

Study | Aid

and 5.3.

## **WORDS YOU NEED** to Know

- 1. State the vertex, equation of the axis of symmetry, and zeros of the parabola at the left.
- **2.** Match each form with the correct equation.
  - a) standard form
- i) y = -2(x+3)(x-1)
- **b)** factored form
- ii)  $y = -2(x+1)^2 + 8$
- **c)** vertex form
- iii)  $y = -2x^2 4x + 6$

# **SKILLS AND CONCEPTS** You Need

# **Graphing Quadratic Relations**

Different strategies can be used to graph a quadratic relation. The strategy you use might depend on the form of the relation.

#### • For more help and practice, see Lessons 5.6, 3.3, **EXAMPLE**

Describe a strategy you could use to graph each quadratic relation.

a) 
$$y = x^2 + 4x - 1$$

**b)** 
$$y = -2(x+3)(x-5)$$
 **c)**  $y = 2(x-3)^2 - 4$ 

c) 
$$y = 2(x-3)^2 - 4$$

### Solution

- The equation is in standard form.
  - Partially factor the equation to locate two ordered pairs with the same  $\gamma$ -coordinate.
  - Determine the *x*-coordinate of the vertex by calculating the mean of the *x*-coordinates of the points you determined above.
  - Substitute the *x*-coordinate of the vertex into the equation to determine the *y*-coordinate of the vertex.
  - Substitute two other values of *x* into the equation to determine two more points on the parabola.
  - Use symmetry to determine the points on the parabola that are directly across from the two additional points you determined.
  - Plot the vertex and points, then sketch the parabola.
- **b)** The equation is in factored form.
  - Locate the zeros by setting each factor to zero and solving each equation.
  - Determine the *x*-coordinate of the vertex by calculating the mean of the x-coordinates of the zeros that you determined above.
  - Substitute the *x*-coordinate of the vertex into the equation to determine the *y*-coordinate of the vertex.
  - Plot the vertex and zeros, then sketch the parabola.

- **c)** The equation is in vertex form.
  - Locate the vertex and the axis of symmetry.
  - Determine the *y*-intercept by letting *x* equal 0.
  - Use symmetry to determine the point on the parabola that is directly across from the  $\gamma$ -intercept.
  - Plot the vertex and points, then sketch the parabola.
  - **3.** Graph each quadratic relation.

a) 
$$y = (x + 4)^2 - 3$$

c) 
$$y = (x + 5)(x - 7)$$
 e)  $y = 2x^2 + x - 1$ 

e) 
$$y = 2x^2 + x - 1$$

**b)** 
$$y = -3(x-3)^2 - 1$$

**b)** 
$$y = -3(x-3)^2 - 1$$
 **d)**  $y = \frac{1}{2}(x-4)(x-7)$  **f)**  $y = -3x^2 - 5x$ 

$$\mathbf{f)} \ \ y = -3x^2 - 5x$$

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For more help and practice,

see Lessons 4.2 to 4.6.

## **Factoring Quadratic Expressions**

You can use a variety of strategies to factor a quadratic expression.

### **EXAMPLE**

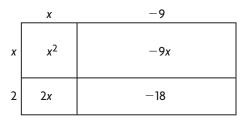
Factor. Use an area diagram for part a). Use decomposition for part b).

a) 
$$x^2 - 7x - 18$$

**b)** 
$$4x^2 + 8x - 5$$

### Solution

a) 
$$x^2 - 7x - 18$$



This is a trinomial where a = 1 and there are no common factors. Look for two binomials that each start with x. To determine the factors, find two numbers whose product is -18 and whose sum is -7. The numbers are -9 and 2.

$$x^2 - 7x - 18 = (x - 9)(x + 2)$$

**b)** 
$$4x^2 + 8x - 5$$
 =  $4x^2 - 2x + 10x - 5$ 

This is a trinomial where  $a \neq 1$  and there are no common factors. Look for two numbers whose sum is 8 and whose product is (4)(-5) = -20. The numbers are -2 and 10. Use these to decompose the middle term.

$$= \underbrace{4x^2 - 2x}_{= 2x(2x - 1)} + \underbrace{10x - 5}_{+ 5(2x - 1)}$$

Group the terms in pairs, and divide out the common factors.

= (2x - 1)(2x + 5)

Divide out the common binomial as a common factor.

**4.** Factor each expression, if possible.

a) 
$$x^2 + 8x + 12$$

c) 
$$x^2 + 7x - 30$$

c) 
$$x^2 + 7x - 30$$
  
d)  $9x^2 - 30x + 25$   
e)  $-6x^2 - 7x + 24$   
f)  $2x^2 - x - 5$ 

**b)** 
$$x^2 - 5x + 6$$

NEL

**d)** 
$$9x^2 - 30x + 25$$

f) 
$$2x^2 - x - 5$$

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• For help, see the Review of Essential Skills and Knowledge Appendix.

Question	Appendix	
5	A-9	

	Х	Х	-1	
х	x <sup>2</sup>	<i>x</i> <sup>2</sup>	- <b>x</b>	
-1	-х	х	1	
-1	<b>—</b> х	— <b>х</b>	1	
-1	<b>—</b> х	— <b>х</b>	1	

### **PRACTICE**

**5.** Solve each equation.

a) 
$$4x + 8 = 0$$

c) 
$$-2x + 12 = 0$$

**b)** 
$$5x - 3 = 0$$

**d)** 
$$12x + 7 = 0$$

**6.** Expand and simplify.

a) 
$$(3x - 5)(x -$$

a) 
$$(3x-5)(x-4)$$
 c)  $(2x+3)(4x-5)$  e)  $(3a+7)(3a+7)$ 

e) 
$$(3a + 7)(3a + 7)$$

**b)** 
$$(n+1)(n-1)$$

**b)** 
$$(n+1)(n-1)$$
 **d)**  $(7-3p)(2p+5)$  **f)**  $(6x-5)^2$ 

**f**) 
$$(6x - 5)^2$$

7. The algebra tiles at the left show  $2x^2 - 7x + 3$  and its factors. Determine the factors for each expression. Use algebra tiles or area diagrams, if you wish.

a) 
$$x^2 + 4x + 3$$

a) 
$$x^2 + 4x + 3$$
 c)  $3x^2 - 5x - 2$  e)  $2x^2 + 12x$   
b)  $x^2 - 8x + 16$  d)  $4x^2 - 9$  f)  $9x^2 - 6x + 1$ 

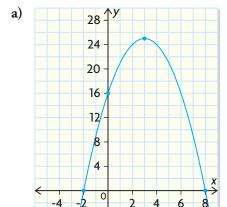
e) 
$$2x^2 + 12x$$

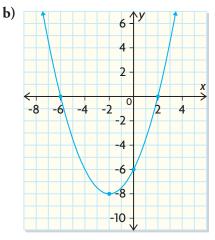
**b)** 
$$x^2 - 8x + 16$$

**d**) 
$$4x^2 - 9$$

f) 
$$9x^2 - 6x + 1$$

**8.** For each quadratic relation, determine the zeros, the y-intercept, the equation of the axis of symmetry, the vertex, and the equation in standard form.





**9.** For each quadratic relation, determine the y-intercept, the equation of the axis of symmetry, and the vertex.

a) 
$$y = (x - 4)(x + 6)$$

**b)** 
$$y = -4(x - 3)^2 - 5$$

- 10. Do you agree or disagree with each statement? Provide examples to support your answers.
  - a) Every quadratic expression can be written as the product of two linear factors.
  - **b)** Every quadratic relation has a maximum value or a minimum value.
  - **c)** The graph of a quadratic relation always has two *x*-intercepts.

# APPLYING What You Know

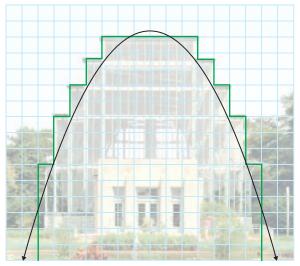
#### **YOU WILL NEED**

- grid paper
- ruler

#### The Jewel Box

This building is called the Jewel Box. It is a large greenhouse in St. Louis, Missouri. Its design is based on a parabola that passes through the corners of the roof line.





## What quadratic relations can be used to model this parabola?

- **A.** Trace the parabola from the photo at the right onto grid paper. Decide where to draw the *x* and *y*-axes.
- **B.** Create an algebraic model for the parabola in vertex form.
- **C.** Create an algebraic model for the parabola in factored form.
- **D.** How are the two models you created for parts B and C the same? How are they different?
- **E.** Write both of your models in standard form. Do all three models represent the same parabola? Explain.
- **F.** Which form of the quadratic relation do you prefer to model the shape of the roof line of the Jewel Box? Justify your answer.

NEL Chapter 6 313