b) $(x - y)(x + y)(x^4 + x^2y^2 + y^4)$

c) Both methods produce factors of (x - y) and (x + y); however, the other factors are different. Since the two factorizations must be equal to each other, this means that $(x^4 + x^2y^2 + y^4)$ must be equal to $(x^2 + xy + y^2)(x^2 - xy + y^2).$

Chapter Self-Test, p. 186

```
1. a) f(x) = a_n x^n + a_{n-1} x^{n-1} + \dots
         + a_1 x + a_0, where a_0, a_1, \ldots, a_n are
         real numbers and n is a whole number.
         The degree of the function is n; the
        leading coefficient is a_n.
```

b) *n* - 1

- **c**) *n*
- d) odd degree function e) even degree function with a negative leading coefficient
- **2.** y = (x + 4)(x + 2)(x 2)
- **3.** a) (x-9)(x+8)(2x-1)

b)
$$(3x - 4)(3x^2 + 9x + 79)$$

- 4. more zeros
- 5. -5 < x < -3; x > 1

7. a)
$$y = 5(2(x-2))^3 + 4$$

b) (2.5, 9)

8.
$$x + 5$$

9.
$$a = -2$$
; zeros at 0, -2, and 2.

Cumulative Review Chapters 1-3, pp. 188–191

1.	(b)	9.	(c)	17.	(a)	25.	(c
2.	(a)	10.	(d)	18.	(d)	26.	(c
3.	(c)	11.	(a)	19.	(b)	27.	(d
4.	(b)	12.	(a)	20.	(c)	28.	(b
5.	(b)	13.	(c)	21.	(b)	29.	(c
6.	(d)	14.	(d)	22.	(b)	30.	(c
7.	(d)	15.	(c)	23.	(b)	31.	(c
8.	(a)	16.	(c)	24.	(a)		
32.	a) 💦	1	y	$f(x) = x^2$			
		3-					
		2-	± 1				
			18	(x)=±√x	r		
		-1 0	I	2 3			
		-1-					
		1	,				

b) Answers may vary. For example, vertical translation up produces horizontal translation of the inverse to the right.



Vertical stretch produces horizontal stretch of inverse.



- c) Answers may vary. For example, if the vertex of the inverse is (a, b), restrict the value of *y* to either $y \ge b$ or $y \le b$.
- **33.** Answers may vary. For example, average rates of change vary between -2 and 4, depending on the interval; instantaneous rates of change are 9 at (0, 1), 0 at (1, 5), -3 at (2, 3), 0 at (3, 1), 9 at (4, 5); instantaneous rate of change is 0 at maximum (1, 5) and at minimum (3, 1).
- a) $f(x) = -2(x+1)^2(x-2)(x-4)$ 34. **b**) *p* = 32
 - c) As $x \to \pm \infty$, $f(x) \to -\infty$; zeros: -1, 2, and 4
 - **d**) -16



Chapter 4

Getting Started, pp. 194–195

1.	a) 3	c) 1
	b) 5	d) $\frac{64}{11}$
2.	a) $x(x + 6$	(x-5)

b) $(x-4)(x^2+4x+16)$ c) $3x(2x+3)(4x^2-6x+9)$ d) (x+3)(x-3)(2x+7)



- c) $-\frac{2}{3}$ and $\frac{5}{2}$ **5.** a) 3 and −3
- **d**) 0.3452 and -4.345 **b)** -10 and 2
- 6. a) (3, 7); Answers may vary. For example, the change in distance over time from t = 3 to t = 7 is greater than at other intervals of time.

b)
$$\frac{1}{3}$$
 m/s; $\frac{3}{4}$ m/s

- c) Answers may vary. For example, away; Erika's displacement, or distance from the sensor, is increasing.
- **7**. **a**) 2 s

4.

- **b)** 4.75 m/s
- c) -10.245 m/s
- 8. a) Disagree; You could use the quadratic formula to solve $y = x^3 + 4x^2 + 3x$ because it equals $x(x^2 + 4x + 3)$.
 - **b**) Disagree; $y = (x + 3)^2(x 2)$ is a cubic equation that will have two roots.

Answers

- c) Disagree; The equation $y = x^3$ will only pass through two quadrants.
- d) Agree; All polynomials are continuous and all polynomials have a y-intercept.
- e) Disagree; f(-3) = 9
- f) Agree; The instantaneous rates of change will tell you whether the graph is increasing, decreasing, or not changing at those points.

Lesson 4.1, pp. 204–206

1. a) 0, 1, -2, 2 d)
$$-6, \frac{5}{2}$$

b) $-\frac{3}{2}, \frac{5}{4}, -7$ e) 0, -3, 3
c) 3, -5, 4 f) -5, -2, 6

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- so somewhere in the middle it must cross the *x*-axis. This means its corresponding equation 0 = f(x) will have at least one real root.
 19. y = x⁵ + x + 1; By the factor theorem,
 - the only possible rational zeros are 1 and - 1. Neither works. Because the degree is odd, the polynomial has opposite end behaviour, and hence must have at least one zero, which must be irrational.

Lesson 4.2, pp. 213-215

1. a)
$$x \le 4$$
; $\{x \in \mathbb{R} \mid x \le 4\}$
b) $x < 7$; $\{x \in \mathbb{R} \mid x < 7\}$
c) $x < -5$; $\{x \in \mathbb{R} \mid x \ge -3\}$
e) $x > -10$; $\{x \in \mathbb{R} \mid x \ge -3\}$
e) $x > -10$; $\{x \in \mathbb{R} \mid x \ge -7\}$
2. a) $x \in [-3, \infty)$
b) $x \in (-\infty, -\frac{2}{3})$
c) $x \in [18, \infty)$
d) $x \in [1, \infty)$
e) $x \in (-\infty, 0)$
f) $x \in [-10, \infty)$
3. $-1 \le x < 6$
 $\overleftarrow{-3 - 2 - 1}$ 0 1 2 3 4 5 6 7
4. a) yes c) no e) yes
b) no d) no f) no
5. a) $x \le 7$ c) $x < -10$ e) $x < 6$
b) $x < 0$ d) $x \ge 5$ f) $x \ge \frac{7}{5}$
6. a) yes c) no e) yes
b) yes d) no f) no
7. a) $-6 < x < 2$
b) $4 < x < 8$
c) $-4 \le x \le 10$
d) $-7 \le x \le -4$
e) $7 < x < 9$
f) $-3 \le x \le -\frac{1}{2}$
8. a) Answers may vary. For example, $3x + 1 \ge 9 + x$
b) Answers may vary. For example, $3x + 1 \le 4 + x$
9. a) $\{x \in \mathbb{R} \mid -6 \le x \le 4\}$
b) $-13 \le 2x - 1 \le 7$
10. Attempting to solve $x - 3 < 3 - x < x - 5$ yields $3 > x > 4$, which has no solution. Solving $x - 3 < 3 - x < x - 5$ yields $3 < x < 4$.
11. a) $\frac{1}{2}x + 1 < 3$
b) $x < 4$
c) $\frac{1}{2}x + 1 < 3$
b) $x < 4$
c) $\frac{1}{2}x + 1 < 3$
b) $x < 4$
c) $\frac{1}{2}x + 1 < 3$
b) $x < 4$
c) $\frac{1}{2}x + 1 < 3$
b) $x < 4$
c) $\frac{1}{2}x + 1 < 3$
b) $x < 4$
f) $-3 \le 2 = F$
b) $C > -40$

15. a)
b)
$$-3 < x < 4$$

16. The solution will always have an upper
and lower bound due to the manner in
which the inequality is solved. The only
exception to this is when there is no
solution set.
17. a) Isolating *x* is very hard.
b) A graphical approach as described in
the lesson yields a solution of $x > 2.75$
(rounded to two places).
18. a) Maintained
b) Maintained if both positive; switched
if both negative; varies if one positive
and one negative.
c) Maintained
d) Switched
e) Switched unless one is positive and the
other is negative, in which case it is
maintained. (If either side is zero, it
become \leq and \geq , respectively.
g) Maintained, except that $<$ and $>$
become \leq and \geq , respectively.
g) Maintained, but it is undefined for
negative numbers.
19. a) { $x \in \mathbb{R} | -2 < x < 2$ }; (-2, 2)
 $\overleftarrow{-5 - 4 - 3 - 2 - 1 \ 0 \ 1 \ 2 \ 3 \ 4 \ 5}$
b) { $x \in \mathbb{R} | -3 \le x \ge 3$ }; (- ∞ , -3) or
(3, ∞)
 $\overleftarrow{-5 - 4 - 3 - 2 - 1 \ 0 \ 1 \ 2 \ 3 \ 4 \ 5}$
c) { $x \in \mathbb{R} | -5 < x < 3$ }; (- ∞ , 3)
 $\overleftarrow{-5 - 4 - 3 - 2 - 1 \ 0 \ 1 \ 2 \ 3 \ 4 \ 5}$
d) { $x \in \mathbb{R} | x \le 3$ }; (- ∞ , 3)
 $\overleftarrow{-5 - 4 - 3 - 2 - 1 \ 0 \ 1 \ 2 \ 3 \ 4 \ 5}$
Mid-Chapter Review, p. 218
1. a) $0, \frac{5}{2}, 4$ d) $-4, 6, 5, -5$
b) -2 e) $0, -2, -9$
c) 1, $-2, 5$ f) 3, $-3, 2, -2$
2. a) $h(t) = -5t^2 + 3t + 24.55$
b) 24.55 m
c) 2.5 s after jumping
d) $t > 2.5$ s Jude is below sea level (in the
water)

c) $(-\infty, -2), (0, 1)$ d) $(-\infty, 2), (2, \infty)$ 6. a) x < -1 or x > 1b) -3 < x < 4c) $x \le -\frac{1}{2}$ or $x \ge 5$ d) -7 < x < 0 or x > 2e) $-\frac{3}{2} < x < 3$ or x > 3f) $-4 \le x \le \frac{3}{2}$ Answers

7. a) $x \le -1$ or $x \ge 7$ **b**) 0 < x < 2 c) $x \le -3$ or $-2 \le x \le 1$ **d**) x < -2, -1 < x < 1 or x > 2e) $x \le -1$ or $0 \le x \le 3$ f) $-1 < x < -\frac{1}{2}$ or x > 28. (-1, 1) and $(2, \infty)$ **a)** $x^3 + 11x^2 + 18x = 0$ 9. **b)** Any values of *x* for which the graph of the corresponding function is above the x-axis ($\gamma = 0$) are solutions to the original inequality. c) -9 < x < -2 or x > 0**10.** $f(x) = -3(x+2)(x-1)(x-3)^2$ 11. a) **b)** 0 < v < 154.77 °C c) 133.78 °C to 139.56 °C **12.** a) 14 m c) 0.3 < t < 2.1**d**) 1.8 s **b**) 3.3 s **13.** V(x) = x(50 - 2x)(30 - 2x);5 < x < 7.19**14.** a) Since all the powers are even and the coefficients are positive, the polynomial on the left is always positive. b) Since all the powers are even and all the coefficients are negative (once all terms are brought to the left), the polynomial on the left is always negative. 15. You cannot divide by a variable expression because you do not know whether it is positive, negative, or zero. The correct solution is x < -1 or x > 4. 16. Answers may vary. For example:



- **17.** a) -4 < x < -3 or -2 < x < 3b) -1 < x < 0 or x > 5
- **18.** x < -1 or x > 2

Lesson 4.4, pp. 235-237

- a) positive on (0, 1), (4, 7), (10, 15.5), (19, 20); negative on (1, 4), (7, 10), (15.5, 19); zero at x = 1, 4, 7, 10, 15.5, and 19
- 640 Answers

- b) A positive slope means the cyclist's elevation is increasing, a negative slope means it is decreasing, and a zero slope means the cyclist's elevation is transitioning from increasing to decreasing or vice versa.
- **2.** a) i) 6 ii) 12 iii) 18
 - **b)** about 12
 - **c)** The graph is increasing on (2, 6).
- **d**) −6 **e**) about −6
- **3.** a) about 0
 - **b**) It indicates that x = 2 is a turning point in the graph.

	1	NY I	1	
	4-		+	
	2-		\square	
_		\sim		
-4	-2 0	2	4	
	-2			
	-4-			
		/		

- **4.** a) 3
 - **b**) Answers may vary. For example, x = 4.5, 3.

5. a) 3 c)
$$-\frac{1}{10}$$
 e) $\frac{2\delta}{3}$
b) 17 d) -7 f) 0

6. a) 3 c) about
$$-\frac{1}{2}$$
 e) about 5.5

b) about 14 **d**) about
$$-6$$
 f) 0
7.

Rate of change is positive on $\left(-\infty, \frac{1}{3}\right)$ and $(1, \infty)$, negative on $\left(\frac{1}{3}, 1\right)$, and zero

- at $x = \frac{1}{3}$ and 1.
- **8.** a) -55 m/s
- b) about -20 m/s9. a) about 2
 - **b**) -2
- c) y = 2x 4
- a) about 10 m/s
 b) about -50 m/s
- c) 0 m/s 11. a)

. a)	<u></u>	
	3-	
	2-	
	1.	
	0 2 4 6 8 10	
	• • • • • • • • • • • • • • • • • • •	

The rate is positive for $t \in (0, 4)$, negative for $t \in (4, 8)$, and zero at t = 0, 4 and 8.

- **b)** When the rate of change is zero, the boat stops.
- c) When the rate of change is negative, the boat is headed back to the dock.
- At (-3, 0), instantaneous rate = -96; at (1, 0), instantaneous rate = 0; at
 (2, 0)
 - (3, 0), instantaneous rate \doteq 24; at (-1, 0), instantaneous rate \doteq 24
- **13.** a) about 5 c) 2x + 3
- **b)** 2x + 3 + h **d)** 2(1) + 3 = 5
- **14.** When the instantaneous rate of change is zero, the function potentially has a local maximum or a local minimum. If the rate is positive to the left and negative to the right, it has a local maximum. If the rate is negative to the left and positive to the right, it has a local minimum.
- **15.** a) Rate of change and f(5) are both approximately 148.4.
 - b) Answers may vary. For example, the instantaneous rate of change at x = 1 is 2.7; at x = 3, it is 20.1; and at x = 4, it is 54.6.
 - c) The instantaneous rate of change of e^x for any value of x is e^x.
- **16.** a) about -1b) y = -x - 2

b)
$$y = -x -$$

c) $(-2, 0)$

$$\begin{array}{c} 3 \stackrel{y}{\xrightarrow{}} \\ 2 \stackrel{y}{\xrightarrow{}} \\ -3 \stackrel{z}{\xrightarrow{}} \begin{array}{c} 1 \\ 1 \\ -2 \\ -3 \end{array}$$

17. x = -0.53, 2.53

Chapter Review, pp. 240–241

1. a)
$$\pm 3$$
 c) 0, -2, 1
b) $\frac{1}{2}$, -2 d) ± 1 , 2

2. 0, 2,
$$\frac{2}{3}$$
, $\frac{4}{5}$

- **3.** a) f(x) = (x-1)(x-2)(x+1)(x+2)or $f(x) = x^4 - 5x^2 + 4$ b) 48, 3.10
- **4.** 2 cm by 2 cm or 7.4 cm by 7.4 cm
- a) The given information states that the model is valid between 1985 and 1995, so it can be used for 1993, but not 2005.
 - **b**) Set C(t) = 1500 (since the units are in thousands) and solve using a graphing calculator.
 - c) Sales reach 1.5 million in the 8th year after 1985, so in 1993.

6. a) Answers may vary. For example, 2x + 1 > 17**b)** Answers may vary. For example, $3x - 4 \ge -16$ c) Answers may vary. For example, $2x + 3 \le -21$ d) Answers may vary. For example, -19 < 2x - 1 < -3**7.** a) $x \in \left(\frac{25}{2}, \infty\right)$ **b**) $x \in \left[-\frac{23}{8}, \infty\right)$ c) $x \in (-\infty, 2)$ **d**) $x \in (-\infty, 3]$ 8. a) $\{x \in \mathbb{R} \mid -2 < x < 4\}$ **b**) $\{x \in \mathbf{R} \mid -1 \le x \le 0\}$ c) $\{x \in \mathbf{R} \mid -3 \le x \le 5\}$ d) $\{x \in \mathbf{R} \mid -6 < x < -2\}$ 9. a) The second plan is better if one calls more than 350 min per month. b) 44 40 36 32 28 24 100 200 300 400 500 **10.** a) -1 < x < 2**b**) $x \le -\frac{3}{2}$ or $x \ge 5$ c) $x < -\frac{3}{2}$ or 1 < x < 7**d**) $x \le -4$ or $1 \le x \le 5$ **11.** negative when $x \in (0, 5)$, positive when $x \in (-\infty, -2), (-2, 0), (5, \infty)$ **12.** $x \le -3.81$ 13. between January 1993 and March 1994 and between October 1995 and October 1996 **14.** a) average = 7, instantaneous $\doteq 8$ **b**) average = 13, instantaneous \doteq 15 c) average = 129, instantaneous \doteq 145 **d**) average = -464, instantaneous $\doteq -485$ **15.** positive when -1 < x < 1, negative when x < -1 or x > 1, and zero at x = -1, 1**16.** a) *t* ≐ 2.2 s **b)** -11 m/s c) about -22 m/s**17.** a) about 57.002 **b)** about 56.998 c) Both approximate the instantaneous rate of change at x = 3. **18.** a) male: 3.394x + 72.365;female: $g(x) = 0.0002x^3 - 0.026x^2 +$ 1.801x + 14.369b) More females than males will have lung cancer in 2006.

- c) The rate was changing faster for females, on average. Looking only at 1975 and 2000, the incidence among males increased only 5.5 per 100 000, while the incidence among females increased by 31.7.
- d) Between 1995 and 2000, the incidence among males decreased by 6.1 while the incidence among females increased by 5.6. Since 1998 is about halfway between 1995 and 2000, an estimate for the instantaneous rate of change in 1998 is the average rate of change from 1995 to 2000. The two rates of change are about the same in magnitude, but the rate for females is positive, while the rate for males is negative.

Chapter Self-Test, p. 242

- **1.** $1, \frac{3}{2}, -2$
- **2.** a) positive when x < -2 and 0 < x < 2, negative when -2 < x < 0 and x > 2, and zero at -2, 0, 2
 - **b**) positive when -1 < x < 1, negative when x < -1 or 1 < x, and zero at x = -1, 1**c**) −1
- **3.** a) Cost with card: 50 + 5n; Cost without card: 12n b) at least 8 pizzas

4. a)
$$x < \frac{1}{2}$$

b)
$$-2 \le x \le 1$$

c)
$$-2 < x < -1$$
 or $x > 5$
d) $x \ge -3$

d)
$$x \ge -$$

- 5. a) 15 m
 - **b**) 4.6 s
 - c) -3 m/s
- **6.** a) about 5 b) (1, 3) c) y = 5x 27. Since all the exponents are even and all the coefficients are positive, all values of the function are positive and greater than or equal to 4 for all real numbers x.
- 8. a) $\{x \in \mathbf{R} \mid -2 \le x \le 7\}$ **b**) -2 < x < 7
- **9.** 2 cm by 2 cm by 15 cm

Chapter 5

Getting Started, pp. 246-247

1. a) (x-5)(x+2)**b**) 3(x+5)(x-1)c) (4x - 7)(4x + 7)d) (3x-2)(3x-2)e) (a-3)(3a+10)f) (2x + 3y)(3x - 7y)**2.** a) 3 - 2s **b**) $\frac{n^3}{3m}, m, n \neq 0$

$$5x - 2 = 5$$

e) $-\frac{x+6}{3+x}, x \neq -3, 3$
f) $\frac{a-b}{a-3b}, a \neq -5b, \frac{3b}{2}$
a) $\frac{7}{15}$
b) $\frac{6}{x}, x \neq 0$
c) $\frac{-4x^2 + 20x - 6}{x-3}, x \neq -2, 3$
d) $\frac{x^3 + 2x - 8x}{x^2 - 1}, x \neq -1, 0, 1, 3$
a) $1\frac{11}{21}$
b) $\frac{19x}{12}$

c) $3x^2 - 4x - 1, x \neq 0$

d) $\frac{1}{x}$, $x \neq \frac{2}{x}$

3.

4.

c)
$$\frac{4+x}{x^2}, x \neq 0$$

d) $\frac{3x-6}{x^2-3x}, x \neq 0, 3$
e) $\frac{2x+10+y}{x^2-25}, x \neq 5, -5$
f) $\frac{-2a+50}{(a+3)(a-5)(a+3)}, x \neq -3, 4, 5$

5. a)
$$x = 6$$

b) $x = 2$
c) $x = 3$
d) $x = \frac{-12}{2}$

vertical: x = 0; horizontal: y = 0; $\mathbf{D} = \{ x \in \mathbf{R} | x \neq 0 \};$ $\mathbf{R} = \{ y \in \mathbf{R} | y \neq 0 \}$







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