\lim_{x \rightarrow -3} \left(\frac{3 - \sqrt{12+x}}{x+3} \right)$ | l) $\lim_{x \rightarrow 2} \left(\frac{\sqrt{x+3} - \sqrt{7-x}}{x-2} \right)$ |

For the last three, use a change of variable to evaluate:

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| m) $\lim_{x \rightarrow 8} \left(\frac{x^{\frac{1}{3}} - 2}{x - 8} \right)$ | n) $\lim_{x \rightarrow 1} \left(\frac{1-x}{x^{\frac{1}{3}} - 1} \right)$ | o) $\lim_{x \rightarrow 0} \left(\frac{(x+1)^{\frac{1}{3}} - 1}{x} \right)$ |
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Answers to selected problems:

- b) $\sqrt{3}$ d) $\sqrt{5}$ f) $\frac{16}{9}$ h) $\frac{1}{4}$ i) 12 k) $-\frac{1}{6}$ m) $\frac{1}{12}$ o) $\frac{1}{3}$