value of *x*. Determine the average rate of change for these values of *x* and *y*. When the average rate of change has stabilized to a constant value, this is the instantaneous rate of change.

a) and b) Only *a* and *k* affect the instantaneous rate of change. Increases in the absolute value of either parameter tend to increase the instantaneous rate of change.

Chapter Review, pp. 510-511

- **1.** a) $y = \log_4 x$ c) $y = \log_{\frac{3}{4}} x$
 - **b**) $y = \log_a x$ **d**) $m = \log_p q$
- **2. a)** vertical stretch by a factor of 3, reflection in the *x*-axis, horizontal compression by a factor of $\frac{1}{2}$
 - **b)** horizontal translation 5 units to the right, vertical translation 2 units up
 - c) vertical compression by a factor of $\frac{1}{2}$,
 - horizontal compression by a factor of $\frac{1}{5}$ d) horizontal stretch by a factor of 3, reflection in the *y*-axis, vertical shift 3 units down

3. a) $y = \frac{2}{5} \log x - 3$ b) $y = -\log \left[\frac{1}{2}(x - 3)\right]$

c)
$$y = 5 \log(-2x)$$

d) y = log (-x - 4) - 2
4. Compared to y = log x, y = 3 log (x - 1) + 2 is vertically stretched by a factor of 3, horizontally translated 1 unit to the right, and vertically translated 2 units up.
5. a) 3 c) 0

		-)	
	b) −2	d)	-4
6.	a) 3.615	c)	2.829
	b) -1.661	d)	2.690
7.	a) log 55	c)	log ₅ 4
	b) log 5	d)	log 128
8.	a) 1	c)	$\frac{2}{3}$
	b) 2	d)	3
9.	It is shifted 4	units up.	
10.	a) 5	c)	-2
	b) 3.75	d)	-0.2
11.	a) 2.432	c)	2.553
	b) 3.237	d)	4.799
12.	a) 0.79; 0.5		
	b) -0.43		
13.	5.45 days		
14.	a) 63	c)	9
	b) $\frac{10\ 000}{3}$	d)	1.5
15.	a) 1	c)	3
	b) 5	d)	$\pm \sqrt{10\ 001}$
16.	$10^{-2} W/m^2$		
17.	$10^{-3.8} \text{W/m}^2$		

19. 3.9 times
20.
$$\frac{10^{4.7}}{10^{2.3}} = 251.2$$

 $\frac{10^{12.5}}{10^{10.1}} = 251.2$

The relative change in each case is the same. Each change produces a solution with concentration 251.2 times the orignial solution.

- **21.** Yes; $y = 3(2.25^x)$
- **22.** 17.8 years
- a) 8671 people per year
 b) 7114; The rate of growth for the first 30 years is slower than the rate of growth for the entire period.
 - c) $y = 134322(1.03^{x})$, where x is the number of years after 1950
 - d) i) 7171 people per year
 ii) 12 950 people per year
- **24.** a) exponential; $y = 23(1.17^x)$, where x is the number of years since 1998 b) 221 909
 - **b)** 331 808
 - c) Answers may vary. For example, I assumed that the rate of growth would be the same through 2015. This is not reasonable. As more people buy the players, there will be fewer people remaining to buy them, or newer technology may replace them.
 - d) about 5300 DVD players per year
 - e) about 4950 DVD players per year
 - f) Answers may vary. For example, the prediction in part e) makes sense because the prediction is for a year covered by the data given. The prediction made in part b) does not make sense because the prediction is for a year that is beyond the data given, and conditions may change, making the model invalid.

Chapter Self-Test, p. 512

1. a) $x = 4^{y}; \log_4 x = y$

b) $y = 6^x; \log_6 y = x$

- a) horizontal compression by a factor of ¹/₂, horizontal translation 4 units to the right, vertical translation 3 units up
 - b) vertical compression by a factor of ¹/₂, reflection in the *x*-axis, horizontal translation 5 units to the left, vertical translation 1 unit down

b) 5

b) 7

b) 1²/₋

- **3.** a) −2 **4.** a) 2
- **5.** $\log_4 xy$
- **6.** 7.85
- **7.** a) 2
- **8. a)** 50 g
- **b**) $A(t) = 100(0.5)^{\frac{t}{5730}}$
- **c)** 1844 years
- **d**) -0.015 g/year
- **9. a**) 6 min **b**) 97°

Chapter 9

Getting Started, p. 516

- **1.** a) f(-1) = 30, f(4) = 0**b**) f(-1) = -2, $f(4) = -5\frac{1}{3}$ c) f(-1) is undefined, $f(4) \doteq 1.81$ **d**) f(-1) = -20, f(4) = -0.625**2.** D = { $x \in \mathbf{R} | x \neq 1$ } $\mathbf{R} = \{ \mathbf{y} \in \mathbf{R} | \mathbf{y} \neq 2 \}$ There is no minimum or maximum value; the function is never increasing; the function is decreasing from $(-\infty, 1)$ and $(1, \infty)$; the function approaches $-\infty$ as *x* approaches 1 from the left and ∞ as x approaches 1 from the right; vertical asymptote is x = 1; horizontal asymptote is y = 2**3.** a) y = 2|x - 3|**b**) $y = -\cos(2x)$ c) $y = \log_3(-x - 4) - 1$ **d**) $y = -\frac{4}{x} - 5$ **4. a**) $x = -1, \frac{1}{2}, \text{ and } 4$ **b**) $x = -\frac{5}{3}$ or x = 3c) x = 5 or x = -2Cannot take the log of a negative number, so x = 5. **d**) $x = -\frac{3}{4}$ **e**) x = -3**f**) sin $x = \frac{3}{2}$ or sin x = -1. Since sin x cannot be greater than 1, the first equation does not give a solution; $x = 270^{\circ}$ **5.** a) $(-\infty, -4) \cup (2, 3)$ **b**) $\left(-2,\frac{3}{2}\right) \cup [4,\infty)$
- **6.** a) odd c) even**b**) neither**d**) neither
- Polynomial, logarithmic, and exponential functions are continuous. Rational and trigonometric functions are sometimes continuous and sometimes not.

Lesson 9.1, p. 520

1. Answers may vary. For example, the graph of $y = \left(\left(\frac{1}{2}\right)^{x}\right)(2x)$ is



18. 5 times

2. a) Answers may vary. For example, $y = (2^x)(2x);$



b) Answers may vary. For example, $y = (2x)(\cos(2\pi x));$



c) Answers may vary. For example, $y = (2x)(\sin(2\pi x));$



d) Answers may vary. For example, $y = (\sin 2\pi x) (\cos 2\pi x);$



e) Answers may vary. For example, $\gamma = \left(\frac{1}{2}\right)^x (\cos 2\pi x),$

where
$$0 \le x \le 2\pi$$
;



f) Answers may vary. For example, $y = 2x \sin 2\pi x$, where $0 \le x \le 2\pi$;



3. Answers will vary. For example, $y = x^2$



Lesson 9.2, pp. 528-530

- **1.** a) $\{(-4, 6), (-2, 5), (1, 5), (4, 10)\}$ b) $\{(-4, 6), (-2, 5), (1, 5), (4, 10)\}$
 - c) $\{(-4, 2), (-2, 3), (1, 1), (4, 2)\}$
 - d) $\{(-4, -2), (-2, -3), (1, -1), (4, -2)\}$
 - e) $\{(-4, 8), (-2, 8), (1, 6), (3, 10), (4, 12)\}$
 - f) $\{(-4,0), (-2,0), (0,0), (1,0), (2,0), (4,0)\}$
- **2.** a) 10
 - b) 2; (f + g) (x) is undefined at x = 2 because g(x) is undefined at x = 2.
 c) {x ∈ R | x ≠ 2}
- **3.** $\{x \in \mathbf{R} \mid -1 \le x < 1\}$
- **4.** Graph of f + g:







relative maximum at x = 0 and relative minimums at x = -0.4882 and x = 0.4882period: N/A The domain is all real numbers. The range is all real numbers greater than -0.1308. $f(x) - g(x) = \cos(2\pi x) - x^4$ The function is symmetric across the line x = 0. The function is increasing from $-\infty$ to -0.9180 and -0.5138 to 0 and 0.5138 to 0.9180; decreasing from -0.9180 to -0.5138 and 0 to 0.5138 and 0.9180 to ∞ . zeros at x = -1, -0.8278, -0.2494,0.2494, 0.8278, 1 relative maxima at -0.9180, 0, and0.9180; relative minima at -0.5138 and 0.5138 period: N/A The domain is all real numbers. The range is all real numbers less than 1. c) $f(x) + g(x) = \log(x) + 2x$ The function is not symmetric. The function is increasing from 0 to ∞ . no zeros no maximum or minimum period: N/A The domain is all real numbers greater than 0. The range is all real numbers. $f(x) - g(x) = \log(x) - 2x$ The function is not symmetric. The function is increasing from 0 to approximately 0.2 and decreasing from approximately 0.2 to ∞ . no zeros maximum at $x \doteq 0.2$ period: N/A The domain is all real numbers greater than 0. The range is all real numbers less than or equal to approximately -1.1.**d**) $f(x) + g(x) = \sin(2\pi x) + 2\sin(\pi x)$ The function is symmetric about the origin. The function is increasing from -0.33 + 2k to 0.33 + 2k and decreasing from 0.33 + 2k to 1.67 + 2k. zero at k minimum at x = -0.33 + 2kmaximum at x = 0.33 + 2kperiod: 2 The domain is all real numbers. The range is all real numbers between -2.598 and 2.598. $f(x) - g(x) = \sin(2\pi x) - 2\sin(\pi x)$ The function is symmetric about the origin, increasing from 0.67 + 2k to 1.33 + 2k and decreasing from

-0.67 + 2k to 0.67 + 2kzero at k minimum at 0.67 + 2k and maximum at 1.33 + 2kperiod: 2 The domain is all real numbers. The range is all real numbers between -2.598 to 2.598. e) $f(x) + g(x) = \sin(2\pi x) + \frac{1}{2}$ The function is not symmetric. The function is increasing and decreasing at irregular intervals. The zeros are changing at irregular intervals. The maximums and minimums are changing at irregular intervals. period: N/A The domain is all real numbers except 0. The range is all real numbers. $f(x) - g(x) = \sin(2\pi x) - \frac{1}{2}$ The function is not symmetric.^x The function is increasing and decreasing at irregular intervals. The zeros are changing at irregular intervals. The maximums and minimums are changing at irregular intervals. period: N/A The domain is all real numbers except 0. The range is all real numbers. **f**) $f(x) + g(x) = \sqrt{x-2} + \frac{1}{x-2}$ The function is not symmetric. The function is increasing from 3.5874 to ∞ and decreasing from 2 to 3.5874. zeros: none minimum at x = 3.5874period: N/A The domain is all real numbers greater than 2. The range is all real numbers greater than 1.8899. $f(x) - g(x) = \sqrt{x - 2} - \frac{1}{x - 2}$ The function is not symmetric. The function is increasing from 2 to ∞ . zero at x = 3no maximum or minimum period: N/A The domain is all real numbers greater than 2. The range is all real numbers. **10.** a) The sum of two even functions will be even because replacing x with -x will still result in the original function. **b**) The sum of two odd functions will be

> c) The sum of an even and an odd function will result in neither an even nor an odd function because replacing *x* with -*x* will not result in the same function or in the opposite of the function.

odd because replacing x with -x will

function.

still result in the opposite of the original

11. a) $R(t) = 5000 - 25t - 1000 \cos\left(\frac{\pi}{6}t\right);$

it is neither odd nor even; it is increasing during the first 6 months of each year and decreasing during the last 6 months of each year; it has one zero, which is the point at which the deer population has become extinct; it has a maximum value of 3850 and a minimum value of 0, so its range is $\{R(t) \in \mathbf{R} | 0 \le R(t) \le 3850\}.$

b) after about 167 months, or 13 years and 11 months

- **12.** The stopping distance can be defined by the function $s(x) = 0.006x^2 + 0.21x$. If the vehicle is travelling at 90 km/h, the stopping distance is 67.5 m.
- **13.** $f(x) = \sin(\pi x); g(x) = \cos(\pi x)$
- **14.** The function is neither even nor odd; it is not symmetrical with respect to the *y*-axis or with respect to the origin; it extends from the third quadrant to the first quadrant; it has a turning point between -n and 0 and another turning point at 0; it has zeros at -n and 0; it has no maximum or minimum values; it is increasing when $x \in (-\infty, -n)$ and when $x \in (0, \infty)$; when $x \in (-n, 0)$, it increases, has a turning point, and then decreases; its domain is $\{x \in \mathbf{R}\}$, and its range is $\{y \in \mathbf{R}\}$.

15. a)
$$f(x) = 0; g(x) = 0$$

b) $f(x) = x^2; g(x) = x^2$
c) $f(x) = \frac{1}{x-2}; g(x) = \frac{1}{x-2} + 2.$

16. m = 2, n = 3

Lesson 9.3, pp. 537–539





Answers





6. 4(a): The function is symmetric about the line x = 0. The function is increasing from 0 to ∞ . The function is decreasing from $-\infty$ to 0. zeros at x = -7, 7The minimum is at x = 0. period: N/A 4(b): The function is not symmetric. The function is increasing from -10 to ∞ . zero at x = -10The minimum is at x = -10. period: N/A 4(c): The function is not symmetric. The function is increasing from $-\infty$ to 0 and from 6 to ∞ . zeros at x = 0, 9The relative minimum is at x = -6. The relative maximum is at x = 0. period: N/A 4(d): The function is symmetric about the line x = -1.75. The function is increasing from $-\infty$ to - 1.75 and is decreasing from - 1.75 to $\infty.$ zero at x = -1.75The maximum is at x = -1.75. period: N/A 4(e): The function is not symmetric. The function is increasing from $-\infty$ to 0 and from 6 to ∞ . zeros at x = 0, 9The relative minima are at x = -4.5336and 4.4286. The relative maximum is at x = -1.1323.period: N/A 4(f): The function is not symmetric. The function is increasing from -4 to ∞ . zeros: none maximum/minimum: none period: N/A 7. 8. a) $\left\{ x \in \mathbf{R} \mid x \neq -2, 7, \frac{\pi}{2}, \text{ or } \frac{3\pi}{2} \right\}$ **b**) $\{x \in \mathbf{R} \mid x > 8\}$ c) $\{x \in \mathbf{R} | x \ge -81 \text{ and } x \ne 0, \pi, \text{ or } 2\pi \}$ **d**) $\{x \in \mathbf{R} | x \leq -1 \text{ or } x \geq 1,$ and $x \neq -3$ **9.** $(f \times p)(t)$ represents the total energy consumption in a particular country at time t **10.** a) $R(x) = (20\ 000 - 750x)(25 + x)$ or

 $R(x) = 500\ 000 + 1250x - 750x^2,$ where x is the increase in the admission fee in dollars

- **b**) Yes, it's the product of the function $P(x) = 20\ 000 - 750x$, which represents the number of daily visitors, and F(x) = 25 + x, which represents the admission fee. **c**) \$25.83
- **11.** $m(t) = ((0.9)^t)(650 + 300t)$ The amount of contaminated material is at its greatest after about 7.3 s.
- **12.** The statement is false. If f(x) and g(x) are odd functions, then their product will always be an even function. When you multiply a function that has an odd degree with another function that has an odd degree, you add the exponents, and when you add two odd numbers together, you get an even number.
- **13.** $f(x) = 3x^2 + 2x + 5$ and $g(x) = 2x^2 4x 2$
- **14.** a) $(f \times g)(x) = \sqrt{-x} \log (x + 10)$ The domain is $\{x \in \mathbf{R} | -10 < x \le 0\}$.
 - **b**) One strategy is to create a table of values for f(x) and g(x) and to multiply the corresponding *y*-values together. The resulting values could then be graphed. Another strategy is to graph f(x) and g(x) and to then create a graph for $(f \times g)(x)$ based on these two graphs. The first strategy is probably better than the second strategy, since the *y*-values for f(x) and g(x) will not be easily discernable from the graphs of f(x) and g(x).



-6

- c) The range will always be 1. If *f* is of odd degree, there will always be at least one value that makes the product undefined and which is excluded from the domain. If *f* is of even degree, there may be no values that are excluded from the domain.
- 16. a) $f(x) = 2^{x}$ $g(x) = x^{2} + 1$ $(f \times g)(x) = 2^{x}(x^{2} + 1)$ b) f(x) = x $g(x) = \sin(2\pi x)$ $(f \times g)(x) = x \sin(2\pi x)$ 17. a) f(x) = (2x + 9) g(x) = (2x - 9)b) $f(x) = (2 \sin x + 3)$ $g(x) = (4 \sin^{2} x - 6 \sin x + 9)$ c) $f(x) = x^{\frac{1}{2}}$ $g(x) = (4x^{5} - 3x^{3} + 1)$ d) $f(x) = \frac{1}{2x + 1}$ g(x) = 6x - 5

Lesson 9.4, p. 542

1. a)
$$(f \div g)(x) = \frac{5}{x}, x \neq 0$$

b) $(f \div g)(x) = \frac{4x}{2x - 1}, x \neq \frac{1}{2}$
c) $(f \div g)(x) = \frac{4x}{x^2 + 4}$
d) $(f \div g)(x) = \frac{(x + 2)(\sqrt{x - 2})}{x - 2}, x > 2$
e) $(f \div g)(x) = \frac{8}{1 + (\frac{1}{2})^x}$
f) $(f \div g)(x) = \frac{x^2}{\log(x)}, x > 0$

2. a) 1(a):





1(f): domain of $f: \{x \in \mathbf{R}\};$ domain of $g: \{x \in \mathbf{R} | x > 0\}$

Answers 677





Mid-Chapter Review, p. 544

- 1. multiplication
- a) $\{(-9, 2), (-6, -9), (0, 14)\}$ 2. **b**) $\{(-9, 2), (-6, -9), (0, 14)\}$ c) $\{(-9, -6), (-6, 3), (0, -10)\}$

d) {(-9, 6), (-6, -3), (0, 10)}
a)
$$P(x) = -5x^2 + 140x - 30$$

3. a)
$$P(x) = -5x^2 + 140x - b$$



b)
$$N(h) = 24.97h$$

c) $W(h) = 24.78h$

4.

d)
$$S(h) = 25.36h$$

e) \$317
5. a) $(f \times g)(x) = x^2 + x + \frac{1}{2}$

$$D = \{x \in \mathbf{R}\}$$

b) $(f \times g)(x) = \sin(3x)(\sqrt{x-10})$
$$D = \{x \in \mathbf{R} | x \ge 10\}$$

c)
$$(f \times g)(x) = \frac{22x^3}{x+5}$$

 $D = \{x \in \mathbb{R} | x \neq -5\}$
d) $(f \times g)(x) = 8100x^2 - 1$
 $D = \{x \in \mathbb{R}\}$
6. a) $\mathbb{R}(h) = 90 \cos\left(\frac{\pi}{6}h\right) \sin\left(\frac{\pi}{6}h\right)$
 $-102 \sin\left(\frac{\pi}{6}h\right) - 210 \cos\left(\frac{\pi}{6}h\right) + 238$
b) Average Revenue
 $\int_{100}^{10} \int_{10}^{10} \int_{1$

Lesson 9.5, pp. 552-554

1. a) −1 **b)** −24 **c**) −129 7 d) 16 **e**) 1 **f**) −8 **2.** a) 3 **b**) 5 **c)** 10 **d**) $(f \circ g)(0)$ is undefined. **e)** 2 **f**) 4 **3.** a) 5 **b**) 5 **c)** 4 d) $(f \circ f)(2)$ is undefined. **4.** a) C(d(5)) = 36It costs \$36 to travel for 5 h. **b**) C(d(t)) represents the relationship between the time driven and the cost of gasoline.

678 Answers







Answers

Answers 679

 $\mathbf{R} = \{ y \in \mathbf{R} \mid y \ge 1 \}$

c)
$$f \circ g = \sqrt{4 - x^4}$$

 $D = \{x \in \mathbf{R} | -\sqrt{2} \le x \le \sqrt{2}\}$
 $R = \{y \in \mathbf{R} | y \ge 0\}$
 $g \circ f = 4 - x^2$
 $D = \{x \in \mathbf{R} | -2 \le x \le 2\}$
 $R = \{y \in \mathbf{R} | 0 < y < 2\}$
d) $f \circ g = 2\sqrt{x - 1}$
 $D = \{x \in \mathbf{R} | x \ge 1\}$
 $R = \{y \in \mathbf{R} | y \ge 1\}$
 $g \circ f = \sqrt{2^x - 1}$
 $D = \{x \in \mathbf{R} | x \ge 0\}$
 $R = \{y \in \mathbf{R} | y \ge 0\}$
e) $f \circ g = x$
 $D = \{x \in \mathbf{R} | x \ge 0\}$
 $R = \{y \in \mathbf{R} | y \ge 0\}$
e) $f \circ g = x$
 $D = \{x \in \mathbf{R} | x > 0\}$
 $R = \{y \in \mathbf{R}\}$
 $g \circ f = x$
 $D = \{x \in \mathbf{R}\}$
 $R = \{y \in \mathbf{R}\}$
 $R = \{y \in \mathbf{R} | -1 \le y \le 1\}$
 $g \circ f = 5^{2 \sin x} + 1$
 $D = \{x \in \mathbf{R}\}$
 $R = \{y \in \mathbf{R} | -1 \le y \le 1\}$
 $R = \{y \in \mathbf{R} | \frac{26}{25} \le y \le 26\}$
7. a) Answers may vary. For example,
 $f(x) = \sqrt{x}$ and $g(x) = x^2 + 6$
b) Answers may vary. For example,
 $f(x) = x^6$ and $g(x) = 5x - 8$
c) Answers may vary. For example,
 $f(x) = 2^x$ and $g(x) = 6x + 7$

d) Answers may vary. For example, f(x) = ¹/_x and g(x) = x³ - 7x + 2
e) Answers may vary. For example, f(x) = sin²x and g(x) = 10x + 5
f) Answers may vary. For example,

$$f(x) = \sqrt[3]{x}$$
 and $g(x) = (x + 4)^2$
a) $(f \circ g)(x) = 2x^2 - 1$

8.



c) It is compressed by a factor of 2 and translated down 1 unit.

9. a) f(g(x)) = 6x + 3 The slope of g(x) has been multiplied by 2, and the *y*-intercept of g(x) has been vertically translated 1 unit up.
b) g(f(x)) = 6x - 1

The slope of f(x) has been multiplied by 3.

10.
$$D(p) = 780 + 31.96p$$

11. $f(g(x)) = 0.06x$
12. a) $d(s) = \sqrt{16 + s^2}$; $s(t) = 560t$
b) $d(s(t)) = \sqrt{16 + 313600t^2}$, where *t* is the time in hours and $d(s(t))$ is the distance in kilometres
13. $c(v(t)) = \left(\frac{40 + 3t + t^2}{500} - 0.1\right)^2 + 0.15$; The car is running most economically 2 h into the trip.
14. Graph A(k); $f(x)$ is vertically compressed by a factor of 0.5 and reflected in the *x*-axis. Graph B(b); $f(x)$ is translated 3 units to the left. Graph C(d); $f(x)$ is translated 4 units down. Graph E(g); $f(x)$ is translated 4 units down. Graph F(c); $f(x)$ is reflected in the *y*-axis.
15. Sum: $y = f + g$
 $f(x) = \frac{4}{x-3}$; $g(x) = 1$
Product: $y = f \times g$
 $f(x) = x - 3$; $g(x) = \frac{x+1}{(x-3)^2}$
Quotient: $y = f \div g$

Quotient:
$$y = f \div g$$

 $f(x) = 1 + x; g(x) = x - 3$
Composition: $y = f \circ g$
 $f(x) = \frac{4}{x} + 1; g(x) = x - 3$
5. a) $f(k) = 27k - 14$

16. a)
$$f(k) = 27k - 14$$

b) $f(k) = 2\sqrt{9k - 16} - 5$

Lesson 9.6, pp. 560-562

1. a) i)
$$x = \frac{1}{2}$$
, 2, or $\frac{7}{2}$
ii) $x = -1$ or 2
b) i) $\frac{1}{2} < x < 2$ or $x > \frac{7}{2}$
ii) $-1 < x < 2$
c) i) $x \le \frac{1}{2}$; $2 \le x \le \frac{7}{2}$
ii) $x \le -1$ or $x \ge 2$
d) i) $\frac{1}{2} \le x \le 2$ or $x \ge \frac{7}{2}$
ii) $-1 \le x \le 2$
2. a) $x = 0.8$
b) $x = 0$ and 3.5
c) $x = -2.4$
d) $x = 0.7$

4.
$$f(x) < g(x): 1.3 < x < 1.6$$

 $f(x) = g(x): x = 0 \text{ or } 1.3$
 $f(x) = g(x): x = 0 \text{ or } 1.3$
 $f(x) > g(x): 0 < x < 1.3 \text{ or } 1.6 < x < 3$

5. a)
$$x \doteq 2.5$$
 d) $x \doteq -2.1$
b) $x \doteq 2.2$ e) $x = 10$
c) $x \doteq 1.8$ f) $x = 1 \text{ or } 3$
6. a) $x = -1.81 \text{ or } 0.48$
b) $x = -1.38 \text{ or } 1.6$
c) $x = -1.38 \text{ or } 1.30$

- **d**) x = -0.8, 0, or 0.8
- e) x = 0.21 or 0.74
- f) x = 0, 0.18, 0.38, or 1
 7. (0.7, -1.5)
- **8.** They will be about the same in 2012.
- **9.** a) $x \in (-0.57, 1)$ b) $x \in [0, 0.58]$
 - c) $x \in (-\infty, 0)$ d) $x \in (0.17, 0.83)$
 - e) $x \in (0.35, 1.51)$
 - **f**) $x \in (0.1, 0.5)$
- **10.** Answers may vary. For example, $f(x) = x^3 + 5x^2 + 2x - 8$ and g(x) = 0.
- 11. Answers may vary. For example, $f(x) = -x^2 + 25 \text{ and } g(x) = -x + 5.$
- **12.** $a \doteq 7, b \doteq 2$ **13.** Answers may vary. For example:

Perform the necessary algebraic operations to move all of the terms on the right side of the equation to the left side of the equation. Construct the function f(x), such that f(x) equals the left side of the equation.



Determine the *x*-intercepts of the graph that fall within the interval provided, if applicable.

The *x*-intercepts of the graph are the solutions to the equation.

- **14.** $x = 0 \pm 2n, x = -0.67 \pm 2n$ or $x = 0.62 \pm 2n$, where $n \in I$
- **15.** $x \in (2n, 2n + 1)$, where $n \in I$

Lesson 9.7, pp. 569–574







5.

- e) It is the maximum of the function.
- f) From the graph, the rate of change appears to be greatest at t = 0 s.



 $P(t) = 1.4t^2 + 3230$, while an

 $P(t) = 3230(1.016)^{t}$. While neither model is perfect, it appears that the polynomial model fits the data better.

Answers

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exponential model is

8.

b) $P(155) = 1.4(155)^2 + 3230$ $= 36\,865$

$$P(155) = 3230(1.016)^{155} \doteq 37\ 820$$

- c) A case could be made for either model. The polynomial model appears to fit the data better, but population growth is usually exponential.
- d) According to the polynomial model, in 2000, the population was increasing at a rate of about 389 000 per year, while according to the exponential model, in 2000, the population was increasing at a rate of about 465 000 per year.

11. a) $P(t) = 3339.18(1.13225)^{t}$ **b**) They were introduced around the year 1924.

- c) rate of growth $\doteq 2641$ rabbits per year
- **d)** $P(65) \doteq 10\ 712\ 509.96$
- **12.** a) $V(t) = 155.6 \sin \left(120\pi t + \frac{\pi}{2} \right)$
 - **b**) $V(t) = 155.6 \cos(120\pi t)$ c) The cosine function was easier to determine. The cosine function is at its maximum when the argument is 0, so no horizontal translation was necessary.

13. a) Answers will vary. For example, a linear model is P(t) = -9t + 400, a quadratic model is $P(t) = \frac{23}{90} (t - 30)^2$ + 170, and an exponential model is $P(t) = 400(0.972)^{t}$.

> The exponential model fits the data far better than the other two models.

b)
$$P(t) = -9t + 400$$

 $P(60) = -140 \text{ kPa}$
 $P(t) = \frac{23}{90}(t - 30)^2 + 170,$
 $P(60) = 400 \text{ kPa}$

- $P(t) = 400(0.972)^{t}, P(60) \doteq 73 \text{ kPa}$ c) The exponential model gives the most realistic answer, because it fits the data the best. Also, the pressure must be less than 170 kPa, but it cannot be negative.
- **14.** As a population procreates, the population becomes larger, and thus, more and more organisms exist that can procreate some more. In other words, the act of procreating enables even more procreating in the future.
- 15. a) linear, quadratic, or exponential **b**) linear or quadratic c) exponential

16. a)
$$T(n) = \frac{1}{6}n^3 + \frac{1}{2}n^2 + \frac{1}{3}n$$

b) 47 850 $= \frac{1}{6}n^3 + \frac{1}{2}n^2 + \frac{1}{3}n$

So, $n \doteq 64.975$. So, it is not a tetrahedral number because *n* must be an integer.

17. a) $P(t) = 30.75(1.008 418)^{t}$ **b**) In 2000, the growth rate of Canada was less than the growth rate of Ontario and Alberta.

Chapter Review, pp. 576–577

- **1.** division
- **2. a)** Shop 2 **b)** $S_{1+2} = t^3 + 1.6t^2 + 1200$

 - **c)** 1 473 600
 - d) The owner should close the first shop, because the sales are decreasing and will eventually reach zero.
- **3.** a) $C(x) = 9.45x + 52\,000$
 - **b**) I(x) = 15.8x
- c) $P(x) = 6.35x 52\,000$ 4.
- **a)** 12 sin (7x)**b)** $9x^2$
- c) $121x^2 49$
- **d**) $2a^2b^{3x}$
- a) $C \times A = 42\,750\,000\,000(1.01)^t$ 5. $+ 3\,000\,000\,000t(1.01)^{t}$ b)
 - Taxes Collected 400 320 Taxes (\$billion) 240 160 80 0 10 20 30 40 50 Years from now

d) about \$156 402 200 032.31

6. a)
$$\frac{21}{x}$$

b) $\frac{1}{2x+9}$
c) $\frac{\sqrt{x+15}}{x+15}$
d) $\frac{x^3}{2\log x}$
7. a) $\{x \in \mathbb{R} | x \neq 0\}$

b)
$$\left\{ x \in \mathbf{R} \mid x \neq 4, x \neq -\frac{9}{2} \right\}$$

c)
$$\{x \in \mathbf{R} \mid x > -15\}$$

$$\mathbf{d} \quad \{x \in \mathbf{R} \mid x > 0\}$$

8. a) Domain of $f(x): \{x \in \mathbb{R} | x > -1\}$ Range of f(x): { $y \in \mathbf{R} | y > 0$ } Domain of g(x): { $x \in \mathbf{R}$ } Range of g(x): { $y \in \mathbf{R} | y \ge 3$ } **b**) $f(g(x)) = \frac{1}{\sqrt{x^2 + 4}}$ c) $g(f(x)) = \frac{3x+4}{x+1}$ **d**) $f(g(0)) = \frac{1}{2}$ e) g(f(0)) = 4

f) For
$$f(g(x))$$
: $\{x \in \mathbf{R}\}$
For $g(f(x))$: $\{x \in \mathbf{R} | x > -1\}$

9. a)
$$x - 6$$

b) $x - 9$

c)
$$x - 12$$

d) $x - 3(1 + n)$
10. a) $A(r) = \pi r^2$
b) $r(C) = \frac{C}{2\pi}$

c)
$$A(r(C)) = \frac{C^2}{4\pi}$$

d)
$$\frac{C^2}{L} \doteq 1.03 \text{ m}$$

- 4π **11.** f(x) < g(x): -1.2 < x < 0 or x > 1.2f(x) = g(x): x = -1.2, 0, or 1.2
- f(x) > g(x): x < -1.2 or 0 < x < 1.2**12.** a) $x \doteq 4.0$
 - **b**) *x* ≐ 2.0
 - c) $x \doteq -0.8$
 - **d)** $x \doteq 0.7$
- **13.** a) P(t) = 600t 1000. The slope is the rate that the population is changing.
 - **b)** $P(t) = 617.6(1.26)^t$, 617.6 is the initial population and 1.26 represents the growth.

14.
$$P(t) = 2570.99(1.018)^{t}$$



When t = 13, P(t) = 3242. When t = 23, P(t) = 3875. When t = 90, P(t) = 12806.

Chapter Self-Test, p. 578

1. a) $A(r) = 4\pi r^2$ **b**) $r(V) = \sqrt[3]{\frac{3V}{4\pi}}$ c) $A(r(V)) = 4\pi \left(\frac{3V}{4\pi}\right)^{\frac{2}{3}}$

d)
$$4\pi \left(\frac{3(0.75)}{4\pi}\right)^{\frac{2}{3}} \doteq 4 \text{ m}^2$$



From the graph, the solution is $-1.62 \le x \le 1.62.$

3. Answers may vary. For example, $g(x) = x^7$ and h(x) = 2x + 3, $g(x) = (x + 3)^7$ and h(x) = 2x

4. a) $N(n) = 1n^3 + 8n^2 + 40n + 400$ b) N(3) = 619

5.
$$(f \times g)(x) = 30x^3 + 405x^2 + 714x - 4785$$

6. a) There is a horizontal asymptote of y = 275 cm. This is the maximum height this species will reach.
b) when t = 21.2 months

7. x = 4.5 or 4500 items



The solutions are x = -3.1, -1.4, -0.6, 0.5, or 3.2.

9. Division will turn it into a tangent function that is not sinusoidal.

Cumulative Review Chapters 7–9, pp. 580–583

1.	(d)	10.	(d)	19.	(c)	28.	(a)
2.	(b)	11.	(a)	20.	(d)	29.	(d)
3.	(a)	12.	(b)	21.	(b)	30.	(d)
4.	(a)	13.	(d)	22.	(a)	31.	(c)
5.	(d)	14.	(d)	23.	(c)	32.	(d)
6.	(c)	15.	(c)	24.	(c)	33.	(d)
7.	(d)	16.	(a)	25.	(c)	34.	(b)
8.	(b)	17.	(b)	26.	(b)		
9.	(c)	18.	(b)	27.	(a)		
35.	27° o	or 63°					

36. a) Answers may vary. For example, Niagara: $P(x) = (414.8)(1.0044^{x});$ Waterloo: $P(x) = (418.3)(1.0117^{x})$

- b) Answers may vary. For example, Niagara: 159 years; Waterloo: 60 years
- c) Answers may vary. For example, Waterloo is growing faster. In 2025, the instantaneous rate of change for the population in Waterloo is about 6800 people/year, compared to about 2000 people/year for Niagara.

37.
$$m(t) = 30\ 000\ -\ 100t,$$

 $a(t) = \frac{T}{30\ 000\ -\ 100t} -\ 10,$
 $v(t) = -\frac{\log\left(1-\frac{t}{300}\right)}{\log 2.72} - gt;$
 $at\ t = 0, \frac{T}{30\ 000} -\ 10$ must be greater than

0 m/s², so T must be greater than 300 000 kg \times m/s² (or 300 000 N)